LIGHT QUARKS (u, d, s)

OMITTED FROM SUMMARY TABLE

u-QUARK MASS

The u-, d-, and s-quark masses are estimates of so-called "current-quark masses," in a mass- independent subtraction scheme such as $\overline{\text{MS}}$. The ratios m_u/m_d and m_s/m_d are extracted from pion and kaon masses using chiral symmetry. The estimates of d and u masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the u quark could be essentially massless. The s-quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the $\overline{\text{MS}}$ masses at a renormalization scale of $\mu = 2$ GeV. Results quoted in the literature at $\mu = 1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID		TECN	COMMENT
$2.3^{+0.7}_{-0.5}$ OUR EVALUATION	See the ideogram below.			
$2.15\pm0.03\pm0.10$	[1] DURR	11	LATT	$\overline{\text{MS}}$ scheme
$2.24\pm0.10\pm0.34$	[2] BLUM	10	LATT	$\overline{\text{MS}}$ scheme
2.01 ± 0.14	[3] MCNEILE	10	LATT	$\overline{\text{MS}}$ scheme
2.9 ± 0.2	[4] DOMINGUEZ	09	THEO	$\overline{\text{MS}}$ scheme
2.7 ± 0.4	[5] JAMIN	06	THEO	$\overline{\text{MS}}$ scheme
1.9 ± 0.2	[6] MASON	06	LATT	$\overline{\text{MS}}$ scheme
2.8 ± 0.2	[7] NARISON	06	THEO	$\overline{\text{MS}}$ scheme
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.01 ± 0.14	[3] DAVIES	10	LATT	$\overline{\text{MS}}$ scheme
2.9 ± 0.8	[8] DEANDREA	08	THEO	$\overline{\text{MS}}$ scheme
3.02 ± 0.33	[9] BLUM	07	LATT	$\overline{\text{MS}}$ scheme
1.7 ± 0.3	[10] AUBIN	04A	LATT	$\overline{\text{MS}}$ scheme

[1] DURR 11 determine quark mass from a lattice computation of the meson spectrum using $N_f = 2 + 1$ dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual m_u, m_d values are obtained using the lattice determination of the average mass m_{ud} and of the ratio m_s/m_{ud} and the value of $Q = (m_s^2 - m_{\text{ud}}^2) / (m_d^2 - m_u^2)$ as determined from $\eta \rightarrow 3\pi$ decays.

[2] BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use 2+1 dynamical quark flavors.

[3] DAVIES 10 and MCNEILE 10 determine $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$ using a lattice computation with $N_f = 2 + 1$ dynamical fermions of the pseudoscalar meson masses. Mass m_u is obtained from this using the value of m_c from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios, $m_s/\overline{m}$ and m_u/m_d.

[4] DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order α_s^4.

[5] JAMIN 06 determine m_u(2 GeV) by combining the value of m_s obtained from the spectral function for the scalar $K\pi$ form factor with other determinations of the quark mass ratios.

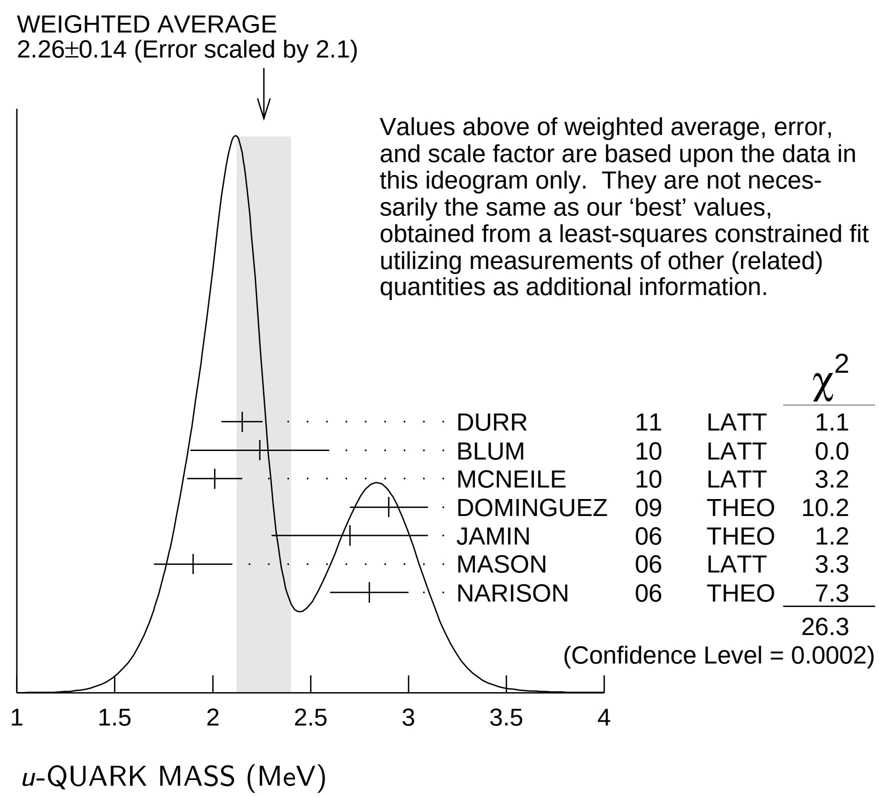
[6] MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order. The quark masses m_u and m_d were determined from their $(m_u+m_d)/2$ measurement and AUBIN 04A m_u/m_d value.

[7] NARISON 06 uses sum rules for $e^+e^- \rightarrow$ hadrons to order α_s^3 to determine m_s combined with other determinations of the quark mass ratios.

[8] DEANDREA 08 determine $m_u - m_d$ from $\eta \rightarrow 3\pi^0$, and combine with the PDG 06 lattice average value of $m_u+m_d = 7.6 \pm 1.6$ to determine m_u and m_d.

[9] BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

[10] AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.



d-QUARK MASS

See the comment for the *u* quark above.

We have normalized the $\overline{\text{MS}}$ masses at a renormalization scale of $\mu = 2$ GeV. Results quoted in the literature at $\mu = 1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	*DOCUMENT ID*		*TECN*	*COMMENT*
4.8 $^{+0.5}_{-0.3}$ OUR EVALUATION	See the ideogram below.			
4.79±0.07±0.12	[1] DURR	11	LATT	$\overline{\text{MS}}$ scheme
4.65±0.15±0.32	[2] BLUM	10	LATT	$\overline{\text{MS}}$ scheme
4.77±0.15	[3] MCNEILE	10	LATT	$\overline{\text{MS}}$ scheme
5.3 ±0.4	[4] DOMINGUEZ	09	THEO	$\overline{\text{MS}}$ scheme
4.8 ±0.5	[5] JAMIN	06	THEO	$\overline{\text{MS}}$ scheme
4.4 ±0.3	[6] MASON	06	LATT	$\overline{\text{MS}}$ scheme
5.1 ±0.4	[7] NARISON	06	THEO	$\overline{\text{MS}}$ scheme
• • • We do not use the following data for averages, fits, limits, etc. • • •				
4.79±0.16	[3] DAVIES	10	LATT	$\overline{\text{MS}}$ scheme
4.7 ±0.8	[8] DEANDREA	08	THEO	$\overline{\text{MS}}$ scheme
5.49±0.39	[9] BLUM	07	LATT	$\overline{\text{MS}}$ scheme
3.9 ±0.5	[10] AUBIN	04A	LATT	$\overline{\text{MS}}$ scheme

[1] DURR 11 determine quark mass from a lattice computation of the meson spectrum using $N_f = 2 + 1$ dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual m_u, m_d values are obtained using the lattice determination of the average mass m_{ud} and of the ratio m_s/m_{ud} and the value of $Q = (m_s^2 - m_{\text{ud}}^2) / (m_d^2 - m_u^2)$ as determined from $\eta \rightarrow 3\pi$ decays.

[2] BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use 2+1 dynamical quark flavors.

[3] DAVIES 10 and MCNEILE 10 determine $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$ using a lattice computation with $N_f = 2 + 1$ dynamical fermions of the pseudoscalar meson masses. Mass m_d is obtained from this using the value of m_c from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios, $m_s/\overline{m}$ and m_u/m_d.

[4] DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order α_s^4.

[5] JAMIN 06 determine m_d(2 GeV) by combining the value of m_s obtained from the spectral function for the scalar $K\pi$ form factor with other determinations of the quark mass ratios.

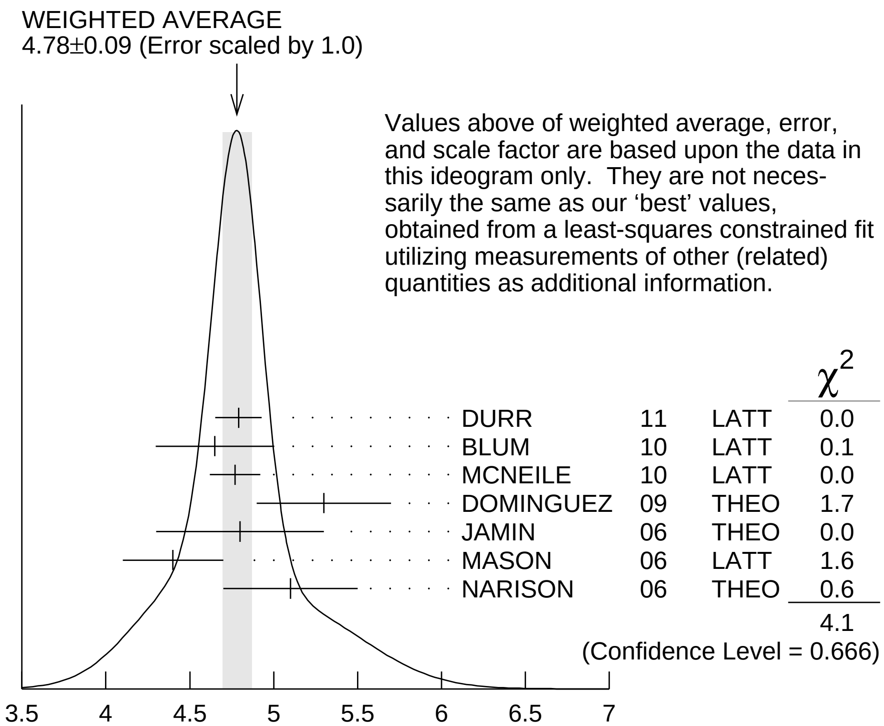
[6] MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate *u* and *d* quarks. Perturbative corrections were included at NNLO order. The quark masses m_u and m_d were determined from their $(m_u+m_d)/2$ measurement and AUBIN 04A m_u/m_d value.

[7] NARISON 06 uses sum rules for $e^+e^- \rightarrow$ hadrons to order α_s^3 to determine m_s combined with other determinations of the quark mass ratios.

[8] DEANDREA 08 determine $m_u - m_d$ from $\eta \rightarrow 3\pi^0$, and combine with the PDG 06 lattice average value of $m_u+m_d = 7.6 \pm 1.6$ to determine m_u and m_d.

[9] BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

[10] AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.



d-QUARK MASS (MeV)

$\overline{m} = (m_u + m_d)/2$

See the comments for the *u* quark above.

We have normalized the $\overline{\text{MS}}$ masses at a renormalization scale of $\mu = 2$ GeV. Results quoted in the literature at $\mu = 1$ GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	*DOCUMENT ID*		*TECN*	*COMMENT*
3.5 $^{+0.7}_{-0.2}$ **OUR EVALUATION**	See the ideogram below.			
3.59 ±0.21	[1] AOKI	11A	LATT	$\overline{\text{MS}}$ scheme
3.469±0.047±0.048	[2] DURR	11	LATT	$\overline{\text{MS}}$ scheme
3.6 ±0.2	[3] BLOSSIER	10	LATT	$\overline{\text{MS}}$ scheme
3.39 ±0.06	[4] MCNEILE	10	LATT	$\overline{\text{MS}}$ scheme
4.1 ±0.2	[5] DOMINGUEZ	09	THEO	$\overline{\text{MS}}$ scheme
3.72 ±0.41	[6] ALLTON	08	LATT	$\overline{\text{MS}}$ scheme

3.55	$^{+0.65}_{-0.28}$		[7] ISHIKAWA	08	LATT	$\overline{\text{MS}}$ scheme
4.25	±0.35		[8] BLUM	07	LATT	$\overline{\text{MS}}$ scheme
4.08	±0.25	±0.42	[9] GOCKELER	06	LATT	$\overline{\text{MS}}$ scheme
4.7	±0.2	±0.3	[10] GOCKELER	06A	LATT	$\overline{\text{MS}}$ scheme
3.2	±0.3		[11] MASON	06	LATT	$\overline{\text{MS}}$ scheme
3.95	±0.3		[12] NARISON	06	THEO	$\overline{\text{MS}}$ scheme

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.40	±0.07		[4] DAVIES	10	LATT	$\overline{\text{MS}}$ scheme
3.85	±0.12	±0.4	[13] BLOSSIER	08	LATT	$\overline{\text{MS}}$ scheme
≥ 4.85	±0.20		[14] DOMINGUEZ...	08B	THEO	$\overline{\text{MS}}$ scheme
4.026	±0.048		[15] NAKAMURA	08	LATT	$\overline{\text{MS}}$ scheme
2.8	±0.3		[16] AUBIN	04	LATT	$\overline{\text{MS}}$ scheme
4.29	±0.14	±0.65	[17] AOKI	03	LATT	$\overline{\text{MS}}$ scheme
3.223	±0.3		[18] AOKI	03B	LATT	$\overline{\text{MS}}$ scheme
4.4	±0.1	±0.4	[19] BECIREVIC	03	LATT	$\overline{\text{MS}}$ scheme
4.1	±0.3	±1.0	[20] CHIU	03	LATT	$\overline{\text{MS}}$ scheme

[1] AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using $N_f = 2 + 1$ dynamical flavors of domain wall fermions.

[2] DURR 11 determine quark mass from a lattice computation of the meson spectrum using $N_f = 2 + 1$ dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

[3] BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using N_f=2 dynamical twisted-mass Wilson fermions.

[4] DAVIES 10 and MCNEILE 10 determine $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$ using a lattice computation with $N_f = 2 + 1$ dynamical fermions of the pseudoscalar meson masses. Mass $\overline{m}$ is obtained from this using the value of m_c from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratio, $m_s/\overline{m}$.

[5] DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order α_s^4.

[6] ALLTON 08 use a lattice computation of the π, K, and Ω masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.

[7] ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of $\mathcal{O}(a)$ improved Wilson quarks, and one-loop perturbative renormalization.

[8] BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

[9] GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with $N_f = 2$ dynamical light quark flavors, and non-perturbative renormalization, to obtain $\overline{m}(2\text{ GeV}) = 4.08 \pm 0.25 \pm 0.19 \pm 0.23$ MeV, where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.

[10] GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with $N_f = 2$ dynamical light quark flavors, and non-perturbative renormalization.

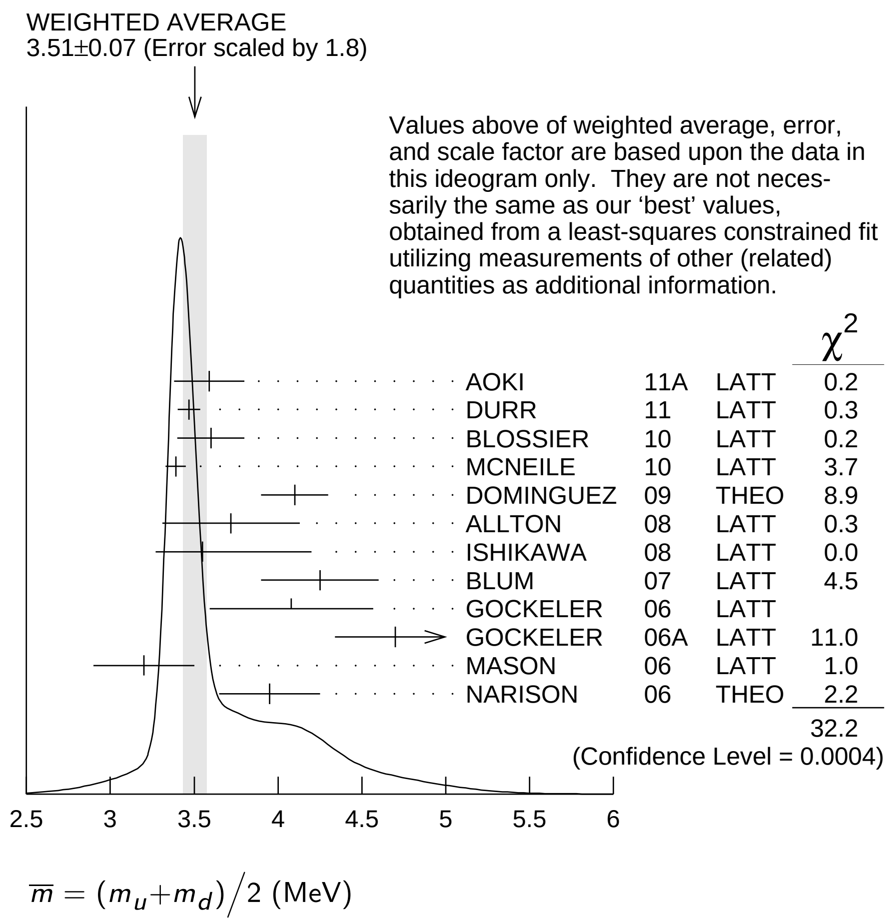
[11] MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order.

[12] NARISON 06 uses sum rules for $e^+ e^- \to$ hadrons to order α_s^3 to determine m_s combined with other determinations of the quark mass ratios.

[13] BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.

[14] DOMINGUEZ-CLARIMON 08B obtain an inequality from sum rules for the scalar two-point correlator.

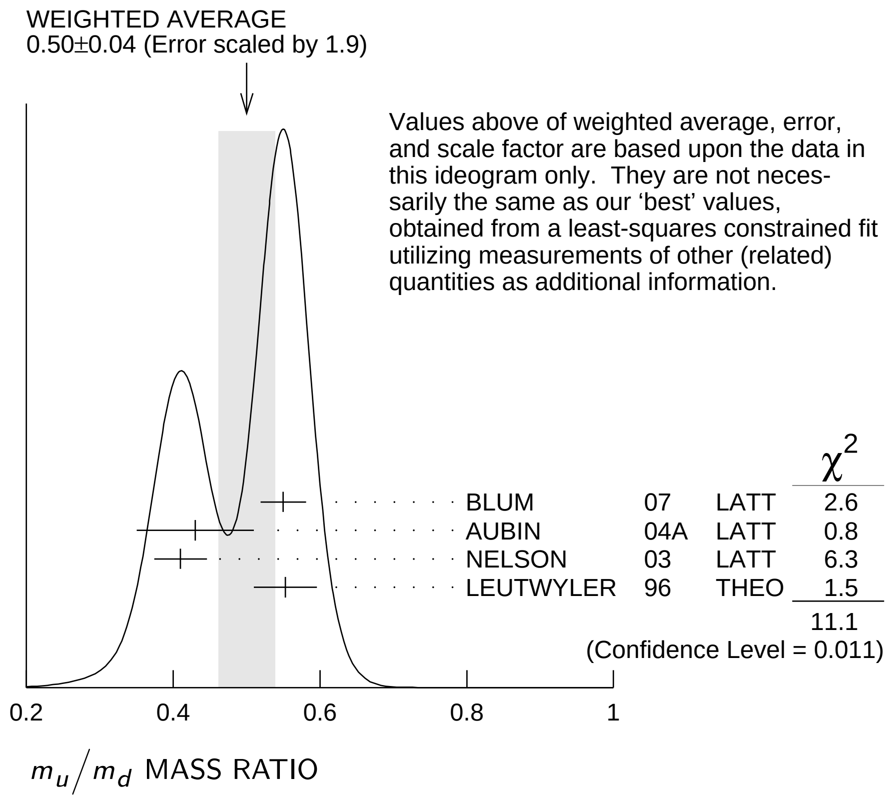
[15] NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
[16] AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
[17] AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.
[18] The errors given in AOKI 03B were $^{+0.046}_{-0.069}$. We changed them to ±0.3 for calculating the overall best values. AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the $\mathcal{O}(a)$ improved Wilson action.
[19] BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses $\mathcal{O}(a)$ improved Wilson action and nonperturbative renormalization.
[20] CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.



m_u/m_d MASS RATIO

VALUE	*DOCUMENT ID*		*TECN*	*COMMENT*
0.38–0.58 OUR EVALUATION	See the ideogram below.			
0.550 ± 0.031	[1] BLUM	07	LATT	
$0.43\ \pm0.08$	[2] AUBIN	04A	LATT	
0.410 ± 0.036	[3] NELSON	03	LATT	
0.553 ± 0.043	[4] LEUTWYLER	96	THEO	Compilation

[1] BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
[2] AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.
[3] NELSON 03 computes coefficients in the order p^4 chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio m_u/m_d is obtained by combining this with the chiral perturbation theory computation of the meson masses to order p^4.
[4] LEUTWYLER 96 uses a combined fit to $\eta \rightarrow 3\pi$ and $\psi' \rightarrow J/\psi$ (π,η) decay rates, and the electromagnetic mass differences of the π and K.



s-QUARK MASS

See the comment for the *u* quark above.

We have normalized the $\overline{\text{MS}}$ masses at a renormalization scale of $\mu = 2$ GeV. Results quoted in the literature at $\mu = 1$ GeV have been rescaled by dividing by 1.35.

VALUE (MeV)	*DOCUMENT ID*		*TECN*	*COMMENT*
95 ± 5 OUR EVALUATION	See the ideogram below.			
94 ± 9	[1] BODENSTEIN	13	THEO	$\overline{\text{MS}}$ scheme
102 ± 3 ± 1	[2] FRITZSCH	12	LATT	$\overline{\text{MS}}$ scheme
96.2± 2.7	[3] AOKI	11A	LATT	$\overline{\text{MS}}$ scheme
95.5± 1.1± 1.5	[4] DURR	11	LATT	$\overline{\text{MS}}$ scheme
95 ± 6	[5] BLOSSIER	10	LATT	$\overline{\text{MS}}$ scheme
97.6± 2.9± 5.5	[6] BLUM	10	LATT	$\overline{\text{MS}}$ scheme
92.2± 1.3	[7] MCNEILE	10	LATT	$\overline{\text{MS}}$ scheme
107.3±11.7	[8] ALLTON	08	LATT	$\overline{\text{MS}}$ scheme

102 ± 8	[9] DOMINGUEZ	08A	THEO	$\overline{\text{MS}}$ scheme
$90.1^{+17.2}_{-\ 6.1}$	[10] ISHIKAWA	08	LATT	$\overline{\text{MS}}$ scheme
105 ± 6 ± 7	[11] CHETYRKIN	06	THEO	$\overline{\text{MS}}$ scheme
111 ± 6 ±10	[12] GOCKELER	06	LATT	$\overline{\text{MS}}$ scheme
119 ± 5 ± 8	[13] GOCKELER	06A	LATT	$\overline{\text{MS}}$ scheme
92 ± 9	[14] JAMIN	06	THEO	$\overline{\text{MS}}$ scheme
87 ± 6	[15] MASON	06	LATT	$\overline{\text{MS}}$ scheme
104 ±15	[16] NARISON	06	THEO	$\overline{\text{MS}}$ scheme
• • • We do not use the following data for averages, fits, limits, etc. • • •				
92.4± 1.5	[7] DAVIES	10	LATT	$\overline{\text{MS}}$ scheme
105 ± 3 ± 9	[17] BLOSSIER	08	LATT	$\overline{\text{MS}}$ scheme
105.6± 1.2	[18] NAKAMURA	08	LATT	$\overline{\text{MS}}$ scheme
119.5± 9.3	[19] BLUM	07	LATT	$\overline{\text{MS}}$ scheme
$\geq 71 \pm 4,\ \leq 151 \pm 14$	[20] NARISON	06	THEO	$\overline{\text{MS}}$ scheme
$96\ ^{+5}_{-3}\ ^{+16}_{-18}$	[21] BAIKOV	05	THEO	$\overline{\text{MS}}$ scheme
81 ±22	[22] GAMIZ	05	THEO	$\overline{\text{MS}}$ scheme
125 ±28	[23] GORBUNOV	05	THEO	$\overline{\text{MS}}$ scheme
93 ±32	[24] NARISON	05	THEO	$\overline{\text{MS}}$ scheme
76 ± 8	[25] AUBIN	04	LATT	$\overline{\text{MS}}$ scheme
116 ± 6 ± 0.65	[26] AOKI	03	LATT	$\overline{\text{MS}}$ scheme
$84.5^{+12}_{-\ 1.7}$	[27] AOKI	03B	LATT	$\overline{\text{MS}}$ scheme
106 ± 2 ± 8	[28] BECIREVIC	03	LATT	$\overline{\text{MS}}$ scheme
92 ± 9 ±16	[29] CHIU	03	LATT	$\overline{\text{MS}}$ scheme
117 ±17	[30] GAMIZ	03	THEO	$\overline{\text{MS}}$ scheme
103 ±17	[31] GAMIZ	03	THEO	$\overline{\text{MS}}$ scheme

[1] BODENSTEIN 13 determines m_s from QCD finite energy sum rules, and the perturbative computation of the pseudoscalar correlator to five-loop order.

[2] FRITZSCH 12 determine m_s using a lattice computation with $N_f = 2$ dynamical flavors.

[3] AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using $N_f = 2 + 1$ dynamical flavors of domain wall fermions.

[4] DURR 11 determine quark mass from a lattice computation of the meson spectrum using $N_f = 2 + 1$ dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

[5] BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using N_f=2 dynamical twisted-mass Wilson fermions.

[6] BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use 2+1 dynamical quark flavors.

[7] DAVIES 10 and MCNEILE 10 determine $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$ using a lattice computation with $N_f = 2 + 1$ dynamical fermions of the pseudoscalar meson masses. Mass m_s is obtained from this using the value of m_c from ALLISON 08 or MCNEILE 10.

[8] ALLTON 08 use a lattice computation of the π, K, and Ω masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.

[9] DOMINGUEZ 08A make determination from QCD finite energy sum rules for the pseudoscalar two-point function computed to order α_s^4.

[10] ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of $\mathcal{O}(a)$ improved Wilson quarks, and one-loop perturbative renormalization.

[11] CHETYRKIN 06 use QCD sum rules in the pseudoscalar channel to order α_s^4.

[12] GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with $N_f = 2$ dynamical light quark flavors, and non-perturbative renormalization, to obtain $\overline{m}_s(2\text{ GeV}) = 111 \pm 6 \pm 4 \pm 6$ MeV, where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.

[13] GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with $N_f = 2$ dynamical light quark flavors, and non-perturbative renormalization.

[14] JAMIN 06 determine $\overline{m}_s(2\text{ GeV})$ from the spectral function for the scalar $K\pi$ form factor.

[15] MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate u and d quarks. Perturbative corrections were included at NNLO order.

[16] NARISON 06 uses sum rules for $e^+ e^- \to$ hadrons to order α_s^3.

[17] BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.

[18] NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.

[19] BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

[20] NARISON 06 obtains the quoted range from positivity of the spectral functions.

[21] BAIKOV 05 determines $\overline{m}_s(M_\tau) = 100^{+5}_{-3}{}^{+17}_{-19}$ from sum rules using the strange spectral function in τ decay. The computations were done to order α_s^3, with an estimate of the α_s^4 terms. We have converted the result to $\mu = 2$ GeV.

[22] GAMIZ 05 determines $\overline{m}_s(2\text{ GeV})$ from sum rules using the strange spectral function in τ decay. The computations were done to order α_s^2, with an estimate of the α_s^3 terms.

[23] GORBUNOV 05 use hadronic tau decays to N^3LO, including power corrections.

[24] NARISON 05 determines $\overline{m}_s(2\text{ GeV})$ from sum rules using the strange spectral function in τ decay. The computations were done to order α_s^3.

[25] AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.

[26] AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory. Determines m_s=$113.8 \pm 2.3^{+5.8}_{-2.9}$ using K mass as input and m_s=$142.3 \pm 5.8^{+22}_{-\ 0}$ using ϕ mass as input. We have performed a weighted average of these values.

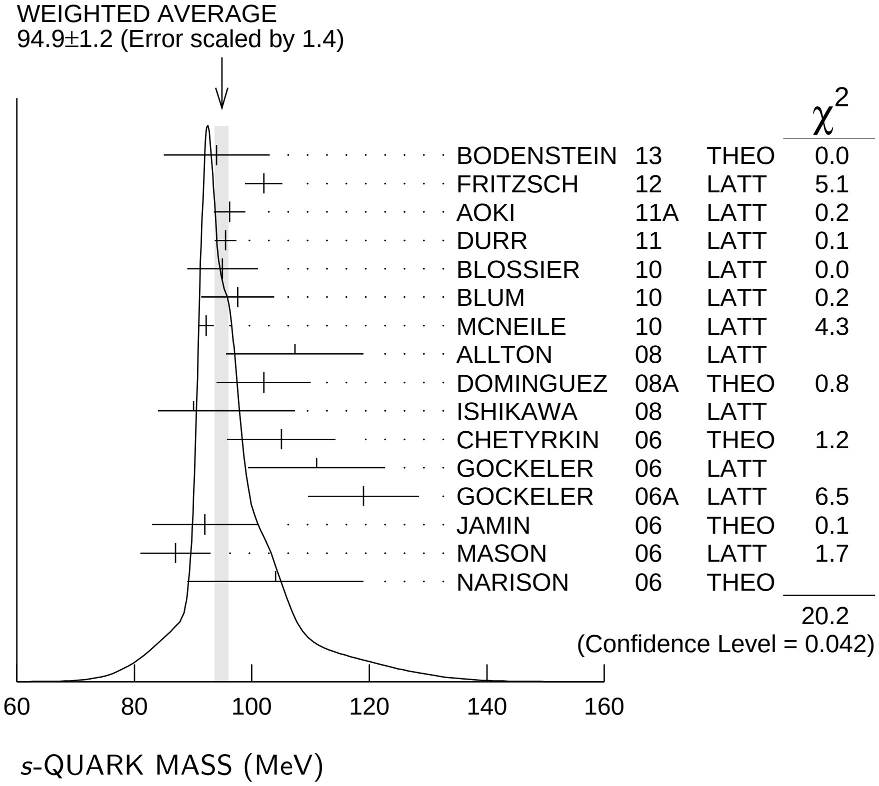
[27] AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the $\mathcal{O}(a)$ improved Wilson action.

[28] BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses $\mathcal{O}(a)$ improved Wilson action and nonperturbative renormalization. They also quote $\overline{m}/m_s$=$24.3 \pm 0.2 \pm 0.6$.

[29] CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.

[30] GAMIZ 03 determines m_s from SU(3) breaking in the τ hadronic width. The value of V_{us} is chosen to satisfy CKM unitarity.

[31] GAMIZ 03 determines m_s from SU(3) breaking in the τ hadronic width. The value of V_{us} is taken from the PDG.



OTHER LIGHT QUARK MASS RATIOS

m_s/m_d MASS RATIO

VALUE	DOCUMENT ID		TECN	COMMENT
17–22 OUR EVALUATION				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
20.0	[1] GAO	97	THEO	
18.9±0.8	[2] LEUTWYLER	96	THEO	Compilation
21	[3] DONOGHUE	92	THEO	
18	[4] GERARD	90	THEO	
18 to 23	[5] LEUTWYLER	90B	THEO	

[1] GAO 97 uses electromagnetic mass splittings of light mesons.

[2] LEUTWYLER 96 uses a combined fit to $\eta \rightarrow 3\pi$ and $\psi' \rightarrow J/\psi\ (\pi,\eta)$ decay rates, and the electromagnetic mass differences of the π and K.

[3] DONOGHUE 92 result is from a combined analysis of meson masses, $\eta \rightarrow 3\pi$ using second-order chiral perturbation theory including nonanalytic terms, and $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$.

[4] GERARD 90 uses large N and η-η' mixing.

[5] LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine L_7.

$m_s/\overline{m}$ MASS RATIO

$\overline{m} \equiv (m_u + m_d)/2$

VALUE	DOCUMENT ID		TECN
27.5 ±1.0 OUR EVALUATION	See the ideogram below.		
26.8 ±1.4	[1] AOKI	11A	LATT
27.53±0.20±0.08	[2] DURR	11	LATT
27.3 ±0.9	[3] BLOSSIER	10	LATT
28.8 ±1.65	[4] ALLTON	08	LATT
27.3 ±0.3 ±1.2	[5] BLOSSIER	08	LATT
23.5 ±1.5	[6] OLLER	07A	THEO
• • • We do not use the following data for averages, fits, limits, etc. • • •			
27.4 ±0.4	[7] AUBIN	04	LATT

[1] AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using $N_f = 2 + 1$ dynamical flavors of domain wall fermions.

[2] DURR 11 determine quark mass from a lattice computation of the meson spectrum using $N_f = 2 + 1$ dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

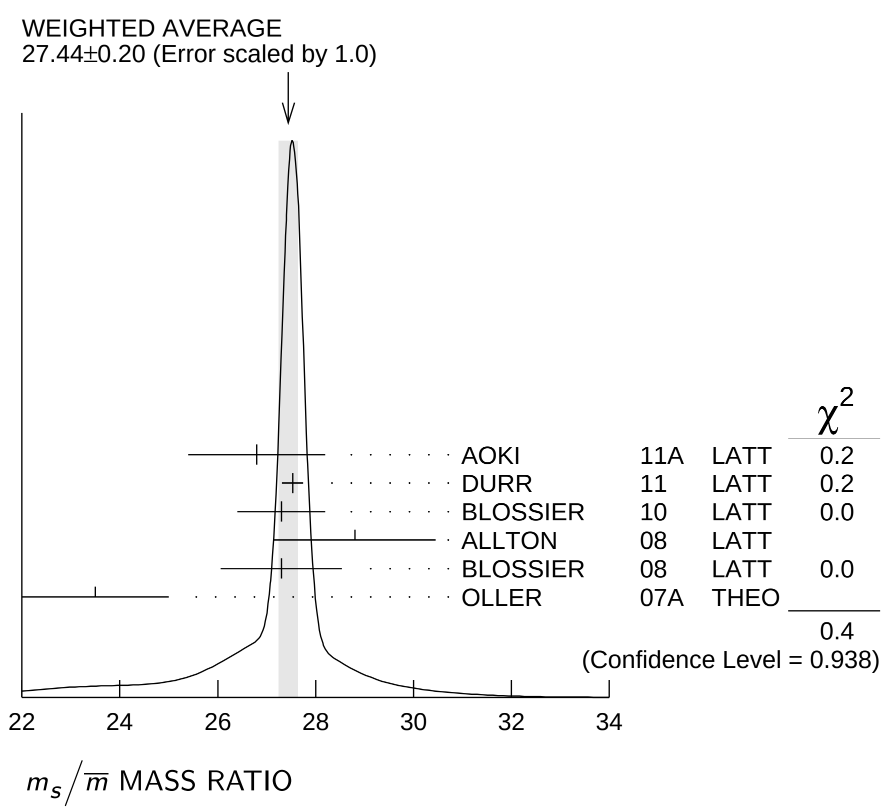
[3] BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using N_f=2 dynamical twisted-mass Wilson fermions.

[4] ALLTON 08 use a lattice computation of the π, K, and Ω masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.

[5] BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.

[6] OLLER 07A use unitarized chiral perturbation theory to order p^4.

[7] Three flavor dynamical lattice calculation of pseudoscalar meson masses.



Q MASS RATIO

$Q \equiv \sqrt{(m^2{}_s - \overline{m}^2)/(m^2{}_d - m^2{}_u)}$; $\overline{m} \equiv (m_u + m_d)/2$

VALUE	DOCUMENT ID		TECN
• • • We do not use the following data for averages, fits, limits, etc. • • •			
22.8±0.4	[1] MARTEMYA...	05	THEO
22.7±0.8	[2] ANISOVICH	96	THEO

[1] MARTEMYANOV 05 determine Q from $\eta \to 3\pi$ decay.

[2] ANISOVICH 96 find Q from $\eta \to \pi^+ \pi^- \pi^0$ decay using dispersion relations and chiral perturbation theory.

LIGHT QUARKS (*u*, *d*, *s*) REFERENCES

BODENSTEIN	13	JHEP 1307 138	S. Bodenstein, C.A. Dominguez, K. Schilcher (MANZ+)
FRITZSCH	12	NP B865 397	P. Fritzsch *et al.* (ALPHA Collab.)
AOKI	11A	PR D83 074508	Y. Aoki *et al.* (RBC-UKQCD Collab.)
DURR	11	PL B701 265	S. Durr *et al.* (BMW Collab.)
BAZAVOV	10	RMP 82 1349	A. Bazavov *et al.* (MILC Collab.)
BLOSSIER	10	PR D82 114513	B. Blossier *et al.* (ETM Collab.)
BLUM	10	PR D82 094508	T. Blum *et al.*
DAVIES	10	PRL 104 132003	C.T.H. Davies *et al.* (HPQCD Collab.)
MCNEILE	10	PR D82 034512	C. McNeile *et al.* (HPQCD Collab.)
DOMINGUEZ	09	PR D79 014009	C.A. Dominguez *et al.*
ALLISON	08	PR D78 054513	I. Allison *et al.* (HPQCD Collab.)
ALLTON	08	PR D78 114509	C. Allton *et al.* (RBC and UKQCD Collab.)
BLOSSIER	08	JHEP 0804 020	B. Blossier *et al.* (ETM Collab.)
DEANDREA	08	PR D78 034032	A. Deandrea, A. Nehme, P. Talavera
DOMINGUEZ	08A	JHEP 0805 020	C.A. Dominguez *et al.*
DOMINGUEZ...	08B	PL B660 49	A. Dominguez-Clarimon, E. de Rafael, J. Taron
ISHIKAWA	08	PR D78 011502	T. Ishikawa *et al.* (CP-PACS and JLQCD Collab.)
NAKAMURA	08	PR D78 034502	Y. Nakamura *et al.* (CP-PACS Collab.)
BLUM	07	PR D76 114508	T. Blum *et al.* (RBC Collab.)
OLLER	07A	EPJ A34 371	J.A. Oller, L. Roca
CHETYRKIN	06	EPJ C46 721	K.G. Chetyrkin, A. Khodjamirian
GOCKELER	06	PR D73 054508	M. Gockeler *et al.* (QCDSF, UKQCD Collabs)
GOCKELER	06A	PL B639 307	M. Gockeler *et al.* (QCDSF, UKQCD Collabs)
JAMIN	06	PR D74 074009	M. Jamin, J.A. Oller, A. Pich
MASON	06	PR D73 114501	Q. Mason *et al.* (HPQCD Collab.)
NARISON	06	PR D74 034013	S. Narison
PDG	06	JP G33 1	W.-M. Yao *et al.* (PDG Collab.)
BAIKOV	05	PRL 95 012003	P.A. Baikov, K.G. Chetyrkin, J.H. Kuhn
GAMIZ	05	PRL 94 011803	E. Gamiz *et al.*
GORBUNOV	05	PR D71 013002	D.S. Gorbunov, A.A. Pivovarov
MARTEMYA...	05	PR D71 017501	B.V. Martemyanov, V.S. Sopov
NARISON	05	PL B626 101	S. Narison
AUBIN	04	PR D70 031504	C. Aubin *et al.* (HPQCD, MILC, UKQCD Collabs.)
AUBIN	04A	PR D70 114501	C. Aubin *et al.* (MILC Collab.)
AOKI	03	PR D67 034503	S. Aoki *et al.* (CP-PACS Collab.)
AOKI	03B	PR D68 054502	S. Aoki *et al.* (CP-PACS Collab.)
BECIREVIC	03	PL B558 69	D. Becirevic, V. Lubicz, C. Tarantino
CHIU	03	NP B673 217	T.-W. Chiu, T.-H. Hsieh
GAMIZ	03	JHEP 0301 060	E. Gamiz *et al.*
NELSON	03	PRL 90 021601	D. Nelson, G.T. Fleming, G.W. Kilcup
GAO	97	PR D56 4115	D.-N. Gao, B.A. Li, M.-L. Yan
ANISOVICH	96	PL B375 335	A.V. Anisovich, H. Leutwyler
LEUTWYLER	96	PL B378 313	H. Leutwyler
DONOGHUE	92	PRL 69 3444	J.F. Donoghue, B.R. Holstein, D. Wyler (MASA+)
GERARD	90	MPL A5 391	J.M. Gerard (MPIM)
LEUTWYLER	90B	NP B337 108	H. Leutwyler (BERN)