

# $V_{cb}$ and $V_{ub}$ CKM Matrix Elements

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## $V_{cb}$ MEASUREMENTS

For the discussion of  $V_{cb}$  measurements, which is not repeated here, see the review on “Determination of  $|V_{cb}|$ .”

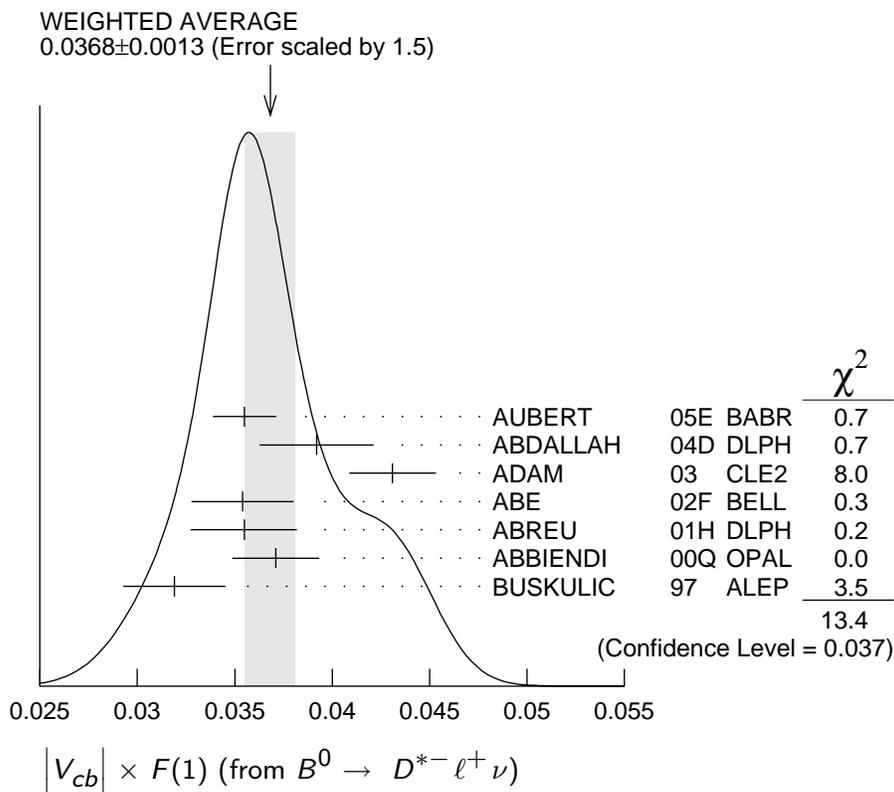
The CKM matrix element  $|V_{cb}|$  can be determined by studying the rate of the semileptonic decay  $B \rightarrow D^{(*)} \ell \nu$  as a function of the recoil kinematics of  $D^{(*)}$  mesons. Taking advantage of theoretical constraints on the normalization and a linear  $\omega$  dependence of the form factors provided by Heavy Quark Effective Theory (HQET), the  $|V_{cb}| \times F(\omega)$  and  $\rho^2$  ( $a^2$ ) can be simultaneously extracted from data, where  $\omega$  is the scalar product of the two-meson four velocities,  $F(1)$  is the form factor at zero recoil ( $\omega=1$ ) and  $\rho^2$  is the slope, sometimes denoted as  $a^2$ . Using the theoretical input of  $F(1)$ , a value of  $|V_{cb}|$  can be obtained.

“OUR EVALUATION” is an average using rescaled values of the data listed below. The average and rescaling were performed by the Heavy Flavor Averaging Group (HFAG) and are described at <http://www.slac.stanford.edu/xorg/hfag/>. The averaging/rescaling procedure takes into account corrections between the measurements.

### $|V_{cb}| \times F(1)$ (from $B^0 \rightarrow D^{*-} \ell^+ \nu$ )

VALUE	DOCUMENT ID	TECN	COMMENT
<b><math>0.0376 \pm 0.0009</math> OUR EVALUATION</b>	with $\rho^2=1.56 \pm 0.14$ and a correlation 0.59. The fitted $\chi^2$ is 30.4 for 14 degrees of freedom.		
<b><math>0.0368 \pm 0.0013</math> OUR AVERAGE</b>	Error includes scale factor of 1.5. See the ideogram below.		
$0.0355 \pm 0.0003 \pm 0.0016$	1 AUBERT	05E BABR	$e^+ e^- \rightarrow \Upsilon(4S)$
$0.0392 \pm 0.0018 \pm 0.0023$	2 ABDALLAH	04D DLPH	$e^+ e^- \rightarrow Z^0$
$0.0431 \pm 0.0013 \pm 0.0018$	3 ADAM	03 CLE2	$e^+ e^- \rightarrow \Upsilon(4S)$
$0.0354 \pm 0.0019 \pm 0.0018$	4 ABE	02F BELL	$e^+ e^- \rightarrow \Upsilon(4S)$
$0.0355 \pm 0.0014^{+0.0023}_{-0.0024}$	5 ABREU	01H DLPH	$e^+ e^- \rightarrow Z$
$0.0371 \pm 0.0010 \pm 0.0020$	6 ABBIENDI	00Q OPAL	$e^+ e^- \rightarrow Z$
$0.0319 \pm 0.0018 \pm 0.0019$	7 BUSKULIC	97 ALEP	$e^+ e^- \rightarrow Z$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
$0.0377 \pm 0.0011 \pm 0.0019$	8 ABDALLAH	04D DLPH	$e^+ e^- \rightarrow Z^0$
$0.0431 \pm 0.0013 \pm 0.0018$	9 BRIERE	02 CLE2	$e^+ e^- \rightarrow \Upsilon(4S)$
$0.0328 \pm 0.0019 \pm 0.0022$	ACKERSTAFF	97G OPAL	Repl. by ABBIENDI 00Q
$0.0350 \pm 0.0019 \pm 0.0023$	10 ABREU	96P DLPH	Repl. by ABREU 01H
$0.0351 \pm 0.0019 \pm 0.0020$	11 BARISH	95 CLE2	Repl. by ADAM 03
$0.0314 \pm 0.0023 \pm 0.0025$	BUSKULIC	95N ALEP	Repl. by BUSKULIC 97

- 1 Measurement using fully reconstructed  $D^*$  sample with a  $\rho^2 = 1.29 \pm 0.03 \pm 0.27$ .
- 2 Measurement using fully reconstructed  $D^*$  sample with a  $\rho^2 = 1.32 \pm 0.15 \pm 0.33$ .
- 3 Average of the  $B^0 \rightarrow D^*(2010)^- \ell^+ \nu$  and  $B^+ \rightarrow \bar{D}^*(2007) \ell^+ \nu$  modes with  $\rho^2 = 1.61 \pm 0.09 \pm 0.21$  and  $f_{+-} = 0.521 \pm 0.012$ .
- 4 Measured using exclusive  $B^0 \rightarrow D^*(892)^- e^+ \nu$  decays with  $\rho^2 = 1.35 \pm 0.17 \pm 0.19$  and a correlation of 0.91.
- 5 ABREU 01H measured using about 5000 partial reconstructed  $D^*$  sample with a  $\rho^2 = 1.34 \pm 0.14^{+0.24}_{-0.22}$ .
- 6 ABBIENDI 00Q: measured using both inclusively and exclusively reconstructed  $D^{*\pm}$  samples with a  $\rho^2 = 1.21 \pm 0.12 \pm 0.20$ . The statistical and systematic correlations between  $|V_{cb}| \times F(1)$  and  $\rho^2$  are 0.90 and 0.54 respectively.
- 7 BUSKULIC 97: measured using exclusively reconstructed  $D^{*\pm}$  with a  $a^2 = 0.31 \pm 0.17 \pm 0.08$ . The statistical correlation is 0.92.
- 8 Combines with previous partial reconstructed  $D^*$  measurement with a  $\rho^2 = 1.39 \pm 0.10 \pm 0.33$ .
- 9 BRIERE 02 result is based on the same analysis and data sample reported in ADAM 03.
- 10 ABREU 96P: measured using both inclusively and exclusively reconstructed  $D^{*\pm}$  samples.
- 11 BARISH 95: measured using both exclusive reconstructed  $B^0 \rightarrow D^{*-} \ell^+ \nu$  and  $B^+ \rightarrow D^{*0} \ell^+ \nu$  samples. They report their experiment's uncertainties  $\pm 0.0019 \pm 0.0018 \pm 0.0008$ , where the first error is statistical, the second is systematic, and the third is the uncertainty in the lifetimes. We combine the last two in quadrature.



## $|V_{cb}| \times F(1)$ (from $B \rightarrow D^- \ell^+ \nu$ )

VALUE DOCUMENT ID TECN COMMENT  
**0.0422 ± 0.0037 OUR EVALUATION** with  $\rho^2 = 1.15 \pm 0.16$  and a correlation of 0.91. The fitted  $\chi^2$  is 0.3 for 4 degrees of freedom.

### **0.039 ± 0.004 OUR AVERAGE**

0.0411 ± 0.0044 ± 0.0052      12 ABE      02E BELL     $e^+ e^- \rightarrow \Upsilon(4S)$

0.0416 ± 0.0047 ± 0.0037      13 BARTELT    99 CLE2     $e^+ e^- \rightarrow \Upsilon(4S)$

0.0278 ± 0.0068 ± 0.0065      14 BUSKULIC    97 ALEP     $e^+ e^- \rightarrow Z$

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.0337 ± 0.0044  $^{+0.0072}_{-0.0049}$       15 ATHANAS    97 CLE2    Repl. by BARTELT 99

<sup>12</sup> Using the missing energy and momentum to extract kinematic information about the undetected neutrino in the  $B^0 \rightarrow D^- \ell^+ \nu$  decay.

<sup>13</sup> BARTELT 99: measured using both exclusive reconstructed  $B^0 \rightarrow D^- \ell^+ \nu$  and  $B^+ \rightarrow D^0 \ell^+ \nu$  samples.

<sup>14</sup> BUSKULIC 97: measured using exclusively reconstructed  $D^\pm$  with a  $a^2 = -0.05 \pm 0.53 \pm 0.38$ . The statistical correlation is 0.99.

<sup>15</sup> ATHANAS 97: measured using both exclusive reconstructed  $B^0 \rightarrow D^- \ell^+ \nu$  and  $B^+ \rightarrow D^0 \ell^+ \nu$  samples with a  $\rho^2 = 0.59 \pm 0.22 \pm 0.12^{+0.59}_{-0}$ . They report their experiment's uncertainties  $\pm 0.0044 \pm 0.0048^{+0.0053}_{-0.0012}$ , where the first error is statistical, the second is systematic, and the third is the uncertainty due to the form factor model variations. We combine the last two in quadrature.

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## $V_{ub}$ MEASUREMENTS

For the discussion of  $V_{ub}$  measurements, which is not repeated here, see the review on “Determination of  $|V_{ub}|$ .”

The CKM matrix element  $|V_{ub}|$  can be determined by studying the rate of the charmless semileptonic decay  $b \rightarrow u \ell \nu$ . Measurements based on exclusive decay channels and on inclusive techniques can be found in the previous  $B$  Listings, which will not repeat here.

## $V_{cb}$ and $V_{ub}$ CKM Matrix Elements REFERENCES

AUBERT	05E PR D71 051502R	B. Aubert <i>et al.</i>	(BABAR Collab.)
ABDALLAH	04D EPJ C33 213	J. Abdallah <i>et al.</i>	(DELPHI Collab.)
ADAM	03 PR D67 032001	N.E. Adam <i>et al.</i>	(CLEO Collab.)
ABE	02E PL B526 258	K. Abe <i>et al.</i>	(BELLE Collab.)
ABE	02F PL B526 247	K. Abe <i>et al.</i>	(BELLE Collab.)
BRIERE	02 PRL 89 081803	R. Briere <i>et al.</i>	(CLEO Collab.)
ABREU	01H PL B510 55	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ABBIENDI	00Q PL B482 15	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
BARTELT	99 PRL 82 3746	J. Bartelt <i>et al.</i>	(CLEO Collab.)
ACKERSTAFF	97G PL B395 128	K. Ackerstaff <i>et al.</i>	(OPAL Collab.)
ATHANAS	97 PRL 79 2208	M. Athanas <i>et al.</i>	(CLEO Collab.)
BUSKULIC	97 PL B395 373	D. Buskulic <i>et al.</i>	(ALEPH Collab.)
ABREU	96P ZPHY C71 539	P. Abreu <i>et al.</i>	(DELPHI Collab.)
BARISH	95 PR D51 1014	B.C. Barish <i>et al.</i>	(CLEO Collab.)
BUSKULIC	95N PL B359 236	D. Buskulic <i>et al.</i>	(ALEPH Collab.)