

K \pm

$I(J^P) = \frac{1}{2}(0^-)$

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K \pm MASS

VALUE (MeV)	DOCUMENT ID	TECN	CHG	COMMENT
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493.677±0.016 OUR FIT Error includes scale factor of 2.8.

493.677±0.013 OUR AVERAGE Error includes scale factor of 2.4. See the ideogram below.

493.696±0.007	¹ DENISOV	91	CNTR	–	Kaonic atoms
493.636±0.011	² GALL	88	CNTR	–	Kaonic atoms
493.640±0.054	LUM	81	CNTR	–	Kaonic atoms
493.670±0.029	BARKOV	79	EMUL	±	$e^+ e^- \rightarrow K^+ K^-$
493.657±0.020	² CHENG	75	CNTR	–	Kaonic atoms
493.691±0.040	BACKENSTO...73	CNTR	–		Kaonic atoms

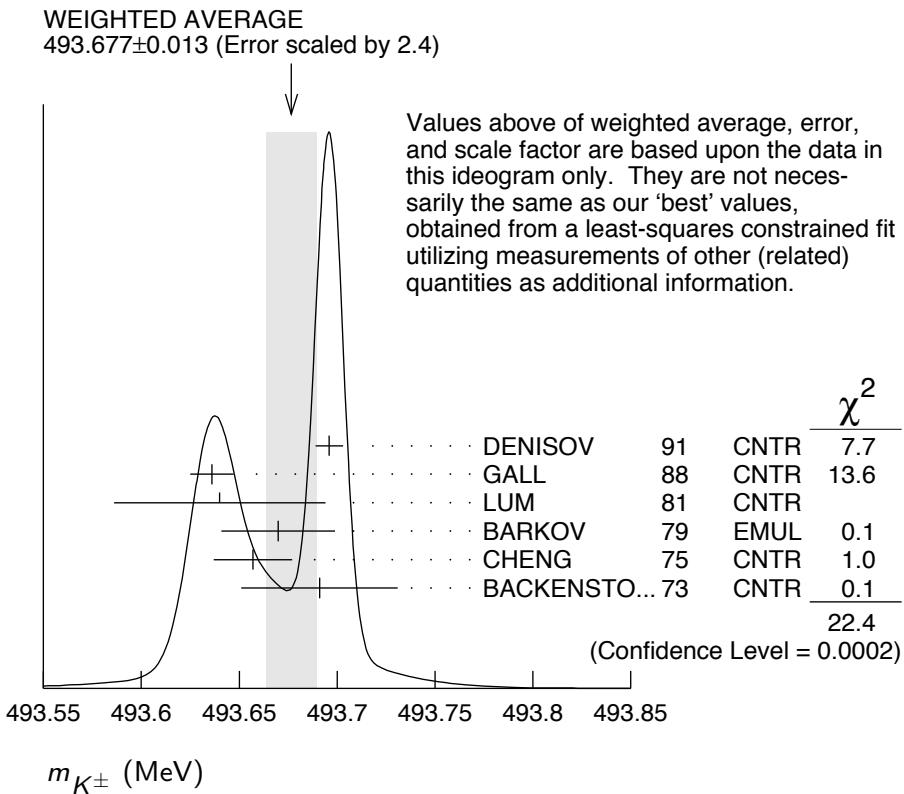
• • • We do not use the following data for averages, fits, limits, etc. • • •

493.631±0.007	GALL	88	CNTR	–	$K^- Pb (9 \rightarrow 8)$
493.675±0.026	GALL	88	CNTR	–	$K^- Pb (11 \rightarrow 10)$
493.709±0.073	GALL	88	CNTR	–	$K^- W (9 \rightarrow 8)$
493.806±0.095	GALL	88	CNTR	–	$K^- W (11 \rightarrow 10)$
493.640±0.022±0.008	³ CHENG	75	CNTR	–	$K^- Pb (9 \rightarrow 8)$
493.658±0.019±0.012	³ CHENG	75	CNTR	–	$K^- Pb (10 \rightarrow 9)$
493.638±0.035±0.016	³ CHENG	75	CNTR	–	$K^- Pb (11 \rightarrow 10)$
493.753±0.042±0.021	³ CHENG	75	CNTR	–	$K^- Pb (12 \rightarrow 11)$
493.742±0.081±0.027	³ CHENG	75	CNTR	–	$K^- Pb (13 \rightarrow 12)$

¹ Error increased from 0.0059 based on the error analysis in IVANOV 92.

² This value is the authors' combination of all of the separate transitions listed for this paper.

³ The CHENG 75 values for separate transitions were calculated from their Table 7 transition energies. The first error includes a 20% systematic error in the noncircular contaminant shift. The second error is due to a ±5 eV uncertainty in the theoretical transition energies.



$m_{K^+} - m_{K^-}$

Test of *CPT*.

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	CHG
-0.032±0.090	1.5M	⁴ FORD	72	ASPK ±

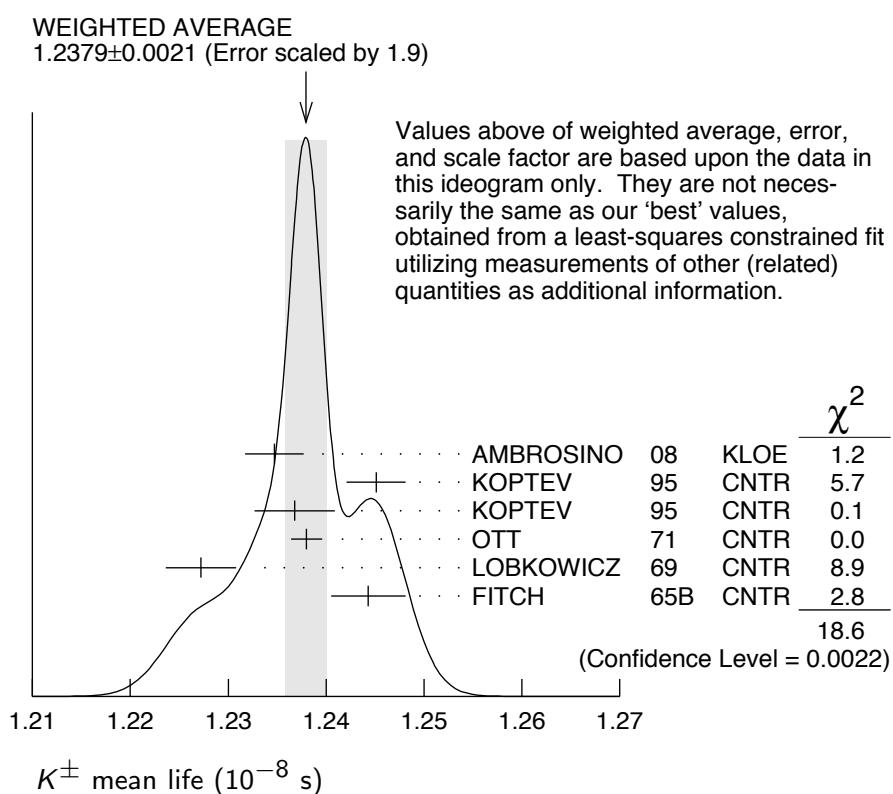
⁴FORD 72 uses $m_{\pi^+} - m_{\pi^-} = +28 \pm 70$ keV.

K^\pm MEAN LIFE

VALUE (10^{-8} s)	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
(1.2380±0.0021) OUR FIT		Error includes scale factor of 1.9.			
(1.2379±0.0021) OUR AVERAGE		Error includes scale factor of 1.9. See the ideogram below.			
1.2347±0.0030	15M	5 AMBROSINO	08	KLOE ±	$\phi \rightarrow K^+ K^-$
1.2451±0.0030	250k	KOPTEV	95	CNTR	K at rest, U target
1.2368±0.0041	150k	KOPTEV	95	CNTR	K at rest, Cu target
1.2380±0.0016	3M	OTT	71	CNTR +	K at rest
1.2272±0.0036		LOBKOWICZ	69	CNTR +	K in flight
1.2443±0.0038		FITCH	65B	CNTR +	K at rest
• • • We do not use the following data for averages, fits, limits, etc. • • •					
1.2415±0.0024	400k	⁶ KOPTEV	95	CNTR	K at rest
1.221 ±0.011		FORD	67	CNTR ±	
1.231 ±0.011		BOYARSKI	62	CNTR +	

⁵ Result obtained by averaging the decay length and decay time analyses taking correlations into account.

⁶ KOPTEV 95 report this weighted average of their U-target and Cu-target results, where they have weighted by $1/\sigma$ rather than $1/\sigma^2$.



$$(\tau_{K^+} - \tau_{K^-}) / \tau_{\text{average}}$$

This quantity is a measure of *CPT* invariance in weak interactions.

VALUE (%)	DOCUMENT ID	TECN
0.10 ± 0.09 OUR AVERAGE	Error includes scale factor of 1.2.	
-0.4 ± 0.4	AMBROSINO 08	KLOE
0.090 ± 0.078	LOBKOWICZ 69	CNTR
0.47 ± 0.30	FORD 67	CNTR

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K^+ DECAY MODES

K^- modes are charge conjugates of the modes below.

Mode	Fraction (Γ_i/Γ)	Scale factor/ Confidence level

Leptonic and semileptonic modes

Γ_1	$e^+ \nu_e$	$(1.584 \pm 0.020) \times 10^{-5}$	
Γ_2	$\mu^+ \nu_\mu$	$(63.55 \pm 0.11) \%$	S=1.2
Γ_3	$\pi^0 e^+ \nu_e$ Called K_{e3}^+ .	$(5.07 \pm 0.04) \%$	S=2.1
Γ_4	$\pi^0 \mu^+ \nu_\mu$ Called $K_{\mu 3}^+$.	$(3.353 \pm 0.034) \%$	S=1.8
Γ_5	$\pi^0 \pi^0 e^+ \nu_e$	$(2.2 \pm 0.4) \times 10^{-5}$	
Γ_6	$\pi^+ \pi^- e^+ \nu_e$	$(4.09 \pm 0.10) \times 10^{-5}$	
Γ_7	$\pi^+ \pi^- \mu^+ \nu_\mu$	$(1.4 \pm 0.9) \times 10^{-5}$	
Γ_8	$\pi^0 \pi^0 \pi^0 e^+ \nu_e$	$< 3.5 \times 10^{-6}$	CL=90%

Hadronic modes

Γ_9	$\pi^+ \pi^0$	$(20.66 \pm 0.08) \%$	S=1.2
Γ_{10}	$\pi^+ \pi^0 \pi^0$	$(1.761 \pm 0.022) \%$	S=1.1
Γ_{11}	$\pi^+ \pi^+ \pi^-$	$(5.59 \pm 0.04) \%$	S=1.3

Leptonic and semileptonic modes with photons

Γ_{12}	$\mu^+ \nu_\mu \gamma$	$[a,b] (6.2 \pm 0.8) \times 10^{-3}$	
Γ_{13}	$\mu^+ \nu_\mu \gamma (\text{SD}^+)$	$[c,d] (1.33 \pm 0.22) \times 10^{-5}$	
Γ_{14}	$\mu^+ \nu_\mu \gamma (\text{SD}^+ \text{INT})$	$[c,d] < 2.7 \times 10^{-5}$	CL=90%
Γ_{15}	$\mu^+ \nu_\mu \gamma (\text{SD}^- + \text{SD}^- \text{INT})$	$[c,d] < 2.6 \times 10^{-4}$	CL=90%
Γ_{16}	$e^+ \nu_e \gamma$	$(9.4 \pm 0.4) \times 10^{-6}$	
Γ_{17}	$\pi^0 e^+ \nu_e \gamma$	$[a,b] (2.56 \pm 0.16) \times 10^{-4}$	
Γ_{18}	$\pi^0 e^+ \nu_e \gamma (\text{SD})$	$[c,d] < 5.3 \times 10^{-5}$	CL=90%
Γ_{19}	$\pi^0 \mu^+ \nu_\mu \gamma$	$[a,b] (1.25 \pm 0.25) \times 10^{-5}$	
Γ_{20}	$\pi^0 \pi^0 e^+ \nu_e \gamma$	$< 5 \times 10^{-6}$	CL=90%

Hadronic modes with photons or $\ell\bar{\ell}$ pairs

Γ_{21}	$\pi^+ \pi^0 \gamma (\text{INT})$	$(-4.2 \pm 0.9) \times 10^{-6}$	
Γ_{22}	$\pi^+ \pi^0 \gamma (\text{DE})$	$[a,e] (6.0 \pm 0.4) \times 10^{-6}$	
Γ_{23}	$\pi^+ \pi^0 \pi^0 \gamma$	$[a,b] (7.6 \pm 6.0) \times 10^{-6}$	
Γ_{24}	$\pi^+ \pi^+ \pi^- \gamma$	$[a,b] (1.04 \pm 0.31) \times 10^{-4}$	
Γ_{25}	$\pi^+ \gamma \gamma$	$[a] (1.10 \pm 0.32) \times 10^{-6}$	
Γ_{26}	$\pi^+ 3\gamma$	$[a] < 1.0 \times 10^{-4}$	CL=90%
Γ_{27}	$\pi^+ e^+ e^- \gamma$	$(1.19 \pm 0.13) \times 10^{-8}$	

Leptonic modes with $\ell\bar{\ell}$ pairs

Γ_{28}	$e^+ \nu_e \nu \bar{\nu}$	$< 6 \times 10^{-5}$	CL=90%
Γ_{29}	$\mu^+ \nu_\mu \nu \bar{\nu}$	$< 6.0 \times 10^{-6}$	CL=90%
Γ_{30}	$e^+ \nu_e e^+ e^-$	$(2.48 \pm 0.20) \times 10^{-8}$	
Γ_{31}	$\mu^+ \nu_\mu e^+ e^-$	$(7.06 \pm 0.31) \times 10^{-8}$	
Γ_{32}	$e^+ \nu_e \mu^+ \mu^-$	$(1.7 \pm 0.5) \times 10^{-8}$	
Γ_{33}	$\mu^+ \nu_\mu \mu^+ \mu^-$	$< 4.1 \times 10^{-7}$	CL=90%

**Lepton Family number (*LF*), Lepton number (*L*), $\Delta S = \Delta Q$ (*SQ*)
violating modes, or $\Delta S = 1$ weak neutral current (*S1*) modes**

Γ_{34}	$\pi^+ \pi^+ e^- \bar{\nu}_e$	<i>SQ</i>	<	1.2	$\times 10^{-8}$	CL=90%	
Γ_{35}	$\pi^+ \pi^+ \mu^- \bar{\nu}_\mu$	<i>SQ</i>	<	3.0	$\times 10^{-6}$	CL=95%	
Γ_{36}	$\pi^+ e^+ e^-$	<i>S1</i>	(3.00 ± 0.09) $\times 10^{-7}$		
Γ_{37}	$\pi^+ \mu^+ \mu^-$	<i>S1</i>	(9.4 ± 0.6) $\times 10^{-8}$	S=2.6	
Γ_{38}	$\pi^+ \nu \bar{\nu}$	<i>S1</i>	(1.7 ± 1.1) $\times 10^{-10}$		
Γ_{39}	$\pi^+ \pi^0 \nu \bar{\nu}$	<i>S1</i>	<	4.3	$\times 10^{-5}$	CL=90%	
Γ_{40}	$\mu^- \nu e^+ e^+$	<i>LF</i>	<	2.0	$\times 10^{-8}$	CL=90%	
Γ_{41}	$\mu^+ \nu_e$	<i>LF</i>	[f]	<	4	$\times 10^{-3}$	CL=90%
Γ_{42}	$\pi^+ \mu^+ e^-$	<i>LF</i>	<	1.3	$\times 10^{-11}$	CL=90%	
Γ_{43}	$\pi^+ \mu^- e^+$	<i>LF</i>	<	5.2	$\times 10^{-10}$	CL=90%	
Γ_{44}	$\pi^- \mu^+ e^+$	<i>L</i>	<	5.0	$\times 10^{-10}$	CL=90%	
Γ_{45}	$\pi^- e^+ e^+$	<i>L</i>	<	6.4	$\times 10^{-10}$	CL=90%	
Γ_{46}	$\pi^- \mu^+ \mu^+$	<i>L</i>	[f]	<	1.1	$\times 10^{-9}$	CL=90%
Γ_{47}	$\mu^+ \bar{\nu}_e$	<i>L</i>	[f]	<	3.3	$\times 10^{-3}$	CL=90%
Γ_{48}	$\pi^0 e^+ \bar{\nu}_e$	<i>L</i>	<	3	$\times 10^{-3}$	CL=90%	
Γ_{49}	$\pi^+ \gamma$	[g]	<	2.3	$\times 10^{-9}$	CL=90%	

[a] See the Particle Listings below for the energy limits used in this measurement.

[b] Most of this radiative mode, the low-momentum γ part, is also included in the parent mode listed without γ 's.

[c] Structure-dependent part.

[d] See the “Note on $\pi^\pm \rightarrow \ell^\pm \nu \gamma$ and $K^\pm \rightarrow \ell^\pm \nu \gamma$ Form Factors” in the π^\pm Particle Listings for definitions and details.

[e] Direct-emission branching fraction.

[f] Derived from an analysis of neutrino-oscillation experiments.

[g] Violates angular-momentum conservation.

CONSTRAINED FIT INFORMATION

An overall fit to the mean life, a decay rate, and 13 branching ratios uses 32 measurements and one constraint to determine 8 parameters. The overall fit has a $\chi^2 = 51.8$ for 25 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients $\langle \delta p_i \delta p_j \rangle / (\delta p_i \cdot \delta p_j)$, in percent, from the fit to parameters p_i , including the branching fractions, $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$. The fit constrains the x_i whose labels appear in this array to sum to one.

x_3	-64						
x_4	-62 90						
x_5	-3 4 3						
x_9	-65	1	-1	0			
x_{10}	-13	-6	-6	0	-6		
x_{11}	-21	-9	-9	0	-10	3	
Γ	5	2	2	0	2	-1	-24
	x_2	x_3	x_4	x_5	x_9	x_{10}	x_{11}

	Mode	Rate (10^8 s^{-1})	Scale factor
Γ_2	$\mu^+ \nu_\mu$	0.5133 ± 0.0013	1.5
Γ_3	$\pi^0 e^+ \nu_e$ Called K_{e3}^+ .	0.0410 ± 0.0004	2.1
Γ_4	$\pi^0 \mu^+ \nu_\mu$ Called $K_{\mu 3}^+$.	0.02708 ± 0.00028	1.9
Γ_5	$\pi^0 \pi^0 e^+ \nu_e$	$(1.77 \quad {}^{+0.35}_{-0.30}) \times 10^{-5}$	
Γ_9	$\pi^+ \pi^0$	0.1669 ± 0.0007	1.3
Γ_{10}	$\pi^+ \pi^0 \pi^0$	0.01423 ± 0.00018	1.1
Γ_{11}	$\pi^+ \pi^+ \pi^-$	0.04518 ± 0.00029	1.2

K^\pm DECAY RATES

$\Gamma(\mu^+ \nu_\mu)$

Γ_2

VALUE (10^6 s^{-1}) DOCUMENT ID TECN CHG

51.33 \pm 0.13 OUR FIT Error includes scale factor of 1.5.

• • • We do not use the following data for averages, fits, limits, etc. • • •

51.2 \pm 0.8

FORD 67 CNTR \pm

$\Gamma(\pi^+ \pi^+ \pi^-)$

Γ_{11}

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
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(4.518±0.029) OUR FIT Error includes scale factor of 1.2.

4.511±0.024 ⁷ FORD 70 ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.529 ± 0.032 3.2M ⁷ FORD 70 ASPK

4.496 ± 0.030 ⁷ FORD 67 CNTR ±

⁷ First FORD 70 value is second FORD 70 combined with FORD 67.

$(\Gamma(K^+) - \Gamma(K^-)) / \Gamma(K)$

$K^\pm \rightarrow \mu^\pm \nu_\mu$ RATE DIFFERENCE/AVERAGE

Test of *CPT* conservation.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
-0.54±0.41		FORD	67	CNTR

$K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ RATE DIFFERENCE/AVERAGE

Test of *CP* conservation.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
0.08±0.12		⁸ FORD	70	ASPK
-0.02±0.16		⁹ SMITH	73	ASPK ±
0.10±0.14	3.2M	⁸ FORD	70	ASPK
-0.50±0.90		FLETCHER	67	OSPK
-0.04±0.21		⁸ FORD	67	CNTR

⁸ First FORD 70 value is second FORD 70 combined with FORD 67.

⁹ SMITH 73 value of $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ rate difference is derived from SMITH 73 value of $K^\pm \rightarrow \pi^\pm 2\pi^0$ rate difference.

$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ RATE DIFFERENCE/AVERAGE

Test of *CP* conservation.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
0.0 ±0.6 OUR AVERAGE				
0.08±0.58		SMITH	73	ASPK ±
-1.1 ±1.8	1802	HERZO	69	OSPK

$K^\pm \rightarrow \pi^\pm \pi^0$ RATE DIFFERENCE/AVERAGE

Test of *CPT* conservation.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
0.8±1.2		HERZO	69	OSPK

$K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ RATE DIFFERENCE/AVERAGE

Test of *CP* conservation.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>	<u>COMMENT</u>
0.9±3.3 OUR AVERAGE					
0.8±5.8	2461	SMITH	76	WIRE ±	E_π 55–90 MeV
1.0±4.0	4000	ABRAMS	73B	ASPK ±	E_π 51–100 MeV

K^+ BRANCHING RATIOS

Leptonic and semileptonic modes

$\Gamma(e^+\nu_e)/\Gamma(\mu^+\nu_\mu)$

Γ_1/Γ_2

See the note on "Decay Constants of Charged Pseudoscalar Mesons" in the D_s^+ Listings.

VALUE (units 10^{-5})	EVTS	DOCUMENT ID	TECN	CHG
2.493±0.025±0.019	13.8K	10 AMBROSINO 09E	KLOE	±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.51 ± 0.15	404	HEINTZE	76	SPEC +
2.37 ± 0.17	534	HEARD	75B	SPEC +
2.42 ± 0.42	112	CLARK	72	OSPK +

¹⁰ The ratio is defined to include internal-bremsstrahlung, ignoring direct-emission contributions. AMBROSINO 09E determined the ratio from the measurement of $\Gamma(K \rightarrow e\nu(\gamma), E_\gamma < 10 \text{ MeV}) / \Gamma(K \rightarrow \mu\nu(\gamma))$. 89.8% of $K \rightarrow e\nu(\gamma)$ events had $E_\gamma < 10 \text{ MeV}$.

$\Gamma(\mu^+\nu_\mu)/\Gamma_{\text{total}}$

Γ_2/Γ

See the note on "Decay Constants of Charged Pseudoscalar Mesons" in the D_s^+ Listings.

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
63.55±0.11 OUR FIT					Error includes scale factor of 1.2.
63.60±0.16 OUR AVERAGE					
63.66±0.09±0.15	865k	11 AMBROSINO 06A	KLOE	+	
63.24±0.44	62k	CHIANG	72	OSPK +	1.84 GeV/c K^+

¹¹ Fully inclusive. Used tagged kaons from ϕ decays.

$\Gamma(\pi^0e^+\nu_e)/\Gamma_{\text{total}}$

Γ_3/Γ

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
5.07 ±0.04 OUR FIT					Error includes scale factor of 2.1.
4.94 ±0.05 OUR AVERAGE					
4.965±0.038±0.037		12 AMBROSINO 08A	KLOE	±	
4.86 ± 0.10	3516	CHIANG	72	OSPK +	1.84 GeV/c K^+

^{• • •} We do not use the following data for averages, fits, limits, etc. ^{• • •}

4.7 ± 0.3	429	SHAKLEE	64	HLBC +
5.0 ± 0.5		ROE	61	HLBC +

¹² Depends on K^+ lifetime τ . AMBROSINO 08A uses PDG 06 value of $\tau = (1.2385 \pm 0.0024) \times 10^{-8} \text{ sec}$. The correlation between K_{e3}^+ and $K_{\mu3}^+$ branching fraction measurements is 62.7%.

$\Gamma(\pi^0e^+\nu_e)/\Gamma(\mu^+\nu_\mu)$

Γ_3/Γ_2

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.0798±0.0008 OUR FIT				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.069 ± 0.006	350	ZELLER	69	ASPK +
0.0775±0.0033	960	BOTTERILL	68C	ASPK +
0.069 ± 0.006	561	GARLAND	68	OSPK +
0.0791±0.0054	295	13 AUERBACH	67	OSPK +

¹³ AUERBACH 67 changed from 0.0797 ± 0.0054 . See comment with ratio $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\mu^+ \nu_\mu)$. The value 0.0785 ± 0.0025 given in AUERBACH 67 is an average of AUERBACH 67 $\Gamma(\pi^0 e^+ \nu_e)/\Gamma(\mu^+ \nu_\mu)$ and CESTER 66 $\Gamma(\pi^0 e^+ \nu_e)/[\Gamma(\mu^+ \nu_\mu) + \Gamma(\pi^+ \pi^0)]$.

$\Gamma(\pi^0 e^+ \nu_e)/[\Gamma(\mu^+ \nu_\mu) + \Gamma(\pi^+ \pi^0)]$

$\Gamma_3/(\Gamma_2+\Gamma_9)$

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
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6.02±0.06 OUR FIT Error includes scale factor of 2.1.

6.02±0.15 OUR AVERAGE

6.16±0.22	5110	ESCHSTRUTH 68	OSPK	+
5.89±0.21	1679	CESTER 66	OSPK	+
• • • We do not use the following data for averages, fits, limits, etc. • • •				
5.92±0.65		14 WEISSENBERG 76	SPEC	+

¹⁴ Value calculated from WEISSENBERG 76 ($\pi^0 e\nu$), ($\mu\nu$), and ($\pi\pi^0$) values to eliminate dependence on our 1974 ($\pi 2\pi^0$) and ($\pi\pi^+\pi^-$) fractions.

$\Gamma(\pi^0 e^+ \nu_e)/[\Gamma(\pi^0 \mu^+ \nu_\mu) + \Gamma(\pi^+ \pi^0) + \Gamma(\pi^+ \pi^0 \pi^0)]$

$\Gamma_3/(\Gamma_4+\Gamma_9+\Gamma_{10})$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.1968±0.0016 OUR FIT		Error includes scale factor of 2.4.		
0.1962±0.0008±0.0035	71k	SHER	03	B865

$\Gamma(\pi^0 e^+ \nu_e)/\Gamma(\pi^+ \pi^0)$

Γ_3/Γ_9

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
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0.2455±0.0023 OUR FIT Error includes scale factor of 2.6.

0.2470±0.0009±0.0004 87k BATLEY 07A NA48 ±

• • • We do not use the following data for averages, fits, limits, etc. **• • •**

0.221 ± 0.012 786 ¹⁵ LUCAS 73B HBC – Dalitz pairs only

¹⁵ LUCAS 73B gives $N(K_{e3}) = 786 \pm 3.1\%$, $N(2\pi) = 3564 \pm 3.1\%$. We use these values to obtain quoted result.

$\Gamma(\pi^0 e^+ \nu_e)/\Gamma(\pi^+ \pi^+ \pi^-)$

Γ_3/Γ_{11}

VALUE	EVTS	DOCUMENT ID	TECN	CHG
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0.907±0.010 OUR FIT Error includes scale factor of 1.6.

• • • We do not use the following data for averages, fits, limits, etc. **• • •**

0.867±0.027	2768	BARMIN	87	XEBC	+
0.856±0.040	2827	BRAUN	75	HLBC	+
0.850±0.019	4385	¹⁶ HAIDT	71	HLBC	+
0.846±0.021	4385	¹⁶ EICHTEN	68	HLBC	+
0.94 ± 0.09	854	BELLOTTI	67B	HLBC	
0.90 ± 0.06	230	BORREANI	64	HBC	+

¹⁶ HAIDT 71 is a reanalysis of EICHTEN 68. Not included in average because of large discrepancy in $\Gamma(\pi^0 \mu^+ \nu)/\Gamma(\pi^0 e^+ \nu)$ with more precise results.

$\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma_{\text{total}}$ Γ_4/Γ

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
3.353±0.034 OUR FIT		Error includes scale factor of 1.8.			
3.24 ±0.04 OUR AVERAGE					
3.233±0.029±0.026	17	AMBROSINO 08A	KLOE	±	
3.33 ±0.16	2345	CHIANG 72	OSPK	+	1.84 GeV/c K^+
• • • We do not use the following data for averages, fits, limits, etc. • • •					
2.8 ±0.4	18	TAYLOR 59	EMUL	+	
17 Depends on K^+ lifetime τ . AMBROSINO 08A uses PDG 06 value of $\tau = (1.2385 \pm 0.0024) \times 10^{-8}$ sec. The correlation between K_{e3}^+ and $K_{\mu 3}^+$ branching fraction measurements is 62.7%.					
18 Earlier experiments not averaged.					

 $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\mu^+ \nu_\mu)$ Γ_4/Γ_2

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.0528±0.0006 OUR FIT		Error includes scale factor of 1.8.			
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.054 ±0.009	240	ZELLER 69	ASPK	+	
0.0480±0.0037	424	19 GARLAND 68	OSPK	+	
0.0486±0.0040	307	20 AUERBACH 67	OSPK	+	
19 GARLAND 68 changed from 0.055 ± 0.004 in agreement with μ -spectrum calculation of GAILLARD 70 appendix B. L.G.Pondrom, (private communication 73).					
20 AUERBACH 67 changed from 0.0602 ± 0.0046 by erratum which brings the μ -spectrum calculation into agreement with GAILLARD 70 appendix B.					

 $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\pi^0 e^+ \nu_e)$ Γ_4/Γ_3

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.6608±0.0030 OUR FIT		Error includes scale factor of 1.1.			
0.6618±0.0027 OUR AVERAGE					
0.663 ±0.003 ±0.001	77k	BATLEY 07A	NA48	±	
0.671 ±0.007 ±0.008	24k	HORIE 01	SPEC		
0.670 ±0.014	22	HEINTZE 77	SPEC	+	
0.667 ±0.017	5601	BOTTERILL 68B	ASPK	+	
• • • We use the following data for averages but not for fits. • • •					
0.6511±0.0064	21	AMBROSINO 08A	KLOE	±	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.608 ±0.014	1585	23 BRAUN 75	HLBC	+	
0.705 ±0.063	554	24 LUCAS 73B	HBC	–	Dalitz pairs only
0.698 ±0.025	3480	25 CHIANG 72	OSPK	+	1.84 GeV/c K^+
0.596 ±0.025		26 HAIDT 71	HLBC	+	
0.604 ±0.022	1398	26 EICHTEN 68	HLBC		
0.703 ±0.056	1509	CALLAHAN 66B	HLBC		

21 Not used in the fit. This result enters the fit via correlation of K_{e3}^+ and $K_{\mu 3}^+$ branching fraction measurements of AMBROSINO 08A.

22 HEINTZE 77 value from fit to λ_0 . Assumes μ -e universality.

23 BRAUN 75 value is from form factor fit. Assumes μ -e universality.

24 LUCAS 73B gives $N(K_{\mu 3}) = 554 \pm 7.6\%$, $N(K_{e3}) = 786 \pm 3.1\%$. We divide.

25 CHIANG 72 $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\pi^0 e^+ \nu_e)$ is statistically independent of CHIANG 72 $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma_{\text{total}}$ and $\Gamma(\pi^0 e^+ \nu_e)/\Gamma_{\text{total}}$.

26 HAIDT 71 is a reanalysis of EICHTEN 68. Not included in average because of large discrepancy with more precise results.

$[\Gamma(\pi^0 \mu^+ \nu_\mu) + \Gamma(\pi^+ \pi^0)]/\Gamma_{\text{total}}$

$(\Gamma_4 + \Gamma_9)/\Gamma$

We combine these two modes for experiments measuring them in xenon bubble chamber because of difficulties of separating them there.

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
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24.02±0.08 OUR FIT Error includes scale factor of 1.2.

• • • We do not use the following data for averages, fits, limits, etc. • • •

25.4 ± 0.9	886	SHAKLEE	64	HLBC	+
23.4 ± 1.1		ROE	61	HLBC	+

$\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\pi^+ \pi^0)$

Γ_4/Γ_9

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.1637±0.0006±0.0003	77k	BATLEY	07A	NA48

$\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\pi^+ \pi^+ \pi^-)$

Γ_4/Γ_{11}

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.599±0.007 OUR FIT					Error includes scale factor of 1.6.

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.503±0.019	1505	27 HAIDT	71	HLBC	+
0.510±0.017	1505	27 EICHTEN	68	HLBC	+
0.63 ± 0.07	2845	28 BISI	65B	BC	+

27 HAIDT 71 is a reanalysis of EICHTEN 68. Not included in average because of large discrepancy in $\Gamma(\pi^0 \mu^+ \nu)/\Gamma(\pi^0 e^+ \nu)$ with more precise results.

28 Error enlarged for background problems. See GAILLARD 70.

$\Gamma(\pi^0 \pi^0 e^+ \nu_e)/\Gamma_{\text{total}}$

Γ_5/Γ

VALUE (units 10^{-5})	EVTS	DOCUMENT ID	TECN	CHG
(2.2+0.4) OUR FIT				
2.54±0.89	10	BARMIN	88B	HLBC

$\Gamma(\pi^0 \pi^0 e^+ \nu_e)/\Gamma(\pi^0 e^+ \nu_e)$

Γ_5/Γ_3

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN	CHG
(4.3+0.9-0.7) OUR FIT				
(4.1+1.0-0.7) OUR AVERAGE				

4.2 ± 1.0 -0.9	25	BOLOTOV	86B	CALO	-
3.8 ± 5.0 -1.2	2	LJUNG	73	HLBC	+

$\Gamma(\pi^+ \pi^- e^+ \nu_e)/\Gamma(\pi^+ \pi^+ \pi^-)$

Γ_6/Γ_{11}

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN	CHG
(7.31+0.16) OUR AVERAGE				

7.35±0.01±0.19	388k	29 PISLAK	01	B865
7.21±0.32	30k	ROSSELET	77	SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.36±0.68	500	BOURQUIN	71	ASPK
7.0 ± 0.9	106	SCHWEINB...	71	HLBC
5.83±0.63	269	ELY	69	HLBC

²⁹ PISLAK 01 reports $\Gamma(\pi^+ \pi^- e^+ \nu_e)/\Gamma_{\text{total}} = (4.109 \pm 0.008 \pm 0.110) \times 10^{-5}$ using the PDG 00 value $\Gamma(\pi^+ \pi^+ \pi^-)/\Gamma_{\text{total}} = (5.59 \pm 0.05) \times 10^{-2}$. We divide by the PDG value and unfold its error from the systematic error. PISLAK 03 and PISLAK 10A give additional details on the branching ratio measurement and give improved errors on the S-wave $\pi\pi$ scattering length: $a_0^0 = 0.235 \pm 0.013$ and $a_0^2 = -0.0410 \pm 0.0027$.

$\Gamma(\pi^+ \pi^- \mu^+ \nu_\mu)/\Gamma_{\text{total}}$ Γ_7/Γ

<u>VALUE</u> (units 10^{-5})	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
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• • • We do not use the following data for averages, fits, limits, etc. • • •

$0.77^{+0.54}_{-0.50}$	1	CLINE	65	FBC +
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$\Gamma(\pi^+ \pi^- \mu^+ \nu_\mu)/\Gamma(\pi^+ \pi^+ \pi^-)$ Γ_7/Γ_{11}

<u>VALUE</u> (units 10^{-4})	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
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2.57 ± 1.55	7	BISI	67	DBC +
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• • • We do not use the following data for averages, fits, limits, etc. • • •

~ 2.5	1	GREINER	64	EMUL +
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$\Gamma(\pi^0 \pi^0 \pi^0 e^+ \nu_e)/\Gamma_{\text{total}}$ Γ_8/Γ

<u>VALUE</u> (units 10^{-6})	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
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<3.5	90	0	BOLOTOV	88	SPEC –
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<9	90	0	BARMIN	92	XEBC +
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———— Hadronic modes ————

$\Gamma(\pi^+ \pi^0)/\Gamma_{\text{total}}$ Γ_9/Γ

<u>VALUE</u> (units 10^{-2})	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>	<u>COMMENT</u>
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20.66 ± 0.08 OUR FIT Error includes scale factor of 1.2.

20.70 ± 0.16 OUR AVERAGE Error includes scale factor of 1.8.

$20.65 \pm 0.05 \pm 0.08$	1.4M	30 AMBROSINO	08E	KLOE +	$\phi \rightarrow K^+ K^-$
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21.18 ± 0.28	16k	CHIANG	72	OSPK +	$1.84 \text{ GeV}/c K^+$
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• • • We do not use the following data for averages, fits, limits, etc. • • •

21.0 ± 0.6	CALLAHAN	65	HLBC	See Γ_9/Γ_{11}
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³⁰ Fully inclusive of final-state radiation. The branching ratio is evaluated using K^+ lifetime, $\tau = 12.385$ ns.

$\Gamma(\pi^+ \pi^0)/\Gamma(\pi^+ \pi^+ \pi^-)$ Γ_9/Γ_{11}

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
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3.694 ± 0.029 OUR FIT Error includes scale factor of 1.2.

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.96 ± 0.15	1045	CALLAHAN	66	FBC +
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$\Gamma(\pi^+ \pi^0)/\Gamma(\mu^+ \nu_\mu)$

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT	Γ_9/Γ_2
0.3252±0.0016 OUR FIT		Error includes scale factor of 1.2.				
0.3325±0.0032 OUR AVERAGE						
0.3329±0.0047±0.0010	45k	USHER	92	SPEC	+	$p\bar{p}$ at rest
0.3355±0.0057		³¹ WEISSENBE...	76	SPEC	+	
0.3277±0.0065	4517	³² AUERBACH	67	OSPK	+	
• • • We do not use the following data for averages, fits, limits, etc. • • •						
0.328 ± 0.005	25k	³¹ WEISSENBE...	74	STRC	+	
0.305 ± 0.018	1600	ZELLER	69	ASPK	+	

³¹ WEISSENBERG 76 revises WEISSENBERG 74.

³² AUERBACH 67 changed from 0.3253 ± 0.0065. See comment with ratio $\Gamma(\pi^0 \mu^+ \nu_\mu)/\Gamma(\mu^+ \nu_\mu)$.

$\Gamma(\pi^+ \pi^0 \pi^0)/\Gamma_{\text{total}}$

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT	Γ_{10}/Γ
1.761±0.022 OUR FIT		Error includes scale factor of 1.1.				
1.775±0.028 OUR AVERAGE		Error includes scale factor of 1.2.				
1.763±0.013±0.022		ALOISIO	04A	KLOE	±	
1.84 ± 0.06	1307	CHIANG	72	OSPK	+	1.84 GeV/c K^+
• • • We do not use the following data for averages, fits, limits, etc. • • •						
1.53 ± 0.11	198	³³ PANDOULAS	70	EMUL	+	
1.8 ± 0.2	108	SHAKLEE	64	HLBC	+	
1.7 ± 0.2		ROE	61	HLBC	+	
1.5 ± 0.2		³⁴ TAYLOR	59	EMUL	+	

³³ Includes events of TAYLOR 59.

³⁴ Earlier experiments not averaged.

$\Gamma(\pi^+ \pi^0 \pi^0)/\Gamma(\pi^+ \pi^0)$

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT	Γ_{10}/Γ_9
0.0852±0.0011 OUR FIT		Error includes scale factor of 1.1.				
• • • We do not use the following data for averages, fits, limits, etc. • • •						
0.081 ± 0.005	574	³⁵ LUCAS	73B	HBC	-	Dalitz pairs only
35 LUCAS 73B gives $N(\pi^0 \pi^0) = 574 \pm 5.9\%$, $N(2\pi) = 3564 \pm 3.1\%$. We quote $0.5N(\pi^0 \pi^0)/N(2\pi)$ where 0.5 is because only Dalitz pair π^0 's were used.						

$\Gamma(\pi^+ \pi^0 \pi^0)/\Gamma(\pi^+ \pi^+ \pi^-)$

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT	Γ_{10}/Γ_{11}
0.315±0.004 OUR FIT		Error includes scale factor of 1.1.				
0.303±0.009	2027	BISI	65	BC	+	HBC+HLBC
• • • We do not use the following data for averages, fits, limits, etc. • • •						
0.393±0.099	17	YOUNG	65	EMUL	+	

$\Gamma(\pi^+\pi^+\pi^-)/\Gamma_{\text{total}}$

Γ_{11}/Γ

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
5.59±0.04 OUR FIT		Error includes scale factor of 1.3.			
• • • We do not use the following data for averages, fits, limits, etc. • • •					
5.56±0.20	2330	36 CHIANG	72 OSPK	+	1.84 GeV/c K^+
5.34±0.21	693	37 PANDOULAS	70 EMUL	+	
5.71±0.15		DEMARCO	65 HBC		
6.0 ±0.4	44	YOUNG	65 EMUL	+	
5.54±0.12	2332	CALLAHAN	64 HLBC	+	
5.1 ±0.2	540	SHAKLEE	64 HLBC	+	
5.7 ±0.3		ROE	61 HLBC	+	

³⁶ Value is not independent of CHIANG 72 $\Gamma(\mu^+\nu_\mu)/\Gamma_{\text{total}}$, $\Gamma(\pi^+\pi^0)/\Gamma_{\text{total}}$, $\Gamma(\pi^+\pi^0\pi^0)/\Gamma_{\text{total}}$, $\Gamma(\pi^0\mu^+\nu_\mu)/\Gamma_{\text{total}}$, and $\Gamma(\pi^0e^+\nu_e)/\Gamma_{\text{total}}$.

³⁷ Includes events of TAYLOR 59.

Leptonic and semileptonic modes with photons

$\Gamma(\mu^+\nu_\mu\gamma)/\Gamma_{\text{total}}$

Γ_{12}/Γ

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
6.2±0.8 OUR AVERAGE					
6.6±1.5	38,39	DEMIDOV	90 XEBC		$P(\mu) < 231.5 \text{ MeV}/c$
6.0±0.9		BARMIN	88 HLBC	+	$P(\mu) < 231.5 \text{ MeV}/c$
• • • We do not use the following data for averages, fits, limits, etc. • • •					
3.5±0.8	39,40	DEMIDOV	90 XEBC		$E(\gamma) > 20 \text{ MeV}$
3.2±0.5	57 41	BARMIN	88 HLBC	+	$E(\gamma) > 20 \text{ MeV}$
5.4±0.3		AKIBA	85 SPEC		$P(\mu) < 231.5 \text{ MeV}/c$

³⁸ $P(\mu)$ cut given in DEMIDOV 90 paper, 235.1 MeV/c, is a misprint according to authors (private communication).

³⁹ DEMIDOV 90 quotes only inner bremsstrahlung (IB) part.

⁴⁰ Not independent of above DEMIDOV 90 value. Cuts differ.

⁴¹ Not independent of above BARMIN 88 value. Cuts differ.

⁴² Assumes μ -e universality and uses constraints from $K \rightarrow e\nu\gamma$.

$\Gamma(\mu^+\nu_\mu\gamma(\text{SD}^+)/\Gamma_{\text{total}}$

Γ_{13}/Γ

Structure-dependent part with $+\gamma$ helicity (SD^+ term). See the “Note on $\pi^\pm \rightarrow \ell^\pm \nu_\gamma$ and $K^\pm \rightarrow \ell^\pm \nu_\gamma$ Form Factors” in the π^\pm section of the Particle Data Listings above.

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN
1.33±0.12±0.18		2588	43 ADLER	00B B787

• • • We do not use the following data for averages, fits, limits, etc. • • •

<3.0 90 AKIBA 85 SPEC

⁴³ ADLER 00B obtains the branching ratio by extrapolating the measurement in the kinematic region $E_\mu > 137 \text{ MeV}$, $E_\gamma > 90 \text{ MeV}$ to the full SD^+ phase-space. Also reports $|F_V + F_A| = 0.165 \pm 0.007 \pm 0.011$ and $-0.04 < F_V - F_A < 0.24$ at 90% CL.

$\Gamma(\mu^+ \nu_\mu \gamma(\text{SD}^+ \text{INT})) / \Gamma_{\text{total}}$

Γ_{14}/Γ

Interference term between internal Bremsstrahlung and SD^+ term. See the “Note on $\pi^\pm \rightarrow \ell^\pm \nu_\gamma$ and $K^\pm \rightarrow \ell^\pm \nu_\gamma$ Form Factors” in the π^\pm section of the Particle Data Listings above.

VALUE (units 10^{-5})	CL%	DOCUMENT ID	TECN
<2.7	90	AKIBA	85

$\Gamma(\mu^+ \nu_\mu \gamma(\text{SD}^- + \text{SD}^- \text{INT})) / \Gamma_{\text{total}}$

Γ_{15}/Γ

Sum of structure-dependent part with $-\gamma$ helicity (SD^- term) and interference term between internal Bremsstrahlung and SD^- term. See the “Note on $\pi^\pm \rightarrow \ell^\pm \nu_\gamma$ and $K^\pm \rightarrow \ell^\pm \nu_\gamma$ Form Factors” in the π^\pm section of the Particle Data Listings above.

VALUE (units 10^{-4})	CL%	DOCUMENT ID	TECN
<2.6	90	44 AKIBA	85

⁴⁴ Assumes μ -e universality and uses constraints from $K \rightarrow e\nu\gamma$.

$\Gamma(e^+ \nu_e \gamma) / \Gamma(\mu^+ \nu_\mu)$

Γ_{16}/Γ_2

VALUE (units 10^{-5})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
1.483 ± 0.066 ± 0.013	1.4K	45 AMBROSINO	09E	KLOE	$\pm E_\gamma$ in 10–250 MeV, $p_e > 200$ MeV/c

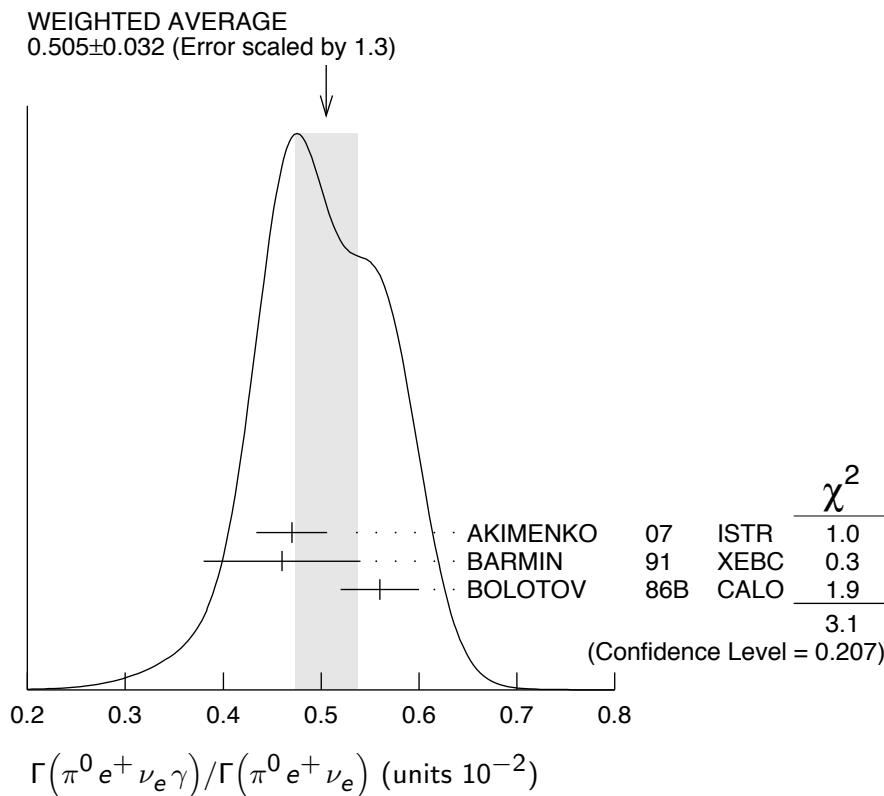
⁴⁵ AMBROSINO 09E measured the differential width $dR_\gamma/dE_\gamma = (1/\Gamma(K \rightarrow \mu\nu)) (d\Gamma(K \rightarrow e\nu\gamma)/dE_\gamma)$. Result obtained by integrating the differential width over E_γ from 10 to 250 MeV.

$\Gamma(\pi^0 e^+ \nu_e \gamma) / \Gamma(\pi^0 e^+ \nu_e)$

Γ_{17}/Γ_3

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.505 ± 0.032 OUR AVERAGE					Error includes scale factor of 1.3. See the ideogram below.
0.47 ± 0.02 ± 0.03	4476	46 AKIMENKO	07 ISTR	–	$E_\gamma > 10$ MeV, $0.6 < \cos(\theta_{e\gamma}) < 0.9$
0.46 ± 0.08	82	47 BARMIN	91 XEBC		$E_\gamma > 10$ MeV, $0.6 < \cos(\theta_{e\gamma}) < 0.9$
0.56 ± 0.04	192	48 BOLOTOV	86B CALO	–	$E_\gamma > 10$ MeV
• • • We do not use the following data for averages, fits, limits, etc. • • •					
1.81 ± 0.03 ± 0.07	4476	46 AKIMENKO	07 ISTR	–	$E_\gamma > 10$ MeV, $\theta_{e\gamma} > 10^\circ$
0.63 ± 0.02 ± 0.03	4476	46 AKIMENKO	07 ISTR	–	$E_\gamma > 30$ MeV, $\theta_{e\gamma} > 20^\circ$
1.51 ± 0.25	82	47 BARMIN	91 XEBC		$E_\gamma > 10$ MeV, $\cos(\theta_{e\gamma}) < 0.98$
0.48 ± 0.20	16	49 LJUNG	73 HLBC	+	$E_\gamma > 30$ MeV
0.22 ± 0.15 – 0.10		49 LJUNG	73 HLBC	+	$E_\gamma > 30$ MeV
0.76 ± 0.28	13	50 ROMANO	71 HLBC		$E_\gamma > 10$ MeV
0.53 ± 0.22		50 ROMANO	71 HLBC	+	$E_\gamma > 30$ MeV
1.2 ± 0.8		BELLOTTI	67 HLBC		$E_\gamma > 30$ MeV

- 46 AKIMENKO 07 provides values for three kinematic regions. For averaging, we use value with $E_\gamma > 10$ MeV and $0.6 < \cos(\theta_{e\gamma}) < 0.9$.
- 47 BARMIN 91 quotes branching ratio $\Gamma(K \rightarrow e\pi^0\nu_e\gamma)/\Gamma_{\text{all}}$. The measured normalization is $[\Gamma(K \rightarrow e\pi^0\nu_e) + \Gamma(K \rightarrow \pi^+\pi^-\pi^-)]$. For comparison with other experiments we used $\Gamma(K \rightarrow e\pi^0\nu_e)/\Gamma_{\text{all}} = 0.0482$ to calculate the values quoted here.
- 48 $\cos(\theta_{e\gamma})$ between 0.6 and 0.9.
- 49 First LJUNG 73 value is for $\cos(\theta_{e\gamma}) < 0.9$, second value is for $\cos(\theta_{e\gamma})$ between 0.6 and 0.9 for comparison with ROMANO 71.
- 50 Both ROMANO 71 values are for $\cos(\theta_{e\gamma})$ between 0.6 and 0.9. Second value is for comparison with second LJUNG 73 value. We use lowest E_γ cut for Summary Table value. See ROMANO 71 for E_γ dependence.



$\Gamma(\pi^0 e^+ \nu_e \gamma(\text{SD}))/\Gamma_{\text{total}}$
Structure-dependent part.

VALUE (units 10^{-5})	CL%	DOCUMENT ID	TECN	CHG
<5.3	90	BOLOTOV	86B	CALO

Γ_{18}/Γ

$\Gamma(\pi^0 \mu^+ \nu_\mu \gamma)/\Gamma_{\text{total}}$

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
(1.25±0.25) OUR AVERAGE						
1.10±0.32±0.05	23	51	ADLER	10	B787	$30 < E_\gamma < 60$ MeV
1.46±0.22±0.32	153	52	TCHIKILEV	07	ISTR	—

Γ_{19}/Γ

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.4 ± 0.5 ± 0.6	125	SHIMIZU	06	K470	+	$E_\gamma > 30 \text{ MeV};$ $\Theta_{\mu\gamma} > 20^\circ$	
<6.1	90	0	LJUNG	73	HLBC	+	$E(\gamma) > 30 \text{ MeV}$

51 Value obtained from $B(K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \gamma) = (2.51 \pm 0.74 \pm 0.12) \times 10^{-5}$ obtained in the kinematic region $E_\gamma > 20 \text{ MeV}$, and then theoretical $K_{\mu 3\gamma}$ spectrum has been used. Also $B(K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \gamma) = (1.58 \pm 0.46 \pm 0.08) \times 10^{-5}$, for $E_\gamma > 30 \text{ MeV}$ and $\theta_{\mu\gamma} > 20^\circ$, was determined.

52 Obtained from measuring $B(K_{\mu 3\gamma}) / B(K_{\mu 3})$ and using PDG 02 value $B(K_{\mu 3}) = 3.27\%$. $B(K_{\mu 3\gamma}) = (8.82 \pm 0.94 \pm 0.86) \times 10^{-5}$ is obtained for $5 \text{ MeV} < E_\gamma < 30 \text{ MeV}$.

$\Gamma(\pi^0 \pi^0 e^+ \nu_e \gamma) / \Gamma_{\text{total}}$			Γ_{20}/Γ				
VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN	CHG	COMMENT	
<5	90	0	BARMIN	92	XEBC	+	$E_\gamma > 10 \text{ MeV}$

Hadronic modes with photons

$\Gamma(\pi^+ \pi^0 \gamma(\text{INT})) / \Gamma_{\text{total}}$			Γ_{21}/Γ		
VALUE (units 10^{-6})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
-4.24 ± 0.63 ± 0.70	600k	53 BATLEY	10A NA48	±	$T_{\pi^+} 0-80 \text{ MeV}$

53 The cut on the photon energy implies $W^2 > 0.2$. BATLEY 10A obtains the INT and DE fractional branchings with respect to IB from a simultaneous kinematical fit of INT and DE and then we use the PDG 10 value for $B(K^+ \rightarrow \pi^+ \pi^0) = 20.66 \pm 0.08$ to determine the IB. The INT and DE correlation coefficients -0.83 . Assuming a constant electric amplitude, X_E , this INT value implies $X_E = -24 \pm 6 \text{ GeV}^{-4}$.

$\Gamma(\pi^+ \pi^0 \gamma(\text{DE})) / \Gamma_{\text{total}}$			Γ_{22}/Γ		
VALUE (units 10^{-6})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
5.99 ± 0.27 ± 0.25	600k	54 BATLEY	10A NA48	±	$T_{\pi^+} 0-80 \text{ MeV}$

• • • We do not use the following data for averages, fits, limits, etc. • • •

$3.8 \pm 0.8 \pm 0.7$	10k	ALIEV	06	K470	+	T_{π^+} 55–90 MeV
$3.7 \pm 3.9 \pm 1.0$	930	UVAROV	06	ISTR	–	T_{π^-} 55–90 MeV
$3.2 \pm 1.3 \pm 1.0$	4k	ALIEV	03	K470	+	T_{π^+} 55–90 MeV
$6.1 \pm 2.5 \pm 1.9$	4k	ALIEV	03	K470	+	T_{π^+} full range
$4.7 \pm 0.8 \pm 0.3$	20k	⁵⁵ ADLER	00C	B787	+	T_{π^+} 55–90 MeV
$20.5 \pm 4.6 \pm 3.9$		BOLOTOV	87	WIRE	–	T_{π^-} 55–90 MeV
$15.6 \pm 3.5 \pm 5.0$		ABRAMS	72	ASPK	±	T_{π^\pm} 55–90 MeV

⁵⁴ The cut on the photon energy implies $W^2 > 0.2$. BATLEY 10A obtains the INT and DE fractional branchings with respect to IB from a simultaneous kinematical fit of INT and DE and then we use the PDG 10 value for $B(K^+ \rightarrow \pi^+ \pi^0) = 20.66 \pm 0.08$ to determine the IB. The INT and DE correlation coefficients –0.93. Assuming constant electric and magnetic amplitudes, X_E and X_M , these INT and DE values imply $X_E = -24 \pm 6 \text{ GeV}^{-4}$ and $X_M = -254 \pm 9 \text{ GeV}^{-4}$.

⁵⁵ ADLER 00C measures the INT component to be $(-0.4 \pm 1.6)\%$ of the inner bremsstrahlung (IB) component.

$\Gamma(\pi^+ \pi^0 \pi^0 \gamma)/\Gamma(\pi^+ \pi^0 \pi^0)$

VALUE (units 10^{-4})	DOCUMENT ID	TECN	CHG	COMMENT
$4.3^{+3.2}_{-1.7}$	BOLOTOV	85	SPEC	$E(\gamma) > 10 \text{ MeV}$

$\Gamma(\pi^+ \pi^+ \pi^- \gamma)/\Gamma_{\text{total}}$

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
(1.04 ± 0.31) OUR AVERAGE					
1.10 ± 0.48	7	BARMIN	89	XEBC	$E(\gamma) > 5 \text{ MeV}$
1.0 ± 0.4		STAMER	65	EMUL	$E(\gamma) > 11 \text{ MeV}$

$\Gamma(\pi^+ \gamma \gamma)/\Gamma_{\text{total}}$

VALUE (units 10^{-7})	CL%	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
11 ± 3 ± 1		31	⁵⁶ KITCHING	97	B787	

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 0.083	90	⁵⁷ ARTAMONOV	05	B949	+	$P_\pi > 213 \text{ MeV}/c$	
< 10	90	0	ATIYA	90B	B787	$T\pi$ 117–127 MeV	
< 84	90	0	ASANO	82	CNTR	+	$T\pi$ 117–127 MeV
-420 ± 520	0	ABRAMS	77	SPEC	+	$T\pi < 92 \text{ MeV}$	
< 350	90	0	LJUNG	73	HLBC	+	6–102, 114–127 MeV
< 500	90	0	KLEMS	71	OSPK	+	$T\pi < 117 \text{ MeV}$
-100 ± 600		CHEN	68	OSPK	+	$T\pi$ 60–90 MeV	

⁵⁶ KITCHING 97 is extrapolated from their model-independent branching fraction $(6.0 \pm 1.5 \pm 0.7) \times 10^{-7}$ for $100 \text{ MeV}/c < P_{\pi^+} < 180 \text{ MeV}/c$ using Chiral Perturbation Theory.

⁵⁷ ARTAMONOV 05 limit assumes ChPT with $\hat{c} = 1.8$ with unitarity corrections. With $\hat{c} = 1.6$ and no unitarity corrections they obtain $< 2.3 \times 10^{-8}$ at 90% CL. This partial branching ratio is predicted to be 6.10×10^{-9} and 0.49×10^{-9} for the cases with and without unitarity correction.

$\Gamma(\pi^+ 3\gamma)/\Gamma_{\text{total}}$

Values given here assume a phase space pion energy spectrum.

VALUE (units 10^{-4})	CL%	DOCUMENT ID	TECN	CHG	COMMENT
<1.0	90	ASANO 82	CNTR	+	$T(\pi)$ 117–127 MeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

<3.0	90	KLEMS	71	OSPK	+	$T(\pi) > 117$ MeV
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$\Gamma(\pi^+ e^+ e^- \gamma)/\Gamma_{\text{total}}$

Γ_{26}/Γ

VALUE (units 10^{-8})	EVTS	DOCUMENT ID	TECN	COMMENT
1.19±0.12±0.04	113	58 BATLEY	08	NA48 $m_{ee\gamma} > 260$ MeV

⁵⁸ BATLEY 08 also reports the Chiral Perturbation Theory parameter $\hat{c} = 0.9 \pm 0.45$ obtained using the shape of the $e^+ e^- \gamma$ invariant mass spectrum. By extrapolating the theoretical amplitude to $m_{ee\gamma} < 260$ MeV, it obtains the inclusive $B(K^+ \rightarrow \pi^+ e^+ e^- \gamma) = (1.29 \pm 0.13 \pm 0.03) \times 10^{-8}$, where the first error is the combined statistical and systematic errors and the second error is from the uncertainty in \hat{c} .

———— Leptonic modes with $\ell\bar{\ell}$ pairs ———

$\Gamma(e^+ \nu_e \nu \bar{\nu})/\Gamma(e^+ \nu_e)$

Γ_{28}/Γ_1

VALUE	CL%	EVTS	DOCUMENT ID	TECN	CHG
<3.8	90	0	HEINTZ 79	SPEC	+

$\Gamma(\mu^+ \nu_\mu \nu \bar{\nu})/\Gamma_{\text{total}}$

Γ_{29}/Γ

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN	CHG
<6.0	90	0	59 PANG	73	CNTR

⁵⁹ PANG 73 assumes μ spectrum from ν - ν interaction of BARDIN 70.

$\Gamma(e^+ \nu_e e^+ e^-)/\Gamma_{\text{total}}$

Γ_{30}/Γ

VALUE (units 10^{-8})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
2.48±0.14±0.14	410	POBLAQUEV 02	B865	+	$m_{ee} > 150$ MeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

20	± 20	4	DIAMANT-...	76	SPEC	+	$m_{e^+ e^-} > 140$ MeV
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$\Gamma(\mu^+ \nu_\mu e^+ e^-)/\Gamma_{\text{total}}$

Γ_{31}/Γ

VALUE (units 10^{-8})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
7.06±0.16±0.26	2.7k	POBLAQUEV 02	B865	+	$m_{ee} > 145$ MeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

100	± 30	14	DIAMANT-...	76	SPEC	+	$m_{e^+ e^-} > 140$ MeV
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$\Gamma(e^+ \nu_e \mu^+ \mu^-)/\Gamma_{\text{total}}$

Γ_{32}/Γ

VALUE (units 10^{-8})	CL%	DOCUMENT ID	TECN
1.72±0.45		MA 06	B865

• • • We do not use the following data for averages, fits, limits, etc. • • •

<50	90	ADLER	98	B787
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$\Gamma(\mu^+ \nu_\mu \mu^+ \mu^-)/\Gamma_{\text{total}}$

<u>VALUE</u> (units 10^{-7})	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
<4.1	90	ATIYA	89	B787 +

Γ_{33}/Γ

— Lepton Family number (*LF*), Lepton number (*L*), $\Delta S = \Delta Q$ (*SQ*) —
— violating modes, or $\Delta S = 1$ weak neutral current (*S1*) modes —

$\Gamma(\pi^+ \pi^+ e^- \bar{\nu}_e)/\Gamma_{\text{total}}$

Test of $\Delta S = \Delta Q$ rule.

<u>VALUE</u> (units 10^{-7})	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
• • • We do not use the following data for averages, fits, limits, etc. • • •					
< 9.0	95	0	SCHWEINB...	71	HLBC +
< 6.9	95	0	ELY	69	HLBC +
<20.	95		BIRGE	65	FBC +

Γ_{34}/Γ

$\Gamma(\pi^+ \pi^+ e^- \bar{\nu}_e)/\Gamma(\pi^+ \pi^- e^+ \nu_e)$

Test of $\Delta S = \Delta Q$ rule.

<u>VALUE</u> (units 10^{-4})	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
< 3	90	3	60 BLOCH	76 SPEC
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<130.	95	0	BOURQUIN	71 ASPK

60 BLOCH 76 quotes 3.6×10^{-4} at CL = 95%, we convert.

Γ_{34}/Γ_6

$\Gamma(\pi^+ \pi^+ \mu^- \bar{\nu}_\mu)/\Gamma_{\text{total}}$

Test of $\Delta S = \Delta Q$ rule.

<u>VALUE</u> (units 10^{-6})	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
<3.0	95	0	BIRGE	65	FBC +

Γ_{35}/Γ

$\Gamma(\pi^+ e^+ e^-)/\Gamma_{\text{total}}$

Test for $\Delta S = 1$ weak neutral current. Allowed by combined first-order weak and electromagnetic interactions.

<u>VALUE</u> (units 10^{-7})	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>CHG</u>
(3.00±0.09) OUR AVERAGE				
3.11±0.04±0.12	7253	61 BATLEY	09 NA48	±
2.94±0.05±0.14	10300	62 APPEL	99 SPEC	+
2.75±0.23±0.13	500	63 ALLIEGRO	92 SPEC	+
2.7 ± 0.5	41	64 BLOCH	75 SPEC	+

Γ_{36}/Γ

61 Value extrapolated from a measurement in the region $z = (m_{ee}/m_K)^2 > 0.08$. BATLEY 09 also evaluated the shape of the form factor using four different theoretical models.

62 APPEL 99 establishes vector nature of this decay and determines form factor $f(Z) = f_0(1+\delta Z)$, $Z = M_{ee}^2/m_K^2$, $\delta = 2.14 \pm 0.13 \pm 0.15$.

63 ALLIEGRO 92 assumes a vector interaction with a form factor given by $\lambda = 0.105 \pm 0.035 \pm 0.015$ and a correlation coefficient of -0.82 .

64 BLOCH 75 assumes a vector interaction.

$\Gamma(\pi^+ \mu^+ \mu^-)/\Gamma_{\text{total}}$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interactions.

VALUE (units 10^{-8})	CL%	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
(9.4±0.6) OUR AVERAGE	Error includes scale factor of 2.6. See the ideogram below.					
9.62±0.21±0.13	3120	65	BATLEY	11A	NA48	± 2003-04 data
9.8 ± 1.0 ± 0.5	110	66	PARK	02	HYCP	±
9.22±0.60±0.49	402	67	MA	00	B865	+
5.0 ± 0.4 ± 0.9	207	68	ADLER	97C	B787	+
• • • We do not use the following data for averages, fits, limits, etc. • • •						
9.7 ± 1.2 ± 0.4	65	PARK	02	HYCP		+
10.0 ± 1.9 ± 0.7	35	PARK	02	HYCP		-
<23	90	ATIYA	89	B787		+

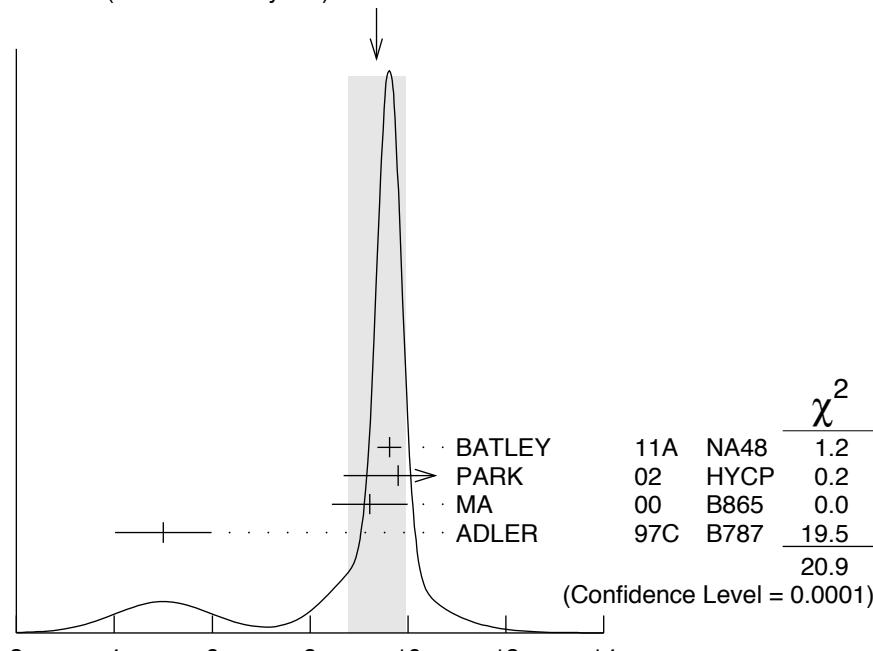
⁶⁵ BATLEY 11A also studies the form factor $f(z)$ dependence of the decay, described via single photon exchange: i) assuming a linear form factor, $f(z) = f_0 (1 + \delta z)$, $z = (M_{\mu\mu}/m_K)^2$, finding $f_0 = 0.470 \pm 0.040$ and $\delta = 3.11 \pm 0.57$ and ii) assuming a linear form factor including $\pi\pi$ rescattering, $W_{\pi\pi}$, as in DAMBROSIO 98A, finding $f(z) = G_F m_K^2 (a_+ + b_+ z) + W_{\pi\pi}(z)$, $a_+ = -0.575 \pm 0.039$, $b_+ = -0.813 \pm 0.145$.

⁶⁶ PARK 02 “±” result comes from combining $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ and $K^- \rightarrow \pi^- \mu^+ \mu^-$, assuming CP is conserved.

⁶⁷ MA 00 establishes vector nature of this decay and determines form factor $f(z) = f_0 (1 + \delta z)$, $z = (M_{\mu\mu}/m_K)^2$, $\delta = 2.45^{+1.30}_{-0.95}$.

⁶⁸ ADLER 97C gives systematic error 0.7×10^{-8} and theoretical uncertainty 0.6×10^{-8} , which we combine in quadrature to obtain our second error.

WEIGHTED AVERAGE
9.4±0.6 (Error scaled by 2.6)



$$\Gamma(\pi^+ \mu^+ \mu^-)/\Gamma_{\text{total}}$$

$$\Gamma_{37}/\Gamma$$

$\Gamma(\pi^+ \nu \bar{\nu})/\Gamma_{\text{total}}$ Γ_{38}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interactions. Branching ratio values are extrapolated from the momentum or energy regions shown in the comments assuming Standard Model phase space except for those labeled "Scalar" or "Tensor" to indicate the assumed non-Standard-Model interaction.

<i>VALUE</i> (units 10^{-9})	<i>CL%</i>	<i>EVTS</i>	<i>DOCUMENT ID</i>	<i>TECN</i>	<i>CHG</i>	<i>COMMENT</i>
0.173 ^{+0.115} _{-0.105}	7	69	ARTAMONOV 08	B949	+	$140 < P_\pi < 199 \text{ MeV}$, $211 < P_\pi < 229 \text{ MeV}$
• • • We do not use the following data for averages, fits, limits, etc. • • •						
0.789 ^{+0.926} _{-0.510}	3	70	ARTAMONOV 08	B949	+	$140 < P_\pi < 199 \text{ MeV}$
< 2.2	90	1	ADLER 04	B787	+	$211 < P_\pi < 229 \text{ MeV}$
< 2.7	90		ADLER 04	B787	+	Scalar
< 1.8	90		ADLER 04	B787	+	Tensor
0.147 ^{+0.130} _{-0.089}	3	72	ANISIMOVSKY 04	B949	+	$211 < P_\pi < 229 \text{ MeV}$
0.157 ^{+0.175} _{-0.082}	2		ADLER 02	B787	+	$P_\pi > 211 \text{ MeV}/c$
< 4.2	90	1	ADLER 02C	B787	+	$140 < P_\pi < 195 \text{ MeV}$
< 4.7	90	73	ADLER 02C	B787	+	Scalar
< 2.5	90	73	ADLER 02C	B787	+	Tensor
0.15 ^{+0.34} _{-0.12}	1		ADLER 00	B787		In ADLER 02
0.42 ^{+0.97} _{-0.35}	1		ADLER 97	B787		
< 2.4	90		ADLER 96	B787		
< 7.5	90		ATIYA 93	B787	+	$T(\pi) 115\text{--}127 \text{ MeV}$
< 5.2	90	74	ATIYA 93	B787	+	
< 17	90	0	ATIYA 93B	B787	+	$T(\pi) 60\text{--}100 \text{ MeV}$
< 34	90		ATIYA 90	B787	+	
<140	90		ASANO 81B	CNTR	+	$T(\pi) 116\text{--}127 \text{ MeV}$

⁶⁹ Value obtained combining ANISIMOVSKY 04, ADLER 04, and the present ARTAMONOV 08 results.

⁷⁰ Observed 3 events with an estimated background of $0.93 \pm 0.17^{+0.32}_{-0.24}$. Signal-to-background ratio for each of these 3 events is 0.20, 0.42, and 0.47.

⁷¹ Value obtained combining the previous result ADLER 02C with 1 event and the present result with 0 events to obtain an expected background 1.22 ± 0.24 events and 1 event observed.

⁷² Value obtained combining the previous E787 result ADLER 02 with 2 events and the present E949 with 1 event. The additional event has a signal-to-background ratio 0.9. Superseded by ARTAMONOV 08.

⁷³ Superseded by ADLER 04.

⁷⁴ Combining ATIYA 93 and ATIYA 93B results. Superseded by ADLER 96.

 $\Gamma(\pi^+ \pi^0 \nu \bar{\nu})/\Gamma_{\text{total}}$ Γ_{39}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interactions.

<i>VALUE</i> (units 10^{-5})	<i>CL%</i>	<i>DOCUMENT ID</i>	<i>TECN</i>
<4.3	90	75 ADLER 01	SPEC

⁷⁵ Search region defined by $90 \text{ MeV}/c < P_{\pi^+} < 188 \text{ MeV}/c$ and $135 \text{ MeV} < E_{\pi^0} < 180 \text{ MeV}$.

$\Gamma(\mu^- \nu e^+ e^+)/\Gamma(\pi^+ \pi^- e^+ \nu_e)$

Test of lepton family number conservation.

VALUE (units 10^{-3})	CL%	EVTS	DOCUMENT ID	TECN	CHG
<0.5	90	0	76 DIAMANT-...	76 SPEC	+

76 DIAMANT-BERGER 76 quotes this result times our 1975 $\pi^+ \pi^- e \nu$ BR ratio.

Γ_{40}/Γ_6

$\Gamma(\mu^+ \nu_e)/\Gamma_{\text{total}}$

Forbidden by lepton family number conservation.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<0.004	90	0	77 LYONS	81 HLBC	200 GeV K^+ narrow band ν beam

• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.012	90	77 COOPER	82 HLBC	Wideband ν beam
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77 COOPER 82 and LYONS 81 limits on ν_e observation are here interpreted as limits on lepton family number violation in the absence of mixing.

Γ_{41}/Γ

$\Gamma(\pi^+ \mu^+ e^-)/\Gamma_{\text{total}}$

Test of lepton family number conservation.

VALUE (units 10^{-10})	CL%	EVTS	DOCUMENT ID	TECN	CHG
<0.13	90	78 SHER	05 RVUE	+	

• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.21	90	SHER	05 B865	+
<0.39	90	APPEL	00 B865	+
<2.1	90	LEE	90 SPEC	+

78 This result combines SHER 05 1998 data, APPEL 00 1996 data, and data from BERGMAN 97 and PISLAK 97 theses, all from BNL-E865, with LEE 90 BNL-E777 data.

Γ_{42}/Γ

$\Gamma(\pi^+ \mu^- e^+)/\Gamma_{\text{total}}$

Test of lepton family number conservation.

VALUE (units 10^{-10})	CL%	EVTS	DOCUMENT ID	TECN	CHG
< 5.2	90	0	APPEL 00B	B865	+

• • • We do not use the following data for averages, fits, limits, etc. • • •

<70	90	0	79 DIAMANT-...	76 SPEC	+
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79 Measurement actually applies to the sum of the $\pi^+ \mu^- e^+$ and $\pi^- \mu^+ e^+$ modes.

Γ_{43}/Γ

$\Gamma(\pi^- \mu^+ e^+)/\Gamma_{\text{total}}$

Test of total lepton number conservation.

VALUE (units 10^{-10})	CL%	EVTS	DOCUMENT ID	TECN	CHG
< 5.0	90	0	APPEL 00B	B865	+

• • • We do not use the following data for averages, fits, limits, etc. • • •

<70	90	0	80 DIAMANT-...	76 SPEC	+
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80 Measurement actually applies to the sum of the $\pi^+ \mu^- e^+$ and $\pi^- \mu^+ e^+$ modes.

Γ_{44}/Γ

$\Gamma(\pi^- e^+ e^+)/\Gamma_{\text{total}}$

Test of total lepton number conservation.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	CHG
$<6.4 \times 10^{-10}$	90	0	APPEL 00B	B865	+

• • • We do not use the following data for averages, fits, limits, etc. • • •

$<9.2 \times 10^{-9}$	90	0	DIAMANT-...	76 SPEC	+
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$<1.5 \times 10^{-5}$			CHANG	68 HBC	-
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Γ_{45}/Γ

$\Gamma(\pi^- \mu^+ \mu^+)/\Gamma_{\text{total}}$

Forbidden by total lepton number conservation.

Γ_{46}/Γ

VALUE	CL%	DOCUMENT ID	TECN	CHG
$<1.1 \times 10^{-9}$	90	BATLEY	11A	NA48 \pm
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$				
$<3.0 \times 10^{-9}$	90	APPEL	00B	B865 +
$<1.5 \times 10^{-4}$	90	81 LITTENBERG	92	HBC

⁸¹ LITTENBERG 92 is from retroactive data analysis of CHANG 68 bubble chamber data.

$\Gamma(\mu^+ \bar{\nu}_e)/\Gamma_{\text{total}}$

Forbidden by total lepton number conservation.

Γ_{47}/Γ

VALUE (units 10^{-3})	CL%	DOCUMENT ID	TECN	COMMENT
<3.3	90	82 COOPER	82	HLBC Wideband ν beam

⁸² COOPER 82 limit on $\bar{\nu}_e$ observation is here interpreted as a limit on lepton number violation in the absence of mixing.

$\Gamma(\pi^0 e^+ \bar{\nu}_e)/\Gamma_{\text{total}}$

Forbidden by total lepton number conservation.

Γ_{48}/Γ

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<0.003	90	83 COOPER	82	HLBC Wideband ν beam

⁸³ COOPER 82 limit on $\bar{\nu}_e$ observation is here interpreted as a limit on lepton number violation in the absence of mixing.

$\Gamma(\pi^+ \gamma)/\Gamma_{\text{total}}$

Violates angular momentum conservation and gauge invariance. Current interest in this decay is as a search for non-commutative space-time effects as discussed in ARTAMONOV 05 and for exotic physics such as a vacuum expectation value of a new vector field, non-local Superstring effects, or departures from Lorentz invariance, as discussed in ADLER 02B.

Γ_{49}/Γ

VALUE (units 10^{-9})	CL%	DOCUMENT ID	TECN	CHG
< 2.3	90	ARTAMONOV 05	B949	+
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$				
< 360	90	ADLER	02B	B787 +
<1400	90	ASANO	82	CNTR +
<4000	90	84 KLEMS	71	OSPK +

⁸⁴ Test of model of Selleri, Nuovo Cimento **60A** 291 (1969).

K⁺ LONGITUDINAL POLARIZATION OF EMITTED μ^+

VALUE	CL%	DOCUMENT ID	TECN	CHG	COMMENT
<-0.990	90	85 AOKI	94	SPEC	+
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$					
<-0.990	90	IMAZATO	92	SPEC	+
-0.970 ± 0.047	86	YAMANAKA	86	SPEC	+
-1.0 ± 0.1	86	CUTTS	69	SPRK	+
-0.96 ± 0.12	86	COOMBES	57	CNTR	+

⁸⁵ AOKI 94 measures $\xi P_\mu = -0.9996 \pm 0.0030 \pm 0.0048$. The above limit is obtained by summing the statistical and systematic errors in quadrature, normalizing to the physically significant region ($|\xi P_\mu| < 1$) and assuming that $\xi=1$, its maximum value.

⁸⁶ Assumes $\xi=1$.

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ENERGY DEPENDENCE OF K^\pm DALITZ PLOT

$$|\text{matrix element}|^2 = 1 + gu + hv^2 + kv^2$$

where $u = (s_3 - s_0) / m_\pi^2$ and $v = (s_2 - s_1) / m_\pi^2$

LINEAR COEFFICIENT g FOR $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

Some experiments use Dalitz variables x and y . In the comments we give a_y = coefficient of y term. See note above on “Dalitz Plot Parameters for $K \rightarrow 3\pi$ Decays.” For discussion of the conversion of a_y to g , see the earlier version of the same note in the Review published in Physics Letters **111B** 70 (1982).

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
-0.21134±0.00017	471M	87 BATLEY	07B	NA48 ±	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
-0.2221 ± 0.0065	225k	DEVAUX	77	SPEC +	$a_y = .2814 \pm .0082$
-0.199 ± 0.008	81k	88 LUCAS	73	HBC -	$a_y = .252 \pm 0.011$
-0.2157 ± 0.0028	750k	FORD	72	ASPK +	$a_y = .2734 \pm .0035$
-0.2186 ± 0.0028	750k	FORD	72	ASPK -	$a_y = .2770 \pm .0035$
-0.200 ± 0.009	39819	89 HOFFMASTER72	HLBC +		
-0.196 ± 0.012	17898	90 GRAUMAN	70	HLBC +	$a_y = .228 \pm 0.030$
-0.193 ± 0.010	50919	MAST	69	HBC -	$a_y = .244 \pm 0.013$
-0.218 ± 0.016	9994	91 BUTLER	68	HBC +	$a_y = .277 \pm 0.020$
-0.190 ± 0.023	5778	91,92 MOSCOSO	68	HBC -	$a_y = .242 \pm 0.029$
-0.22 ± 0.024	5428	91,92 ZINCHENKO	67	HBC +	$a_y = .28 \pm 0.03$
-0.220 ± 0.035	1347	93 FERRO-LUZZI	61	HBC -	$a_y = .28 \pm 0.045$

⁸⁷ Final state strong interaction and radiative corrections not included in the fit.

⁸⁸ Quadratic dependence is required by K_L^0 experiments.

⁸⁹ HOFFMASTER 72 includes GRAUMAN 70 data.

⁹⁰ Emulsion data added — all events included by HOFFMASTER 72.

⁹¹ Experiments with large errors not included in average.

⁹² Also includes DBC events.

⁹³ No radiative corrections included.

QUADRATIC COEFFICIENT h FOR $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
1.848±0.040	471M	94 BATLEY	07B	NA48 ±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.06 ± 1.43	225k	DEVAUX	77	SPEC +
1.87 ± 0.62	750k	FORD	72	ASPK +
1.25 ± 0.62	750k	FORD	72	ASPK -
-0.9 ± 1.4	39819	HOFFMASTER72	HLBC +	
-0.1 ± 1.2	50919	MAST	69	HBC -

⁹⁴ Final state strong interaction and radiative corrections not included in the fit.

QUADRATIC COEFFICIENT k FOR $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	CHG
- 4.63 ± 0.14	471M	95 BATLEY	07B NA48	±

• • • We do not use the following data for averages, fits, limits, etc. • • •

-20.5 ± 3.9	225k	DEVAUX	77	SPEC	+
- 7.5 ± 1.9	750k	FORD	72	ASPK	+
- 8.3 ± 1.9	750k	FORD	72	ASPK	-
-10.5 ± 4.5	39819	HOFFMASTER	72	HLBC	+
-14 ± 12	50919	MAST	69	HBC	-

95 Final state strong interaction and radiative corrections not included in the fit.

$(g_+ - g_-) / (g_+ + g_-)$ FOR $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

This is a CP violating asymmetry between linear coefficients g_+ for $K^+ \rightarrow \pi^+ \pi^+ \pi^-$ decay and g_- for $K^- \rightarrow \pi^- \pi^+ \pi^-$ decay.

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN
- 1.5 ± 1.5 ± 1.6	3.1G	96 BATLEY	07E NA48

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.7 ± 2.1 ± 2.0	1.7G	97 BATLEY	06 NA48
-70.0 ± 53	3.2M	FORD	70 ASPK

96 BATLEY 07E includes data from BATLEY 06. Uses quadratic parametrization and value $g_+ + g_- = 2g$ from BATLEY 07B. This measurement neglects any possible charge asymmetries in higher order slope parameters h or k .

97 This measurement neglects any possible charge asymmetries in higher order slope parameters h or k .

LINEAR COEFFICIENT g FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

Unless otherwise stated, all experiments include terms quadratic in $(s_3 - s_0) / m_{\pi^+}^2$. See note above on "Dalitz Plot Parameters for $K \rightarrow 3\pi$ Decays."

See BATUSOV 98 for a discussion of the discrepancy between their result and others, especially BOLOTOV 86. At this time we have no way to resolve the discrepancy so we depend on the large scale factor as a warning.

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.626 ± 0.007 OUR AVERAGE					
0.6259 ± 0.0043 ± 0.0093	493k	AKOPDZHAN..05B	TNF	±	
0.627 ± 0.004 ± 0.010	252k	98,99 AJINENKO	03B ISTR	-	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.736 ± 0.014 ± 0.012	33k	BATUSOV	98	SPEC	+
0.582 ± 0.021	43k	BOLOTOV	86	CALO	-
0.670 ± 0.054	3263	BRAUN	76B	HLBC	+
0.630 ± 0.038	5635	SHEAFF	75	HLBC	+
0.510 ± 0.060	27k	SMITH	75	WIRE	+
0.67 ± 0.06	1365	AUBERT	72	HLBC	+
0.544 ± 0.048	4048	DAVISON	69	HLBC	+
					Also emulsion

98 Measured using in-flight decays of the 25 GeV negative secondary beam.

99 They form new world averages $g_- = (0.617 \pm 0.018)$ and $g_+ = (0.684 \pm 0.033)$ which give $\Delta g_T' = 0.051 \pm 0.028$.

QUADRATIC COEFFICIENT h FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
0.052 ± 0.008 OUR AVERAGE					
0.0551 ± 0.0044 ± 0.0086	493k	AKOPDZHAN..05B	TNF	±	
0.046 ± 0.004 ± 0.012	252k	100 AJINENKO	03B ISTR	—	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.128 ± 0.015 ± 0.024	33k	BATUSOV	98	SPEC	+
0.037 ± 0.024	43k	BOLOTOV	86	CALO	—
0.152 ± 0.082	3263	BRAUN	76B	HLBC	+
0.041 ± 0.030	5635	SHEAFF	75	HLBC	+
0.009 ± 0.040	27k	SMITH	75	WIRE	+
-0.01 ± 0.08	1365	AUBERT	72	HLBC	+
0.026 ± 0.050	4048	DAVISON	69	HLBC	+
					Also emulsion

100 Measured using in-flight decays of the 25 GeV negative secondary beam.

QUADRATIC COEFFICIENT k FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG	
0.0054 ± 0.0035 OUR AVERAGE		Error includes scale factor of 2.5.			
0.0082 ± 0.0011 ± 0.0014	493k	AKOPDZHAN..05B	TNF	±	
0.001 ± 0.001 ± 0.002	252k	101 AJINENKO	03B ISTR	—	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
0.0197 ± 0.0045 ± 0.0029	33k	BATUSOV	98	SPEC	+

101 Measured using in-flight decays of the 25 GeV negative secondary beam.

$(g_+ - g_-) / (g_+ + g_-)$ FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

A nonzero value for this quantity indicates CP violation.

VALUE (units 10^{-4})	EVTS	DOCUMENT ID	TECN
(1.8±1.8) OUR AVERAGE			
1.8 ± 1.7 ± 0.6	91.3M	102 BATLEY	07E NA48
2 ± 18 ± 5	619k	103 AKOPDZHAN..05	TNF

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.8 ± 2.2 ± 1.3 47M 104 BATLEY 06A NA48

102 BATLEY 07E includes data from BATLEY 06A. Uses quadratic parametrization and PDG 06 value $g = 0.626 \pm 0.007$ to obtain $g_+ - g_- = (2.2 \pm 2.1 \pm 0.7) \times 10^{-4}$. Neglects any possible charge asymmetries in higher order slope parameters h or k .

103 Asymmetry obtained assuming that $g_+ + g_- = 2 \times 0.652$ (PDG 02) and that asymmetries in h and k are zero.

104 Linear and quadratic slopes from PDG 04 are used. Any possible charge asymmetries in higher order slope parameters h or k are neglected.

ALTERNATIVE PARAMETRIZATIONS OF $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ DALITZ PLOT

The following functional form for the matrix element suggested by $\pi\pi$ rescattering in $K^+ \rightarrow \pi^+ \pi^+ \pi^- \rightarrow \pi^+ \pi^0 \pi^0$ is used for this fit (CABIBBO 04A, CABIBBO 05): Matrix element = $M_0 + M_1$ where $M_0 = 1 + (1/2)g_0 u + (1/2)h' u^2 + (1/2)k_0 v^2$ with $u = (s_3 - s_0)/(m_{\pi^+})^2$, $v = (s_2 - s_1)/(m_{\pi^+})^2$ and where M_1 takes into account the non-analytic piece due to $\pi\pi$ rescattering amplitudes a_0 and a_2 ; The parameters g_0 and h' are related to the parameters g and h of the matrix element squared

given in the previous section by the approximations $g_0 \sim g^{PDG}$ and $h' \sim h^{PDG} - (g/2)^2$ and $k_0 \sim k^{PDG}$.

In addition, we also consider the effective field theory framework of COLANGELO 06A and BISSEGGER 09 to extract g_{BB} and h'_{BB} .

LINEAR COEFFICIENT g_0 FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.6525±0.0009±0.0033	60M	105 BATLEY	09A NA48	±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.645 ± 0.004 ± 0.009	23M	106 BATLEY	06B NA48	±

105 This fit is obtained with the CABIBBO 05 matrix element in the $2\pi^0$ invariant mass squared range $0.074094 < m_{2\pi^0}^2 < 0.104244$ GeV 2 . Electromagnetic corrections and CHPT constraints for $\pi\pi$ phase shifts (a_0 and a_2) have been used. Also measured $(a_0 - a_2)m_{\pi^+} = 0.2646 \pm 0.0021 \pm 0.0023$, where k_0 was kept fixed in the fit at -0.0099 .

106 Superseded by BATLEY 09A. This fit is obtained with the CABIBBO 05 matrix element in the $2\pi^0$ invariant mass squared range 0.074 GeV $^2 < m_{2\pi^0}^2 < 0.097$ GeV 2 , assuming $k = 0$ (no term proportional to $(s_2 - s_1)^2$) and excluding the kinematic region around the cusp ($m_{2\pi^0}^2 = (2m_{\pi^+})^2 \pm 0.000525$ GeV 2). Also $\pi\pi$ phase shifts a_0 and a_2 are measured: $(a_0 - a_2)m_{\pi^+} = 0.268 \pm 0.010 \pm 0.004 \pm 0.013$ (external) and $a_2 m_{\pi^+} = -0.041 \pm 0.022 \pm 0.014$.

QUADRATIC COEFFICIENT h' FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
-0.0433±0.0008±0.0026	60M	107 BATLEY	09A NA48	±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.047 ± 0.012 ± 0.011	23M	108 BATLEY	06B NA48	±

107 This fit is obtained with the CABIBBO 05 matrix element in the $2\pi^0$ invariant mass squared range $0.074094 < m_{2\pi^0}^2 < 0.104244$ GeV 2 . Electromagnetic corrections and CHPT constraints for $\pi\pi$ phase shifts (a_0 and a_2) have been used. Also measured $(a_0 - a_2)m_{\pi^+} = 0.2646 \pm 0.0021 \pm 0.0023$, where k_0 was kept fixed in the fit at -0.0099 .

108 Superseded by BATLEY 09A. This fit is obtained with the CABIBBO 05 matrix element in the $2\pi^0$ invariant mass squared range 0.074 GeV $^2 < m_{2\pi^0}^2 < 0.097$ GeV 2 , assuming $k = 0$ (no term proportional to $(s_2 - s_1)^2$) and excluding the kinematic region around the cusp ($m_{2\pi^0}^2 = (2m_{\pi^+})^2 \pm 0.000525$ GeV 2). Also $\pi\pi$ phase shifts a_0 and a_2 are measured: $(a_0 - a_2)m_{\pi^+} = 0.268 \pm 0.010 \pm 0.004 \pm 0.013$ (external) and $a_2 m_{\pi^+} = -0.041 \pm 0.022 \pm 0.014$.

QUADRATIC COEFFICIENT k_0 FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.0095±0.00017±0.00048	60M	109 BATLEY	09A NA48	±

109 Assumed $a_2 m_{\pi^+} = -0.0044$ in the fit.

LINEAR COEFFICIENT g_{BB} FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
0.6219 ± 0.0009 ± 0.0033	60M	110 BATLEY	09A NA48	±

110 This fit is obtained using parametrizations of COLANGELO 06A and BISSEGGER 09 in the $2\pi^0$ invariant mass squared range $0.074094 < m_{2\pi^0}^2 < 0.104244$ GeV 2 . Electromagnetic corrections and CHPT constraints for $\pi\pi$ phase shifts (a_0 and a_2) have been used. Also measured ($a_0 - a_2$) $m_{\pi^+} = 0.2633 \pm 0.0024 \pm 0.0024$, where k_0 was kept fixed in the fit at 0.0085.

QUADRATIC COEFFICIENT h_{BB} FOR $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	CHG
-0.0520 ± 0.0009 ± 0.0026	60M	111 BATLEY	09A NA48	±

111 This fit is obtained using parametrizations of COLANGELO 06A and BISSEGGER 09 in the $2\pi^0$ invariant mass squared range $0.074094 < m_{2\pi^0}^2 < 0.104244$ GeV 2 . Electromagnetic corrections and CHPT constraints for $\pi\pi$ phase shifts (a_0 and a_2) have been used. Also measured ($a_0 - a_2$) $m_{\pi^+} = 0.2633 \pm 0.0024 \pm 0.0024$, where k_0 was kept fixed in the fit at 0.0085.

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K_{l3}^\pm FORM FACTORS

In the form factor comments, the following symbols are used.

f_+ and f_- are form factors for the vector matrix element.

f_S and f_T refer to the scalar and tensor term.

$$f_0 = f_+ + f_- t/(m_{K^+}^2 - m_{\pi^0}^2).$$

t = momentum transfer to the π .

λ_+ and λ_0 are the linear expansion coefficients of f_+ and f_0 :

$$f_+(t) = f_+(0) (1 + \lambda_+ t / m_{\pi^+}^2)$$

For quadratic expansion

$$f_+(t) = f_+(0) (1 + \lambda'_+ t / m_{\pi^+}^2 + \frac{\lambda''_+}{2} t^2 / m_{\pi^+}^4)$$

as used by KTeV. If there is a non-vanishing quadratic term, then λ_+

represents an average slope, which is then different from λ'_+ .

NA48 and ISTRA quadratic expansion coefficients are converted with

$$\lambda'_+{}^{PDG} = \lambda'_+{}^{NA48} \text{ and } \lambda''_+{}^{PDG} = 2 \lambda'_+{}^{NA48}$$

$$\lambda'_+{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda'_+{}^{ISTR A} \text{ and}$$

$$\lambda''_+{}^{PDG} = 2 (\frac{m_{\pi^+}}{m_{\pi^0}})^4 \lambda'_+{}^{ISTR A}$$

ISTR A linear expansion coefficients are converted with

$$\lambda'_+{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda'_+{}^{ISTR A} \text{ and } \lambda_0{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda_0{}^{ISTR A}$$

The pole parametrization is

$$f_+(t) = f_+(0) \left(\frac{M_V^2}{M_V^2 - t} \right)$$

$$f_0(t) = f_0(0) \left(\frac{M_S^2}{M_S^2 - t} \right)$$

where M_V and M_S are the vector and scalar pole masses.

The following abbreviations are used:

DP = Dalitz plot analysis.

PI = π spectrum analysis.

MU = μ spectrum analysis.

POL = μ polarization analysis.

BR = $K_{\mu 3}^{\pm}/K_{e 3}^{\pm}$ branching ratio analysis.

E = positron or electron spectrum analysis.

RC = radiative corrections.

λ_+ (LINEAR ENERGY DEPENDENCE OF f_+ IN $K_{e 3}^{\pm}$ DECAY)

These results are for a linear expansion only. See the next section for fits including a quadratic term. For radiative correction of the $K_{e 3}^{\pm}$ Dalitz plot, see GINSBERG 67, BECHERRAWY 70, CIRIGLIANO 02, CIRIGLIANO 04, and ANDRE 07. Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^{\pm}$ and $K_{\ell 3}^0$ Form Factors" above. For earlier, lower statistics results, see the 2004 edition of this review, Physics Letters **B592** 1 (2004).

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
2.97 ± 0.05 OUR FIT	Assuming μ -e universality				
2.98 ± 0.05 OUR AVERAGE					
3.044 ± 0.083 ± 0.074	1.1M	AKOPDZANOV 09	TNF	±	
2.966 ± 0.050 ± 0.034	919k	112 YUSHCHENKO 04B	ISTR	—	DP
2.78 ± 0.26 ± 0.30	41k	SHIMIZU 00	SPEC	+	DP
2.84 ± 0.27 ± 0.20	32k	113 AKIMENKO 91	SPEC		PI, no RC
2.9 ± 0.4	62k	114 BOLOTOV 88	SPEC		PI, no RC
• • • We do not use the following data for averages, fits, limits, etc. • • •					
3.06 ± 0.09 ± 0.06	550k	112, 115 AJINENKO 03C	ISTR	—	DP
2.93 ± 0.15 ± 0.2	130k	115 AJINENKO 02	SPEC		DP

112 Rescaled to agree with our conventions as noted above.

113 AKIMENKO 91 state that radiative corrections would raise λ_+ by 0.0013.

114 BOLOTOV 88 state radiative corrections of GINSBERG 67 would raise λ_+ by 0.002.

115 Superseded by YUSHCHENKO 04B.

λ_+ (LINEAR ENERGY DEPENDENCE OF f_+ IN $K_{\mu 3}^{\pm}$ DECAY)

Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^{\pm}$ and $K_{\ell 3}^0$ Form Factors" above. For earlier, lower statistics results, see the 2004 edition of this review, Physics Letters **B592** 1 (2004).

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
2.97 ± 0.05 OUR FIT	Assuming μ -e universality				
2.96 ± 0.17 OUR FIT	Not assuming μ -e universality				
2.96 ± 0.14 ± 0.10	540k	116 YUSHCHENKO 04	ISTR	—	DP
• • • We do not use the following data for averages, fits, limits, etc. • • •					
3.21 ± 0.45	112k	117 AJINENKO 03	ISTR	—	DP
116 Rescaled to agree with our conventions as noted above.					
117 Superseded by YUSHCHENKO 04.					

f_T/f_+ FOR $K_{\mu 3}^\pm$ DECAY

Ratio of tensor to f_+ couplings.

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
-0.07 ± 0.71 ± 0.20	540k	YUSHCHENKO04	ISTR	-	DP
• • • We do not use the following data for averages, fits, limits, etc. • • •					
-2.1 ± 2.8 ± 1.4	112k	134 AJINENKO	03	ISTR	- DP
2 ± 12	1585	BRAUN	75	HLBC	

134 The second error is the theoretical error from the uncertainty in the chiral perturbation theory prediction for λ_0 . Superseded by YUSHCHENKO 04.

$K_{\ell 4}^\pm$ FORM FACTORS

Based on the parametrizations of AMOROS 99, the $K_{\ell 4}^\pm$ form factors can be expressed as

$$\begin{aligned} F_s &= f_s + f'_s q^2 + f''_s q^4 + f'_e S_e / 4m_\pi^2 \\ F_p &= f_p + f'_p q^2 \\ G_p &= g_p + g'_p q^2 \\ H_p &= h_p + h'_p q^2 \end{aligned}$$

where $q^2 = (S_\pi / 4m_\pi^2) - 1$, S_π is the invariant mass squared of the dipion, and S_e is the invariant mass squared of the dilepton.

f_s FOR $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ DECAY

VALUE	EVTS	DOCUMENT ID	TECN	CHG
5.75 ± 0.02 ± 0.08	400k	135 PISLAK	03	B865 +

135 Radiative corrections included. Using Roy equations and not including isospin breaking, PISLAK 03 obtains the following $\pi\pi$ scattering lengths $a_0^0 = 0.228 \pm 0.012 \pm 0.004^{+0.012}_{-0.016}$ (theor.) and $a_0^2 = -0.0365 \pm 0.0023 \pm 0.0008^{+0.0031}_{-0.0026}$ (theor.).

f'_s/f_s FOR $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ DECAY

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
15.2 ± 0.7 ± 0.5	1.13M	136 BATLEY	10C	NA48 ±

• • • We do not use the following data for averages, fits, limits, etc. • • •

17.2 ± 0.9 ± 0.6 670k 137 BATLEY 08A NA48 ±

136 Radiative corrections included. Using Roy equations and including isospin breaking, BATLEY 10C obtains the following scattering lengths $a_0^0 = 0.2220 \pm 0.0128 \pm 0.0050 \pm 0.0037$ (theor.), $a_0^2 = -0.0432 \pm 0.0086 \pm 0.0034 \pm 0.0028$ (theor.). The correlation with $f''_s/f_s = -0.954$ and with $f'_e/f_s = 0.080$. Supersedes BATLEY 08A.

137 Radiative corrections included. Using Roy equations and not including isospin breaking, BATLEY 08A obtains the following $\pi\pi$ scattering length $a_0^0 = 0.233 \pm 0.016 \pm 0.007$, $a_0^2 = -0.0471 \pm 0.011 \pm 0.004$.

- 144 Radiative corrections included. Using Roy equations and including isospin breaking, BATLEY 10C obtains the following scattering lengths $a_0^0 = 0.2220 \pm 0.0128 \pm 0.0050 \pm 0.0037$ (theor.), $a_0^2 = -0.0432 \pm 0.0086 \pm 0.0034 \pm 0.0028$ (theor.). Supersedes BATLEY 08A. The correlation with $g_p'/f_s = -0.914$. Supersedes BATLEY 08A.
- 145 Radiative corrections included. Using Roy equations and not including isospin breaking, BATLEY 08A obtains the following $\pi\pi$ scattering length $a_0^0 = 0.233 \pm 0.016 \pm 0.007$, $a_0^2 = -0.0471 \pm 0.011 \pm 0.004$.
- 146 Radiative corrections included. Using Roy equations PISLAK 03 obtains the following scattering lengths $a_0^0 = 0.203 \pm 0.033 \pm 0.004$, $a_0^2 = -0.055 \pm 0.023 \pm 0.003$.

g_p'/f_s FOR $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ DECAY

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
8.9 ± 1.7 ± 1.3	1.13M	147 BATLEY	10C NA48	±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
8.1 ± 2.2 ± 1.5	670k	148 BATLEY	08A NA48	±
12.0 ± 1.9 ± 0.7	400k	149 PISLAK	03 B865	±

- 147 Radiative corrections included. Using Roy equations and including isospin breaking, BATLEY 10C obtains the following scattering lengths $a_0^0 = 0.2220 \pm 0.0128 \pm 0.0050 \pm 0.0037$ (theor.), $a_0^2 = -0.0432 \pm 0.0086 \pm 0.0034 \pm 0.0028$ (theor.). The correlation with $g_p/f_s = -0.914$. Supersedes BATLEY 08A.
- 148 Radiative corrections included. Using Roy equations and not including isospin breaking, BATLEY 08A obtains the following $\pi\pi$ scattering length $a_0^0 = 0.233 \pm 0.016 \pm 0.007$, $a_0^2 = -0.0471 \pm 0.011 \pm 0.004$.
- 149 Radiative corrections included. Using Roy equations PISLAK 03 obtains the following scattering lengths $a_0^0 = 0.203 \pm 0.033 \pm 0.004$, $a_0^2 = -0.055 \pm 0.023 \pm 0.003$.

h_p/f_s FOR $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$ DECAY

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
-39.8 ± 1.5 ± 0.8	1.13M	150 BATLEY	10C NA48	±
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-41.1 ± 1.9 ± 0.8	670k	151 BATLEY	08A NA48	±
-51.3 ± 3.3 ± 3.5	400k	152 PISLAK	03 B865	±

- 150 Radiative corrections included. Using Roy equations and including isospin breaking, BATLEY 10C obtains the following scattering lengths $a_0^0 = 0.2220 \pm 0.0128 \pm 0.0050 \pm 0.0037$ (theor.), $a_0^2 = -0.0432 \pm 0.0086 \pm 0.0034 \pm 0.0028$ (theor.). Supersedes BATLEY 08A.
- 151 Radiative corrections included. Using Roy equations and not including isospin breaking, BATLEY 08A obtains the following $\pi\pi$ scattering length $a_0^0 = 0.233 \pm 0.016 \pm 0.007$, $a_0^2 = -0.0471 \pm 0.011 \pm 0.004$.
- 152 Radiative corrections included. Using Roy equations PISLAK 03 obtains the following scattering lengths $a_0^0 = 0.203 \pm 0.033 \pm 0.004$, $a_0^2 = -0.055 \pm 0.023 \pm 0.003$.

DECAY FORM FACTOR FOR $K^\pm \rightarrow \pi^0 \pi^0 e^\pm \nu$

Given in BOLOTOV 86B, BARMIN 88B, and SHIMIZU 04.

$K^\pm \rightarrow \ell^\pm \nu_\ell \gamma$ FORM FACTORS

For definitions of the axial-vector F_A and vector F_V form factor, see the "Note on $\pi^\pm \rightarrow \ell^\pm \nu_\ell \gamma$ and $K^\pm \rightarrow \ell^\pm \nu_\ell \gamma$ Form Factors" in the π^\pm section. In the kaon literature, often different definitions $a_K = F_A/m_K$ and $v_K = F_V/m_K$ are used.

$F_A + F_V$, SUM OF AXIAL-VECTOR AND VECTOR FORM FACTOR FOR $K \rightarrow e\nu_e\gamma$

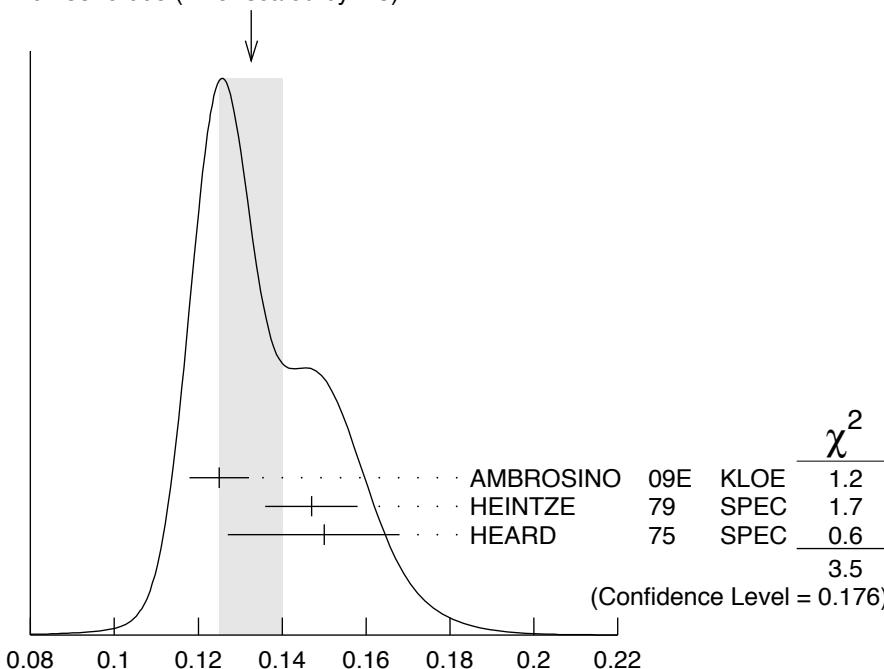
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.133±0.008 OUR AVERAGE				Error includes scale factor of 1.3. See the ideogram below.
0.125±0.007±0.001	1.4K	153 AMBROSINO	09E KLOE	E_γ in 10–250 MeV, $p_e > 200$ MeV/c
0.147±0.011	51	154 HEINTZ	79 SPEC	
0.150 ^{+0.018} _{-0.023}	56	155 HEARD	75 SPEC	

153 Vector form factor fitted with a linear function, $V(x) = F_V (1 + \lambda(1-x))$, $x = 2E_\gamma/m_K$. The fitted value of $\lambda = 0.38 \pm 0.20 \pm 0.02$ with a correlation of -0.93 between $(F_V + F_A)$ and λ .

154 HEINTZ 79 quotes absolute value of $|F_A + F_V| \sin\theta_c$. We use $\sin\theta_c = V_{us} = 0.2205$.

155 HEARD 75 quotes absolute value of $|F_A + F_V| \sin\theta_c$. We use $\sin\theta_c = V_{us} = 0.2205$.

WEIGHTED AVERAGE
0.133±0.008 (Error scaled by 1.3)



$F_A + F_V$, SUM OF AXIAL-VECTOR AND VECTOR FORM FACTOR
FOR $K \rightarrow e\nu_e\gamma$

$F_A + F_V$, SUM OF AXIAL-VECTOR AND VECTOR FORM FACTOR FOR $K \rightarrow \mu\nu_\mu\gamma$

VALUE	CL%	EVTS	DOCUMENT ID	TECN	CHG
0.165±0.007±0.011		2588	156 ADLER	00B B787	+

• • • We do not use the following data for averages, fits, limits, etc. • • •

-1.2 to 1.1	90	DEMIDOV	90	XEBC
< 0.23	90	156 AKIBA	85	SPEC

156 Quotes absolute value. Sign not determined.

$F_A - F_V$, DIFFERENCE OF AXIAL-VECTOR AND VECTOR FORM FACTOR FOR $K \rightarrow e\nu_e\gamma$

VALUE	EVTS	DOCUMENT ID	TECN
<0.49	90	157 HEINTZE	79 SPEC

157 HEINTZE 79 quotes $|F_A - F_V| < \sqrt{11} |F_A + F_V|$.

$F_A - F_V$, DIFFERENCE OF AXIAL-VECTOR AND VECTOR FORM FACTOR FOR $K \rightarrow \mu\nu_\mu\gamma$

VALUE	CL%	EVTS	DOCUMENT ID	TECN	CHG
-0.24 to 0.04	90	2588	ADLER	00B B787	+

• • • We do not use the following data for averages, fits, limits, etc. • • •

-2.2 to 0.6	90	DEMIDOV	90	XEBC
-2.5 to 0.3	90	AKIBA	85	SPEC

K^\pm CHARGE RADIUS

VALUE (fm)	DOCUMENT ID	COMMENT
0.560±0.031 OUR AVERAGE		
0.580±0.040	AMENDOLIA 86B	$K e \rightarrow K e$
0.530±0.050	DALLY 80	$K e \rightarrow K e$
• • • We do not use the following data for averages, fits, limits, etc. • • •		
0.620±0.037	BLATNIK 79	VMD + dispersion relations

CP VIOLATION TESTS IN K^+ AND K^- DECAYS

$$\Delta(K_{\pi ee}^\pm) = \frac{\Gamma(K_{\pi ee}^+) - \Gamma(K_{\pi ee}^-)}{\Gamma(K_{\pi ee}^+) + \Gamma(K_{\pi ee}^-)}$$

VALUE (units 10^{-2})	DOCUMENT ID	TECN
-2.2±1.5±0.6	158 BATLEY 09	NA48

158 This implies an upper limit of 2.1×10^{-2} at 90% CL.

$$\Delta(K_{\pi \mu \mu}^\pm) = \frac{\Gamma(K_{\pi \mu \mu}^+) - \Gamma(K_{\pi \mu \mu}^-)}{\Gamma(K_{\pi \mu \mu}^+) + \Gamma(K_{\pi \mu \mu}^-)}$$

VALUE	DOCUMENT ID	TECN
0.010±0.023 OUR AVERAGE		
0.011±0.023	159 BATLEY 11A	NA48
-0.02 ± 0.11 ± 0.04	PARK 02	HYCP

159 This corresponds to the asymmetry upper limit of $< 2.9 \times 10^{-2}$ at 90% CL.

$$\Delta(K_{\pi\pi\gamma}^{\pm}) = \frac{\Gamma(K_{\pi\pi\gamma}^{+}) - \Gamma(K_{\pi\pi\gamma}^{-})}{\Gamma(K_{\pi\pi\gamma}^{+}) + \Gamma(K_{\pi\pi\gamma}^{-})}$$

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN
0.0 ± 1.0 ± 0.6	1M	160	BATLEY
		10A	NA48

160 This value implies the upper bound for this asymmetry 1.5×10^{-3} at 90% CL.

FORWARD-BACKWARD ASYMMETRY IN K^{\pm} DECAYS

$$A_{FB}(K_{\pi\mu\mu}^{\pm}) = \frac{\Gamma(\cos(\theta_{K\mu}) > 0) - \Gamma(\cos(\theta_{K\mu}) < 0)}{\Gamma(\cos(\theta_{K\mu}) > 0) + \Gamma(\cos(\theta_{K\mu}) < 0)}$$

VALUE	CL%	DOCUMENT ID	TECN
<2.3 × 10⁻²	90	161	BATLEY
		11A	NA48

161 BATLEY 11A gives a corresponding value of the asymmetry $A_{FB} = (-2.4 \pm 1.8) \times 10^{-2}$.

T VIOLATION TESTS IN K^+ AND K^- DECAYS

P_T in $K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$

T-violating muon polarization. Sensitive to new sources of CP violation beyond the Standard Model.

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	CHG
-1.7 ± 2.3 ± 1.1	162	ABE	04F K246	+
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-4.2 ± 4.9 ± 0.9	3.9M	ABE	99S K246	+

162 Includes three sets of data: 96-97 (ABE 99S), 98, and 99-00 totaling about three times the ABE 99S data sample. Corresponds to $P_T < 5.0 \times 10^{-3}$ at 90% CL.

P_T in $K^+ \rightarrow \mu^+ \nu_\mu \gamma$

T-violating muon polarization. Sensitive to new sources of CP violation beyond the Standard Model.

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	CHG
-0.64 ± 1.85 ± 0.10	114k	163 ANISIMOVS...	03 K246	+

163 Muons stopped and polarization measured from decay to positrons.

$\text{Im}(\xi)$ in $K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$ DECAY (from transverse μ pol.)

Test of T reversal invariance.

VALUE	EVTS	DOCUMENT ID	TECN	CHG	COMMENT
-0.006 ± 0.008 OUR AVERAGE					
-0.0053 ± 0.0071 ± 0.0036	164	ABE	04F K246	+	
-0.016 ± 0.025	20M	CAMPBELL	81 CNTR	+	Pol.
• • • We do not use the following data for averages, fits, limits, etc. • • •					
-0.013 ± 0.016 ± 0.003	3.9M	ABE	99S CNTR	+	p_T K^+ at rest

164 Includes three sets of data: 96-97 (ABE 99S), 98, and 99-00 totaling about three times the ABE 99S data sample. Corresponds to $\text{Im}(\xi) < 0.016$ at 90% CL.

HAITT	69B	PL 29B 696	D. Haidt <i>et al.</i>	(AACH, BARI, CERN, EPOL+)
CRONIN	68B	Vienna Conf. 241	J.W. Cronin	(PRIN)
Rapporteur talk.				
WILLIS	67	Heidelberg Conf. 273	W.J. Willis	(YALE)
Rapporteur talk.				
CABIBBO	66	Berkeley Conf. 33	N. Cabibbo	(CERN)
ADAIR	64	PL 12 67	R.K. Adair, L.B. Leipuner	(YALE, BNL)
CABIBBO	64	PL 9 352	N. Cabibbo, A. Maksymowicz	(CERN)
Also		PL 11 360	N. Cabibbo, A. Maksymowicz	(CERN)
Also		PL 14 72	N. Cabibbo, A. Maksymowicz	(CERN)
BIRGE	63	PRL 11 35	R.W. Birge <i>et al.</i>	(LRL, WISC, BARI)
BLOCK	62B	CERN Conf. 371	M.M. Block, L. Lendinara, L. Monari	(NWES, BGNA)
BRENE	61	NP 22 553	N. Brene, L. Egardt, B. Qvist	(NORD)
