

Extra Dimensions

For explanation of terms used and discussion of significant model dependence of following limits, see the “Extra Dimensions” review. Footnotes describe originally quoted limit. δ indicates the number of extra dimensions.

Limits not encoded here are summarized in the “Extra Dimensions” review, where the latest unpublished results are also described.

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Limits on R from Deviations in Gravitational Force Law

This section includes limits on the size of extra dimensions from deviations in the Newtonian ($1/r^2$) gravitational force law at short distances. Deviations are parametrized by a gravitational potential of the form $V = -(G m m'/r) [1 + \alpha \exp(-r/R)]$. For δ toroidal extra dimensions of equal size, $\alpha = 8\delta/3$. Quoted bounds are for $\delta = 2$ unless otherwise noted.

<u>VALUE (μm)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>COMMENT</u>
< 30	95	¹ KAPNER 07	Torsion pendulum
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
		² XU 13	Nuclei properties
		³ BEZERRA 11	Torsion oscillator
		⁴ SUSHKOV 11	Torsion pendulum
		⁵ BEZERRA 10	Microcantilever
		⁶ MASUDA 09	Torsion pendulum
		⁷ GERACI 08	Microcantilever
		⁸ TRENKEL 08	Newton's constant
		⁹ DECCA 07A	Torsion oscillator
< 47	95	¹⁰ TU 07	Torsion pendulum
		¹¹ SMULLIN 05	Microcantilever
<130	95	¹² HOYLE 04	Torsion pendulum
		¹³ CHIAVERINI 03	Microcantilever
\lesssim 200	95	¹⁴ LONG 03	Microcantilever
<190	95	¹⁵ HOYLE 01	Torsion pendulum
		¹⁶ HOSKINS 85	Torsion pendulum

¹ KAPNER 07 search for new forces, probing a range of $\alpha \simeq 10^{-3}$ – 10^5 and length scales $R \simeq 10$ – $1000 \mu\text{m}$. For $\delta = 1$ the bound on R is $44 \mu\text{m}$. For $\delta = 2$, the bound is expressed in terms of M_* , here translated to a bound on the radius. See their Fig. 6 for details on the bound.

- ² XU 13 obtain constraints on non-Newtonian forces with strengths $|\alpha| \simeq 10^{34}\text{--}10^{36}$ and length scales $R \simeq 1\text{--}10$ fm. See their Fig. 4 for more details. These constraints do not place limits on the size of extra flat dimensions.
 - ³ BEZERRA 11 obtain constraints on non-Newtonian forces with strengths $10^{11} \lesssim |\alpha| \lesssim 10^{18}$ and length scales $R = 30\text{--}1260$ nm. See their Fig. 2 for more details. These constraints do not place limits on the size of extra flat dimensions.
 - ⁴ SUSHKOV 11 obtain improved limits on non-Newtonian forces with strengths $10^7 \lesssim |\alpha| \lesssim 10^{11}$ and length scales $0.4 \mu\text{m} < R < 4 \mu\text{m}$ (95% CL). See their Fig. 2. These bounds do not place limits on the size of extra flat dimensions. However, a model dependent bound of $M_* > 70$ TeV is obtained assuming gauge bosons that couple to baryon number also propagate in $(4 + \delta)$ dimensions.
 - ⁵ BEZERRA 10 obtain improved constraints on non-Newtonian forces with strengths $10^{19} \lesssim |\alpha| \lesssim 10^{29}$ and length scales $R = 1.6\text{--}14$ nm (95% CL). See their Fig. 1. This bound does not place limits on the size of extra flat dimensions.
 - ⁶ MASUDA 09 obtain improved constraints on non-Newtonian forces with strengths $10^9 \lesssim |\alpha| \lesssim 10^{11}$ and length scales $R = 1.0\text{--}2.9 \mu\text{m}$ (95% CL). See their Fig. 3. This bound does not place limits on the size of extra flat dimensions.
 - ⁷ GERACI 08 obtain improved constraints on non-Newtonian forces with strengths $|\alpha| > 14,000$ and length scales $R = 5\text{--}15 \mu\text{m}$. See their Fig. 9. This bound does not place limits on the size of extra flat dimensions.
 - ⁸ TRENKEL 08 uses two independent measurements of Newton's constant G to constrain new forces with strength $|\alpha| \simeq 10^{-4}$ and length scales $R = 0.02\text{--}1$ m. See their Fig. 1. This bound does not place limits on the size of extra flat dimensions.
 - ⁹ DECCA 07A search for new forces and obtain bounds in the region with strengths $|\alpha| \simeq 10^{13}\text{--}10^{18}$ and length scales $R = 20\text{--}86$ nm. See their Fig. 6. This bound does not place limits on the size of extra flat dimensions.
 - ¹⁰ TU 07 search for new forces probing a range of $|\alpha| \simeq 10^{-1}\text{--}10^5$ and length scales $R \simeq 20\text{--}1000 \mu\text{m}$. For $\delta = 1$ the bound on R is $53 \mu\text{m}$. See their Fig. 3 for details on the bound.
 - ¹¹ SMULLIN 05 search for new forces, and obtain bounds in the region with strengths $\alpha \simeq 10^3\text{--}10^8$ and length scales $R = 6\text{--}20 \mu\text{m}$. See their Figs. 1 and 16 for details on the bound. This work does not place limits on the size of extra flat dimensions.
 - ¹² HOYLE 04 search for new forces, probing α down to 10^{-2} and distances down to $10 \mu\text{m}$. Quoted bound on R is for $\delta = 2$. For $\delta = 1$, bound goes to $160 \mu\text{m}$. See their Fig. 34 for details on the bound.
 - ¹³ CHIAVERINI 03 search for new forces, probing α above 10^4 and λ down to $3 \mu\text{m}$, finding no signal. See their Fig. 4 for details on the bound. This bound does not place limits on the size of extra flat dimensions.
 - ¹⁴ LONG 03 search for new forces, probing α down to 3, and distances down to about $10 \mu\text{m}$. See their Fig. 4 for details on the bound.
 - ¹⁵ HOYLE 01 search for new forces, probing α down to 10^{-2} and distances down to $20 \mu\text{m}$. See their Fig. 4 for details on the bound. The quoted bound is for $\alpha \geq 3$.
 - ¹⁶ HOSKINS 85 search for new forces, probing distances down to 4 mm. See their Fig. 13 for details on the bound. This bound does not place limits on the size of extra flat dimensions.
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Limits on R from On-Shell Production of Gravitons: $\delta = 2$

This section includes limits on on-shell production of gravitons in collider and astrophysical processes. Bounds quoted are on R , the assumed common radius of the flat extra dimensions, for $\delta = 2$ extra dimensions. Studies often quote bounds in terms of derived parameter; experiments are actually sensitive to the masses of the KK gravitons: $m_{\vec{n}} = |\vec{n}|/R$. See the Review on “Extra Dimensions” for details. Bounds are given in μm for $\delta = 2$.

VALUE (μm)	CL%	DOCUMENT ID	TECN	COMMENT
< 15	95	¹ KHACHATRY...15AL	CMS	$pp \rightarrow jG$
< 0.00016	95	² HANNESTAD 03		Neutron star heating
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
	95	³ AAD	15CS ATLS	$pp \rightarrow \gamma G$
< 25	95	⁴ AAD	13AD ATLS	$pp \rightarrow jG$
< 127	95	⁵ AAD	13C ATLS	$pp \rightarrow \gamma G$
< 34.4	95	⁶ AAD	13D ATLS	$pp \rightarrow jj$
< 0.0087	95	⁷ AJELLO	12 FLAT	Neutron star γ sources
< 23	95	⁸ CHATRCHYAN	12AP CMS	$pp \rightarrow jG$
< 92	95	⁹ AAD	11S ATLS	$pp \rightarrow jG$
< 72	95	¹⁰ CHATRCHYAN	11U CMS	$pp \rightarrow jG$
< 245	95	¹¹ AALTONEN	08AC CDF	$p\bar{p} \rightarrow \gamma G, jG$
< 615	95	¹² ABAZOV	08S D0	$p\bar{p} \rightarrow \gamma G$
< 0.916	95	¹³ DAS	08	Supernova cooling
< 350	95	¹⁴ ABULENCIA,A	06 CDF	$p\bar{p} \rightarrow jG$
< 270	95	¹⁵ ABDALLAH	05B DLPH	$e^+e^- \rightarrow \gamma G$
< 210	95	¹⁶ ACHARD	04E L3	$e^+e^- \rightarrow \gamma G$
< 480	95	¹⁷ ACOSTA	04C CDF	$p\bar{p} \rightarrow jG$
< 0.00038	95	¹⁸ CASSE	04	Neutron star γ sources
< 610	95	¹⁹ ABAZOV	03 D0	$p\bar{p} \rightarrow jG$
< 0.96	95	²⁰ HANNESTAD	03	Supernova cooling
< 0.096	95	²¹ HANNESTAD	03	Diffuse γ background
< 0.051	95	²² HANNESTAD	03	Neutron star γ sources
< 300	95	²³ HEISTER	03C ALEP	$e^+e^- \rightarrow \gamma G$
		²⁴ FAIRBAIRN	01	Cosmology
< 0.66	95	²⁵ HANHART	01	Supernova cooling
		²⁶ CASSISI	00	Red giants
<1300	95	²⁷ ACCIARRI	99S L3	$e^+e^- \rightarrow ZG$

¹ KHACHATRYAN 15AL search for $pp \rightarrow jG$, using 19.7 fb^{-1} of data at $\sqrt{s} = 8 \text{ TeV}$ to place bounds on M_D for two to six extra dimensions, from which this bound on R is derived. See their Table 7 for bounds on all $\delta \leq 6$.

² HANNESTAD 03 obtain a limit on R from the heating of old neutron stars by the surrounding cloud of trapped KK gravitons. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits supersede those in HANNESTAD 02.

³ AAD 15CS search for $pp \rightarrow \gamma G$, using 20.3 fb^{-1} of data at $\sqrt{s} = 8 \text{ TeV}$ to place lower limits on M_D for two to six extra dimensions (see their Fig. 18).

⁴ AAD 13AD search for $pp \rightarrow jG$, using 4.7 fb^{-1} of data at $\sqrt{s} = 7 \text{ TeV}$ to place bounds on M_D for two to six extra dimensions, from which this bound on R is derived. See their Table 8 for bounds on all $\delta \leq 6$.

⁵ AAD 13C search for $pp \rightarrow \gamma G$, using 4.6 fb^{-1} of data at $\sqrt{s} = 7 \text{ TeV}$ to place bounds on M_D for two to six extra dimensions, from which this bound on R is derived.

⁶ AAD 13D search for the dijet decay of quantum black holes in 4.8 fb^{-1} of data produced in pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place bounds on M_D for two to seven extra dimensions,

- from which these bounds on R are derived. Limits on M_D for all $\delta \leq 7$ are given in their Table 3.
- 7 AJELLO 12 obtain a limit on R from the gamma-ray emission of point γ sources that arise from the photon decay of KK gravitons which are gravitationally bound around neutron stars. Limits for all $\delta \leq 7$ are given in their Table 7.
 - 8 CHATRCHYAN 12AP search for $pp \rightarrow jG$, using 5.0 fb^{-1} of data at $\sqrt{s} = 7 \text{ TeV}$ to place bounds on M_D for two to six extra dimensions, from which this bound on R is derived. See their Table 7 for bounds on all $\delta \leq 6$.
 - 9 AAD 11S search for $pp \rightarrow jG$, using 33 pb^{-1} of data at $\sqrt{s} = 7 \text{ TeV}$, to place bounds on M_D for two to four extra dimensions, from which these bounds on R are derived. See their Table 3 for bounds on all $\delta \leq 4$.
 - 10 CHATRCHYAN 11U search for $pp \rightarrow jG$, using 36 pb^{-1} of data at $\sqrt{s} = 7 \text{ TeV}$, to place bounds on M_D for two to six extra dimensions, from which these bounds on R are derived. See their Table 3 for bounds on all $\delta \leq 6$.
 - 11 AALTONEN 08AC search for $p\bar{p} \rightarrow \gamma G$ and $p\bar{p} \rightarrow jG$ at $\sqrt{s} = 1.96 \text{ TeV}$ with 2.0 fb^{-1} and 1.1 fb^{-1} respectively, in order to place bounds on the fundamental scale and size of the extra dimensions. See their Table III for limits on all $\delta \leq 6$.
 - 12 ABAZOV 08S search for $p\bar{p} \rightarrow \gamma G$, using 1 fb^{-1} of data at $\sqrt{s} = 1.96 \text{ TeV}$ to place bounds on M_D for two to eight extra dimensions, from which these bounds on R are derived. See their paper for intermediate values of δ .
 - 13 DAS 08 obtain a limit on R from Kaluza-Klein graviton cooling of SN1987A due to plasmon-plasmon annihilation.
 - 14 ABULENCIA,A 06 search for $p\bar{p} \rightarrow jG$ using 368 pb^{-1} of data at $\sqrt{s} = 1.96 \text{ TeV}$. See their Table II for bounds for all $\delta \leq 6$.
 - 15 ABDALLAH 05B search for $e^+e^- \rightarrow \gamma G$ at $\sqrt{s} = 180\text{--}209 \text{ GeV}$ to place bounds on the size of extra dimensions and the fundamental scale. Limits for all $\delta \leq 6$ are given in their Table 6. These limits supersede those in ABREU 00Z.
 - 16 ACHARD 04E search for $e^+e^- \rightarrow \gamma G$ at $\sqrt{s} = 189\text{--}209 \text{ GeV}$ to place bounds on the size of extra dimensions and the fundamental scale. See their Table 8 for limits with $\delta \leq 8$. These limits supersede those in ACCIARRI 99R.
 - 17 ACOSTA 04C search for $p\bar{p} \rightarrow jG$ at $\sqrt{s} = 1.8 \text{ TeV}$ to place bounds on the size of extra dimensions and the fundamental scale. See their paper for bounds on $\delta = 4, 6$.
 - 18 CASSE 04 obtain a limit on R from the gamma-ray emission of point γ sources that arises from the photon decay of gravitons around newly born neutron stars, applying the technique of HANNESTAD 03 to neutron stars in the galactic bulge. Limits for all $\delta \leq 7$ are given in their Table I.
 - 19 ABAZOV 03 search for $p\bar{p} \rightarrow jG$ at $\sqrt{s}=1.8 \text{ TeV}$ to place bounds on M_D for 2 to 7 extra dimensions, from which these bounds on R are derived. See their paper for bounds on intermediate values of δ . We quote results without the approximate NLO scaling introduced in the paper.
 - 20 HANNESTAD 03 obtain a limit on R from graviton cooling of supernova SN1987a. Limits for all $\delta \leq 7$ are given in their Tables V and VI.
 - 21 HANNESTAD 03 obtain a limit on R from gravitons emitted in supernovae and which subsequently decay, contaminating the diffuse cosmic γ background. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits supersede those in HANNESTAD 02.
 - 22 HANNESTAD 03 obtain a limit on R from gravitons emitted in two recent supernovae and which subsequently decay, creating point γ sources. Limits for all $\delta \leq 7$ are given in their Tables V and VI. These limits are corrected in the published erratum.
 - 23 HEISTER 03C use the process $e^+e^- \rightarrow \gamma G$ at $\sqrt{s} = 189\text{--}209 \text{ GeV}$ to place bounds on the size of extra dimensions and the scale of gravity. See their Table 4 for limits with $\delta \leq 6$ for derived limits on M_D .
 - 24 FAIRBAIRN 01 obtains bounds on R from over production of KK gravitons in the early universe. Bounds are quoted in paper in terms of fundamental scale of gravity. Bounds depend strongly on temperature of QCD phase transition and range from $R < 0.13 \mu\text{m}$ to $0.001 \mu\text{m}$ for $\delta=2$; bounds for $\delta=3,4$ can be derived from Table 1 in the paper.

- ²⁵ HANHART 01 obtain bounds on R from limits on graviton cooling of supernova SN 1987a using numerical simulations of proto-neutron star neutrino emission.
- ²⁶ CASSISI 00 obtain rough bounds on M_D (and thus R) from red giant cooling for $\delta=2,3$. See their paper for details.
- ²⁷ ACCIARRI 99S search for $e^+e^- \rightarrow ZG$ at $\sqrt{s}=189$ GeV. Limits on the gravity scale are found in their Table 2, for $\delta \leq 4$.

Mass Limits on M_{TT}

This section includes limits on the cut-off mass scale, M_{TT} , of dimension-8 operators from KK graviton exchange in models of large extra dimensions. Ambiguities in the UV-divergent summation are absorbed into the parameter λ , which is taken to be $\lambda = \pm 1$ in the following analyses. Bounds for $\lambda = -1$ are shown in parenthesis after the bound for $\lambda = +1$, if appropriate. Different papers use slightly different definitions of the mass scale. The definition used here is related to another popular convention by $M_{TT}^4 = (2/\pi) \Lambda_T^4$, as discussed in the above Review on "Extra Dimensions."

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
> 6.3	95	¹ KHACHATRY...15J	CMS	$pp \rightarrow$ dijet, ang. distrib.
>20.6 (> 15.7)	95	² GIUDICE 03	RVUE	Dim-6 operators
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
> 3.7	95	³ KHACHATRY...15AE	CMS	$pp \rightarrow e^+e^-, \mu^+\mu^-$
> 3.8	95	⁴ AAD 14BE	ATLS	$pp \rightarrow e^+e^-, \mu^+\mu^-$
> 2.94 (>2.52)	95	⁵ AAD 13AS	ATLS	$pp \rightarrow \gamma\gamma$
> 3.2	95	⁶ AAD 13E	ATLS	$pp \rightarrow e^+e^-, \mu^+\mu^-, \gamma\gamma$
> 2.66 (>2.27)	95	⁷ AAD 12Y	ATLS	$pp \rightarrow \gamma\gamma$
		⁸ BAAK 12	RVUE	Electroweak
> 2.86	95	⁹ CHATRCHYAN 12J	CMS	$pp \rightarrow e^+e^-, \mu^+\mu^-$
> 2.84 (>2.41)	95	¹⁰ CHATRCHYAN 12R	CMS	$pp \rightarrow \gamma\gamma$
> 0.90 (>0.92)	95	¹¹ AARON 11C	H1	$e^\pm p \rightarrow e^\pm X$
> 1.74 (>1.71)	95	¹² CHATRCHYAN 11A	CMS	$pp \rightarrow \gamma\gamma$
> 1.48	95	¹³ ABAZOV 09AE	D0	$p\bar{p} \rightarrow$ dijet, ang. distrib.
> 1.45	95	¹⁴ ABAZOV 09D	D0	$p\bar{p} \rightarrow e^+e^-, \gamma\gamma$
> 1.1 (> 1.0)	95	¹⁵ SCHAELE 07A	ALEP	$e^+e^- \rightarrow e^+e^-$
> 0.898 (> 0.998)	95	¹⁶ ABDALLAH 06C	DLPH	$e^+e^- \rightarrow \ell^+\ell^-$
> 0.853 (> 0.939)	95	¹⁷ GERDES 06		$p\bar{p} \rightarrow e^+e^-, \gamma\gamma$
> 0.96 (> 0.93)	95	¹⁸ ABAZOV 05V	D0	$p\bar{p} \rightarrow \mu^+\mu^-$
> 0.78 (> 0.79)	95	¹⁹ CHEKANOV 04B	ZEUS	$e^\pm p \rightarrow e^\pm X$
> 0.805 (> 0.956)	95	²⁰ ABBIENDI 03D	OPAL	$e^+e^- \rightarrow \gamma\gamma$
> 0.7 (> 0.7)	95	²¹ ACHARD 03D	L3	$e^+e^- \rightarrow ZZ$
> 0.82 (> 0.78)	95	²² ADLOFF 03	H1	$e^\pm p \rightarrow e^\pm X$
> 1.28 (> 1.25)	95	²³ GIUDICE 03	RVUE	
> 0.80 (> 0.85)	95	²⁴ HEISTER 03C	ALEP	$e^+e^- \rightarrow \gamma\gamma$
> 0.84 (> 0.99)	95	²⁵ ACHARD 02D	L3	$e^+e^- \rightarrow \gamma\gamma$
> 1.2 (> 1.1)	95	²⁶ ABBOTT 01	D0	$p\bar{p} \rightarrow e^+e^-, \gamma\gamma$
> 0.60 (> 0.63)	95	²⁷ ABBIENDI 00R	OPAL	$e^+e^- \rightarrow \mu^+\mu^-$
> 0.63 (> 0.50)	95	²⁷ ABBIENDI 00R	OPAL	$e^+e^- \rightarrow \tau^+\tau^-$
> 0.68 (> 0.61)	95	²⁷ ABBIENDI 00R	OPAL	$e^+e^- \rightarrow \mu^+\mu^-, \tau^+\tau^-$
		²⁸ ABREU 00A	DLPH	$e^+e^- \rightarrow \gamma\gamma$
> 0.680 (> 0.542)	95	²⁹ ABREU 00S	DLPH	$e^+e^- \rightarrow \mu^+\mu^-, \tau^+\tau^-$

> 15–28	99.7	30	CHANG	00B	RVUE	Electroweak
> 0.98	95	31	CHEUNG	00	RVUE	$e^+e^- \rightarrow \gamma\gamma$
> 0.29–0.38	95	32	GRAESSER	00	RVUE	$(g-2)_\mu$
> 0.50–1.1	95	33	HAN	00	RVUE	Electroweak
> 2.0 (> 2.0)	95	34	MATHEWS	00	RVUE	$\bar{p}p \rightarrow jj$
> 1.0 (> 1.1)	95	35	MELE	00	RVUE	$e^+e^- \rightarrow VV$
		36	ABBIENDI	99P	OPAL	
		37	ACCIARRI	99M	L3	
		38	ACCIARRI	99S	L3	
> 1.412 (> 1.077)	95	39	BOURILKOV	99		$e^+e^- \rightarrow e^+e^-$

¹ KHACHATRYAN 15J use dijet angular distributions in 19.7 fb^{-1} of data from pp collisions at $\sqrt{s} = 8 \text{ TeV}$ to place a lower bound on $\Lambda_{\mathcal{T}}$, here converted to $M_{\mathcal{T}\mathcal{T}}$.

² GIUDICE 03 place bounds on Λ_6 , the coefficient of the gravitationally-induced dimension-6 operator $(2\pi\lambda/\Lambda_6^2)(\sum \bar{f}\gamma_\mu\gamma^5 f)(\sum \bar{f}\gamma^\mu\gamma^5 f)$, using data from a variety of experiments. Results are quoted for $\lambda = \pm 1$ and are independent of δ .

³ KHACHATRYAN 15AE use $20.6 (19.7) \text{ fb}^{-1}$ of data from pp collisions at $\sqrt{s} = 8 \text{ TeV}$ in the dimuon (dielectron) channel to place a lower limit on $\Lambda_{\mathcal{T}}$, here converted to $M_{\mathcal{T}\mathcal{T}}$.

⁴ AAD 14BE use 20 fb^{-1} of data from pp collisions at $\sqrt{s} = 8 \text{ TeV}$ in the dilepton channel to place lower limits on $M_{\mathcal{T}\mathcal{T}}$ (equivalent to their M_S).

⁵ AAD 13AS use 4.9 fb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place lower limits on $M_{\mathcal{T}\mathcal{T}}$ (equivalent to their M_S).

⁶ AAD 13E use 4.9 and 5.0 fb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ in the dielectron and dimuon channels, respectively, to place lower limits on $M_{\mathcal{T}\mathcal{T}}$ (equivalent to their M_S). The dielectron and dimuon channels are combined with previous results in the diphoton channel to set the best limit. Bounds on individual channels and different priors can be found in their Table VIII.

⁷ AAD 12Y use 2.12 fb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place lower limits on $M_{\mathcal{T}\mathcal{T}}$ (equivalent to their M_S).

⁸ BAAK 12 use electroweak precision observables to place bounds on the ratio $\Lambda_{\mathcal{T}}/M_D$ as a function of M_D . See their Fig. 22 for constraints with a Higgs mass of 120 GeV .

⁹ CHATRCHYAN 12J use approximately 2 fb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ in the dielectron and dimuon channels to place lower limits on $\Lambda_{\mathcal{T}}$, here converted to $M_{\mathcal{T}\mathcal{T}}$.

¹⁰ CHATRCHYAN 12R use 2.2 fb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place lower limits on $M_{\mathcal{T}\mathcal{T}}$ (equivalent to their M_S).

¹¹ AARON 11C search for deviations in the differential cross section of $e^\pm p \rightarrow e^\pm X$ in 446 pb^{-1} of data taken at $\sqrt{s} = 301$ and 319 GeV to place a bound on $M_{\mathcal{T}\mathcal{T}}$.

¹² CHATRCHYAN 11A use 36 pb^{-1} of data from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place lower limits on $\Lambda_{\mathcal{T}}$, here converted to $M_{\mathcal{T}\mathcal{T}}$.

¹³ ABAZOV 09AE use dijet angular distributions in 0.7 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place lower bounds on $\Lambda_{\mathcal{T}}$ (equivalent to their M_S), here converted to $M_{\mathcal{T}\mathcal{T}}$.

¹⁴ ABAZOV 09D use 1.05 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place lower bounds on $\Lambda_{\mathcal{T}}$ (equivalent to their M_S), here converted to $M_{\mathcal{T}\mathcal{T}}$.

¹⁵ SCHAEEL 07A use e^+e^- collisions at $\sqrt{s} = 189\text{--}209 \text{ GeV}$ to place lower limits on $\Lambda_{\mathcal{T}}$, here converted to limits on $M_{\mathcal{T}\mathcal{T}}$.

¹⁶ ABDALLAH 06C use e^+e^- collisions at $\sqrt{s} \sim 130\text{--}207 \text{ GeV}$ to place lower limits on $M_{\mathcal{T}\mathcal{T}}$, which is equivalent to their definition of M_S . Bound shown includes all possible final state leptons, $\ell = e, \mu, \tau$. Bounds on individual leptonic final states can be found in their Table 31.

¹⁷ GERDES 06 use 100 to 110 pb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.8 \text{ TeV}$, as recorded by the CDF Collaboration during Run I of the Tevatron. Bound shown includes

- a K -factor of 1.3. Bounds on individual e^+e^- and $\gamma\gamma$ final states are found in their Table I.
- 18 ABAZOV 05V use 246 pb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for deviations in the differential cross section to $\mu^+\mu^-$ from graviton exchange.
 - 19 CHEKANOV 04B search for deviations in the differential cross section of $e^\pm p \rightarrow e^\pm X$ with 130 pb^{-1} of combined data and Q^2 values up to $40,000 \text{ GeV}^2$ to place a bound on M_{TT} .
 - 20 ABBIENDI 03D use e^+e^- collisions at $\sqrt{s}=181\text{--}209 \text{ GeV}$ to place bounds on the ultra-violet scale M_{TT} , which is equivalent to their definition of M_S .
 - 21 ACHARD 03D look for deviations in the cross section for $e^+e^- \rightarrow ZZ$ from $\sqrt{s} = 200\text{--}209 \text{ GeV}$ to place a bound on M_{TT} .
 - 22 ADLOFF 03 search for deviations in the differential cross section of $e^\pm p \rightarrow e^\pm X$ at $\sqrt{s}=301$ and 319 GeV to place bounds on M_{TT} .
 - 23 GIUDICE 03 review existing experimental bounds on M_{TT} and derive a combined limit.
 - 24 HEISTER 03C use e^+e^- collisions at $\sqrt{s}= 189\text{--}209 \text{ GeV}$ to place bounds on the scale of dim-8 gravitational interactions. Their M_S^\pm is equivalent to our M_{TT} with $\lambda=\pm 1$.
 - 25 ACHARD 02 search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}} = 192\text{--}209 \text{ GeV}$.
 - 26 ABBOTT 01 search for variations in differential cross sections to e^+e^- and $\gamma\gamma$ final states at the Tevatron.
 - 27 ABBIENDI 00R uses e^+e^- collisions at $\sqrt{s}= 189 \text{ GeV}$.
 - 28 ABREU 00A search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}}= 189\text{--}202 \text{ GeV}$.
 - 29 ABREU 00S uses e^+e^- collisions at $\sqrt{s}=183$ and 189 GeV . Bounds on μ and τ individual final states given in paper.
 - 30 CHANG 00B derive 3σ limit on M_{TT} of $(28,19,15) \text{ TeV}$ for $\delta=(2,4,6)$ respectively assuming the presence of a torsional coupling in the gravitational action. Highly model dependent.
 - 31 CHEUNG 00 obtains limits from anomalous diphoton production at OPAL due to graviton exchange. Original limit for $\delta=4$. However, unknown UV theory renders δ dependence unreliable. Original paper works in HLZ convention.
 - 32 GRAESSER 00 obtains a bound from graviton contributions to $g-2$ of the muon through loops of 0.29 TeV for $\delta=2$ and 0.38 TeV for $\delta=4,6$. Limits scale as $\lambda^{1/2}$. However calculational scheme not well-defined without specification of high-scale theory. See the "Extra Dimensions Review."
 - 33 HAN 00 calculates corrections to gauge boson self-energies from KK graviton loops and constrain them using S and T . Bounds on M_{TT} range from 0.5 TeV ($\delta=6$) to 1.1 TeV ($\delta=2$); see text. Limits have strong dependence, $\lambda^{\delta+2}$, on unknown λ coefficient.
 - 34 MATHEWS 00 search for evidence of graviton exchange in CDF and $D\bar{O}$ dijet production data. See their Table 2 for slightly stronger δ -dependent bounds. Limits expressed in terms of $\tilde{M}_S^4 = M_{TT}^4/8$.
 - 35 MELE 00 obtains bound from KK graviton contributions to $e^+e^- \rightarrow VV$ ($V=\gamma, W, Z$) at LEP. Authors use Hewett conventions.
 - 36 ABBIENDI 99P search for s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma$ at $E_{\text{cm}}=189 \text{ GeV}$. The limits $G_+ > 660 \text{ GeV}$ and $G_- > 634 \text{ GeV}$ are obtained from combined $E_{\text{cm}}=183$ and 189 GeV data, where G_\pm is a scale related to the fundamental gravity scale.
 - 37 ACCIARRI 99M search for the reaction $e^+e^- \rightarrow \gamma G$ and s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma, W^+W^-, ZZ, e^+e^-, \mu^+\mu^-, \tau^+\tau^-, q\bar{q}$ at $E_{\text{cm}}=183 \text{ GeV}$. Limits on the gravity scale are listed in their Tables 1 and 2.
 - 38 ACCIARRI 99S search for the reaction $e^+e^- \rightarrow ZG$ and s -channel graviton exchange effects in $e^+e^- \rightarrow \gamma\gamma, W^+W^-, ZZ, e^+e^-, \mu^+\mu^-, \tau^+\tau^-, q\bar{q}$ at $E_{\text{cm}}=189 \text{ GeV}$. Limits on the gravity scale are listed in their Tables 1 and 2.

³⁹BOURILKOV 99 performs global analysis of LEP data on e^+e^- collisions at $\sqrt{s}=183$ and 189 GeV. Bound is on Λ_T .

Limits on $1/R = M_c$

This section includes limits on $1/R = M_c$, the compactification scale in models with one TeV-sized extra dimension, due to exchange of Standard Model KK excitations. Bounds assume fermions are not in the bulk, unless stated otherwise. See the “Extra Dimensions” review for discussion of model dependence.

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
>4.16	95	¹ AAD	12CC ATLS	$pp \rightarrow \ell\bar{\ell}$
>6.1		² BARBIERI	04 RVUE	Electroweak
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
>3.8	95	³ ACCOMANDO 15	RVUE	Electroweak
>3.40	95	⁴ KHACHATRYAN 15T	CMS	$pp \rightarrow \ell X$
	95	⁵ CHATRCHYAN 13AQ	CMS	$pp \rightarrow \ell X$
>1.38	95	⁶ CHATRCHYAN 13W	CMS	$pp \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>0.715	95	⁷ EDELHAUSER 13	RVUE	$pp \rightarrow \ell\bar{\ell} + X$
>1.40	95	⁸ AAD	12CP ATLS	$pp \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>1.23	95	⁹ AAD	12X ATLS	$pp \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>0.26	95	¹⁰ ABAZOV	12M D0	$p\bar{p} \rightarrow \mu\mu$
>0.75	95	¹¹ BAAK	12 RVUE	Electroweak
		¹² FLACKE	12 RVUE	Electroweak
>0.43	95	¹³ NISHIWAKI	12 RVUE	$H \rightarrow WW, \gamma\gamma$
>0.729	95	¹⁴ AAD	11F ATLS	$pp \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>0.961	95	¹⁵ AAD	11X ATLS	$pp \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>0.477	95	¹⁶ ABAZOV	10P D0	$p\bar{p} \rightarrow \gamma\gamma, \delta=6, M_D=5$ TeV
>1.59	95	¹⁷ ABAZOV	09AE D0	$p\bar{p} \rightarrow$ dijet, angular dist.
>0.6	95	¹⁸ HAISCH	07 RVUE	$\bar{B} \rightarrow X_s \gamma$
>0.6	90	¹⁹ GOGOLADZE	06 RVUE	Electroweak
>3.3	95	²⁰ CORNET	00 RVUE	Electroweak
> 3.3–3.8	95	²¹ RIZZO	00 RVUE	Electroweak

¹AAD 12CC use 4.9 and 5.0 fb^{-1} of data from pp collisions at $\sqrt{s} = 7$ TeV in the dielectron and dimuon channels, respectively, to place a lower bound on the mass of the lightest KK Z/γ boson (equivalent to $1/R = M_c$). The limit quoted here assumes a flat prior corresponding to when the pure Z/γ KK cross section term dominates. See their Section 15 for more details.

²BARBIERI 04 use electroweak precision observables to place a lower bound on the compactification scale $1/R$. Both the gauge bosons and the Higgs boson are assumed to propagate in the bulk.

³ACCOMANDO 15 use electroweak precision observables to place a lower bound on the compactification scale $1/R$. See their Fig. 2 for the bound as a function of $\sin\beta$, which parametrizes the VEV contribution from brane and bulk Higgs fields. The quoted value is for the minimum bound which occurs at $\sin\beta = 0.45$.

⁴KHACHATRYAN 15T use 19.7 fb^{-1} of data from pp collisions at $\sqrt{s} = 8$ TeV to place a lower bound on the compactification scale $1/R$.

⁵CHATRCHYAN 13AQ use 5.0 fb^{-1} of data from pp collisions at $\sqrt{s} = 7$ TeV and a further 3.7 fb^{-1} of data at $\sqrt{s} = 8$ TeV to place a lower bound on the compactification scale $1/R$, in models with universal extra dimensions and Standard Model fields propagating in the bulk. See their Fig. 5 for the bound as a function of the universal bulk fermion mass parameter μ .

- ⁶ CHATRCHYAN 13W use diphoton events with large missing transverse momentum in 4.93 fb^{-1} of data produced from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays. The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.
- ⁷ EDELHAUSER 13 use 19.6 and 20.6 fb^{-1} of data from pp collisions at $\sqrt{s} = 8 \text{ TeV}$ analyzed by the CMS Collaboration in the dielectron and dimuon channels, respectively, to place a lower bound on the mass of the second lightest Kaluza-Klein Z/γ boson (converted to a limit on $1/R = M_C$). The bound assumes Standard Model fields propagating in the bulk and that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$.
- ⁸ AAD 12CP use diphoton events with large missing transverse momentum in 4.8 fb^{-1} of data produced from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays. The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.
- ⁹ AAD 12X use diphoton events with large missing transverse momentum in 1.07 fb^{-1} of data produced from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays. The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.
- ¹⁰ ABAZOV 12M use same-sign dimuon events in 7.3 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the compactification scale $1/R$, in models with universal extra dimensions where all Standard Model fields propagate in the bulk.
- ¹¹ BAAK 12 use electroweak precision observables to place a lower bound on the compactification scale $1/R$, in models with universal extra dimensions and Standard Model fields propagating in the bulk. Bound assumes a 125 GeV Higgs mass. See their Fig. 25 for the bound as a function of the Higgs mass.
- ¹² FLACKE 12 use electroweak precision observables to place a lower bound on the compactification scale $1/R$, in models with universal extra dimensions and Standard Model fields propagating in the bulk. See their Fig. 1 for the bound as a function of the universal bulk fermion mass parameter μ .
- ¹³ NISHIWAKI 12 use up to 2 fb^{-1} of data from the ATLAS and CMS experiments that constrains the production cross section of a Higgs-like particle to place a lower bound on the compactification scale $1/R$ in universal extra dimension models. The quoted bound assumes Standard Model fields propagating in the bulk and a 125 GeV Higgs mass. See their Fig. 1 for the bound as a function of the Higgs mass.
- ¹⁴ AAD 11F use diphoton events with large missing transverse energy in 3.1 pb^{-1} of data produced from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays. The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.
- ¹⁵ AAD 11X use diphoton events with large missing transverse energy in 36 pb^{-1} of data produced from pp collisions at $\sqrt{s} = 7 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays. The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_C = 20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.
- ¹⁶ ABAZOV 10P use diphoton events with large missing transverse energy in 6.3 fb^{-1} of data produced from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the compactification scale in a universal extra dimension model with gravitational decays.

The bound assumes that the cutoff scale Λ , for the radiative corrections to the Kaluza-Klein masses, satisfies $\Lambda/M_c=20$. The model parameters are chosen such that the decay $\gamma^* \rightarrow G\gamma$ occurs with an appreciable branching fraction.

- 17 ABAZOV 09AE use dijet angular distributions in 0.7 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the compactification scale.
- 18 HAISCH 07 use inclusive \bar{B} -meson decays to place a Higgs mass independent bound on the compactification scale $1/R$ in the minimal universal extra dimension model.
- 19 GOGOLADZE 06 use electroweak precision observables to place a lower bound on the compactification scale in models with universal extra dimensions. Bound assumes a 115 GeV Higgs mass. See their Fig. 3 for the bound as a function of the Higgs mass.
- 20 CORNET 00 translates a bound on the coefficient of the 4-fermion operator $(\bar{\ell}\gamma_\mu\tau^a\ell)(\bar{\ell}\gamma^\mu\tau^a\ell)$ derived by Hagiwara and Matsumoto into a limit on the mass scale of KK W bosons.
- 21 RIZZO 00 obtains limits from global electroweak fits in models with a Higgs in the bulk (3.8 TeV) or on the standard brane (3.3 TeV).

Limits on Kaluza-Klein Gravitons in Warped Extra Dimensions

This sections places limits on the mass of the first Kaluza-Klein (KK) excitation of the graviton in the warped extra dimension model of Randall and Sundrum. Bounds in parenthesis assume Standard Model fields propagate in the bulk. Experimental bounds depend strongly on the warp parameter, k . See the "Extra Dimensions" review for a full discussion.

Here we list limits for the value of the warp parameter $k/\overline{M}_P = 0.1$.

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
>2.73	95	1 KHACHATRY...15AE	CMS	$pp \rightarrow e^+e^-, \mu^+\mu^-$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
>2.66	95	2 AAD	15AD ATLS	$pp \rightarrow G \rightarrow \gamma\gamma$
	95	3 AAD	15BK ATLS	$pp \rightarrow G \rightarrow hh$
	95	4 KHACHATRY...15R	CMS	$pp \rightarrow G \rightarrow hh$
>2.68	95	5 AAD	14V ATLS	$pp \rightarrow G \rightarrow e^+e^-, \mu^+\mu^-$
	95	6 KHACHATRY...14A	CMS	$pp \rightarrow G \rightarrow WW, ZZ, WZ$
>1.23 (> 0.84)	95	7 AAD	13A ATLS	$pp \rightarrow G \rightarrow WW$
>2.23	95	8 AAD	13AS ATLS	$pp \rightarrow \gamma\gamma, e^+e^-, \mu^+\mu^-$
>2.39	95	9 CHATRCHYAN 13AF	CMS	$pp \rightarrow e^+e^-, \mu^+\mu^-$
	95	10 CHATRCHYAN 13U	CMS	$pp \rightarrow G \rightarrow ZZ$
>0.845	95	11 AAD	12AD ATLS	$pp \rightarrow G \rightarrow ZZ$
>2.16	95	12 AAD	12CC ATLS	$pp \rightarrow G \rightarrow \ell\bar{\ell}$
>1.95	95	13 AAD	12Y ATLS	$pp \rightarrow \gamma\gamma, e^+e^-, \mu^+\mu^-$
	95	14 AALTONEN	12V CDF	$p\bar{p} \rightarrow G \rightarrow ZZ$
	95	15 BAAK	12 RVUE	Electroweak
>1.84	95	16 CHATRCHYAN 12R	CMS	$pp \rightarrow G \rightarrow \gamma\gamma$
>1.63	95	17 AAD	11AD ATLS	$pp \rightarrow G \rightarrow \ell\bar{\ell}$
	95	18 AALTONEN	11G CDF	$p\bar{p} \rightarrow G \rightarrow ZZ$
>1.058	95	19 AALTONEN	11R CDF	$p\bar{p} \rightarrow G \rightarrow e^+e^-, \gamma\gamma$
>0.754	95	20 ABAZOV	11H D0	$p\bar{p} \rightarrow G \rightarrow WW$
>1.079	95	21 CHATRCHYAN 11	CMS	$pp \rightarrow G \rightarrow \ell\bar{\ell}$
>0.607	95	22 AALTONEN	10N CDF	$p\bar{p} \rightarrow G \rightarrow WW$

>1.05	23	ABAZOV	10F	D0	$p\bar{p} \rightarrow G \rightarrow e^+e^-, \gamma\gamma$
	24	AALTONEN	08S	CDF	$p\bar{p} \rightarrow G \rightarrow ZZ$
>0.90	25	ABAZOV	08J	D0	$p\bar{p} \rightarrow G \rightarrow e^+e^-, \gamma\gamma$
	26	AALTONEN	07G	CDF	$p\bar{p} \rightarrow G \rightarrow \gamma\gamma$
>0.889	27	AALTONEN	07H	CDF	$p\bar{p} \rightarrow G \rightarrow e\bar{e}$
>0.785	28	ABAZOV	05N	D0	$p\bar{p} \rightarrow G \rightarrow \ell\ell, \gamma\gamma$
>0.71	29	ABULENCIA	05A	CDF	$p\bar{p} \rightarrow G \rightarrow \ell\bar{\ell}$

¹ KHACHATRYAN 15AE use 20.6 (19.7) fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV in the dimuon (dielectron) channel to place a lower bound on the mass of the lightest KK graviton.

² AAD 15AD use 20.3 fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV in the diphoton channel to place a lower limit on the mass of the lightest KK graviton. See their Table IV for limits with warp parameter values k/\overline{M}_P between 0.01 and 0.1.

³ AAD 15BK use 19.5 fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV to search for Higgs boson pair production in the $b\bar{b}b\bar{b}$ final state, and exclude masses of the lightest KK graviton. See their Table 9 for the excluded mass ranges with warp parameter values $k/\overline{M}_P = 1.0, 1.5, \text{ and } 2.0$.

⁴ KHACHATRYAN 15R use 17.9 fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV to search for Higgs boson pair production in the $b\bar{b}b\bar{b}$ final state, and exclude a KK graviton with mass from 380 to 830 GeV.

⁵ AAD 14V use 20 fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV in the dielectron and dimuon channels to place a lower bound on the mass of the lightest KK graviton.

⁶ KHACHATRYAN 14A use 19.7 fb⁻¹ of data from pp collisions at $\sqrt{s} = 8$ TeV to search for KK gravitons in a warped extra dimension decaying to dibosons. See their Figure 9 for limits on the cross section times branching fraction as a function of the KK graviton mass.

⁷ AAD 13A use 4.7 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV to place a lower bound on the mass of the lightest KK graviton.

⁸ AAD 13AS use 4.9 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV in the diphoton channel to place lower limits on the mass of the lightest KK graviton. The diphoton channel is combined with previous results in the dielectron and dimuon channels to set the best limit. See their Table 2 for warp parameter values k/\overline{M}_P between 0.01 and 0.1.

⁹ CHATRCHYAN 13AF use 5.3 and 4.1 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV and 8 TeV, respectively, in the dielectron and dimuon channels, to place a lower bound on the mass of the lightest KK graviton.

¹⁰ CHATRCHYAN 13U use 5 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV to search for KK gravitons in a warped extra dimension decaying to ZZ dibosons. See their Figure 5 for limits on the lightest KK graviton mass as a function of k/\overline{M}_P .

¹¹ AAD 12AD use 1.02 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV to search for KK gravitons in a warped extra dimension decaying to ZZ dibosons in the $lljj$ and $llll$ channels ($\ell=e, \mu$). The limit is quoted for the combined $lljj + llll$ channels. See their Figure 5 for limits on the cross section $\sigma(G \rightarrow ZZ)$ as a function of the graviton mass.

¹² AAD 12CC use 4.9 and 5.0 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV in the dielectron and dimuon channels, respectively, to place a lower bound on the mass of the lightest KK graviton. See their Figure 5 for limits on the lightest KK graviton mass as a function of k/\overline{M}_P .

¹³ AAD 12Y use 2.12 fb⁻¹ of data from pp collisions at $\sqrt{s} = 7$ TeV in the diphoton channel to place lower limits on the mass of the lightest KK graviton. The diphoton channel is combined with previous results in the dielectron and dimuon channels to set the best limit. See their Table 3 for warp parameter values k/\overline{M}_P between 0.01 and 0.1.

¹⁴ AALTONEN 12V use 6 fb⁻¹ of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV to search for KK gravitons in a warped extra dimension decaying to ZZ dibosons in the $lljj$ and $llll$ channels ($\ell=e, \mu$). It provides improved limits over the previous analysis in

- AALTONEN 11G. See their Figure 16 for limits from all channels combined on the cross section times branching ratio $\sigma(p\bar{p} \rightarrow G^* \rightarrow ZZ)$ as a function of the graviton mass.
- 15 BAAK 12 use electroweak precision observables to place a lower bound on the compactification scale $k e^{-\pi k R}$, assuming Standard Model fields propagate in the bulk and the Higgs is confined to the IR brane. See their Fig. 27 for more details.
 - 16 CHATRCHYAN 12R use 2.2 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 7 \text{ TeV}$ in the diphoton channel to place lower limits on the mass of the lightest KK graviton. See their Table III for warp parameter values k/\overline{M}_P between 0.01 and 0.1.
 - 17 AAD 11AD use 1.08 and 1.21 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 7 \text{ TeV}$ in the dielectron and dimuon channels, respectively, to place a lower bound on the mass of the lightest graviton. For warp parameter values k/\overline{M}_P between 0.01 to 0.1 the lower limit on the mass of the lightest graviton is between 0.71 and 1.63 TeV. See their Table IV for more details.
 - 18 AALTONEN 11G use $2.5\text{--}2.9 \text{ fb}^{-1}$ of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for KK gravitons in a warped extra dimension decaying to ZZ dibosons via the $eeee$, $ee\mu\mu$, $\mu\mu\mu\mu$, $eejj$, and $\mu\mu jj$ channels. See their Fig. 20 for limits on the cross section $\sigma(G \rightarrow ZZ)$ as a function of the graviton mass.
 - 19 AALTONEN 11R uses 5.7 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ in the dielectron channel to place a lower bound on the mass of the lightest graviton. It provides combined limits with the diphoton channel analysis of AALTONEN 11U. For warp parameter values k/\overline{M}_P between 0.01 to 0.1 the lower limit on the mass of the lightest graviton is between 612 and 1058 GeV. See their Table I for more details.
 - 20 ABAZOV 11H use 5.4 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the mass of the lightest graviton. Their 95% C.L. exclusion limit does not include masses less than 300 GeV.
 - 21 CHATRCHYAN 11 use 35 and 40 pb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 7 \text{ TeV}$ in the dielectron and dimuon channels, respectively, to place a lower bound on the mass of the lightest graviton. For a warp parameter value $k/\overline{M}_P = 0.05$, the lower limit on the mass of the lightest graviton is 0.855 TeV.
 - 22 AALTONEN 10N use 2.9 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the mass of the lightest graviton.
 - 23 ABAZOV 10F use 5.4 fb^{-1} of data from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to place a lower bound on the mass of the lightest graviton. For warp parameter values of k/\overline{M}_P between 0.01 and 0.1 the lower limit on the mass of the lightest graviton is between 560 and 1050 GeV. See their Fig. 3 for more details.
 - 24 AALTONEN 08S use $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to four electrons via two Z bosons using 1.1 fb^{-1} of data. See their Fig. 8 for limits on $\sigma \cdot \text{B}(G \rightarrow ZZ)$ versus the graviton mass.
 - 25 ABAZOV 08J use $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to electrons and photons using 1 fb^{-1} of data. For warp parameter values of k/\overline{M}_P between 0.01 and 0.1 the lower limit on the mass of the lightest excitation is between 300 and 900 GeV. See their Fig. 4 for more details.
 - 26 AALTONEN 07G use $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to photons using 1.2 fb^{-1} of data. For warp parameter values of $k/\overline{M}_P = 0.1, 0.05, \text{ and } 0.01$ the bounds on the graviton mass are 850, 694, and 230 GeV, respectively. See their Fig. 3 for more details. See also AALTONEN 07H.
 - 27 AALTONEN 07H use $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$ to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to electrons using 1.3 fb^{-1} of data. For a warp parameter value of $k/\overline{M}_P = 0.1$ the bound on the graviton mass is 807 GeV. See their Fig. 4 for more details. A combined analysis with the diphoton data of AALTONEN 07G yields for $k/\overline{M}_P = 0.1$ a graviton mass lower bound of 889 GeV.

- ²⁸ ABAZOV 05N use $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to muons, electrons or photons, using 260 pb^{-1} of data. For warp parameter values of $k/\overline{M}_P = 0.1, 0.05,$ and $0.01,$ the bounds on the graviton mass are 785, 650 and 250 GeV respectively. See their Fig. 3 for more details.
- ²⁹ ABULENCIA 05A use $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV to search for KK gravitons in warped extra dimensions. They search for graviton resonances decaying to muons or electrons, using 200 pb^{-1} of data. For warp parameter values of $k/\overline{M}_P = 0.1, 0.05,$ and $0.01,$ the bounds on the graviton mass are 710, 510 and 170 GeV respectively.

Limits on Kaluza-Klein Gluons in Warped Extra Dimensions

This section places limits on the mass of the first Kaluza-Klein (KK) excitation of the gluon in warped extra dimension models with Standard Model fields propagating in the bulk. Bounds are given for a specific benchmark model with $\Gamma/m = 15.3\%$ where Γ is the width and m the mass of the KK gluon. See the “Extra Dimensions” review for more discussion.

VALUE (TeV)	CL%	DOCUMENT ID	TECN	COMMENT
>2.5	95	¹ CHATRCHYAN 13BMCMS		$g_{KK} \rightarrow t\bar{t}$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
>2.07	95	² AAD	13AQ ATLS	$g_{KK} \rightarrow t\bar{t} \rightarrow \ell j$
		³ CHEN	13A	$\overline{B} \rightarrow X_S \gamma$
>1.5	95	⁴ AAD	12BV ATLS	$g_{KK} \rightarrow t\bar{t} \rightarrow \ell j$

¹ CHATRCHYAN 13BM use 19.7 fb^{-1} of data from pp collisions at $\sqrt{s} = 8$ TeV. Bound is for a width of approximately 15–20% of the KK gluon mass.

² AAD 13AQ use 4.7 fb^{-1} of data from pp collisions at $\sqrt{s} = 7$ TeV.

³ CHEN 13A place limits on the KK mass scale for a specific warped model with custodial symmetry and bulk fermions. See their Figures 4 and 5.

⁴ AAD 12BV use 2.05 fb^{-1} of data from pp collisions at $\sqrt{s} = 7$ TeV.

REFERENCES FOR Extra Dimensions

AAD	15AD	PR D92 032004	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	15BK	EPJ C75 412	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	15CS	PR D91 012008	G. Aad <i>et al.</i>	(ATLAS Collab.)
Also		PR D92 059903 (errat.)	G. Aad <i>et al.</i>	(ATLAS Collab.)
ACCOMANDO	15	MPL A30 1540010	E. Accomando	(SHMP)
KHACHATRY...	15AE	JHEP 1504 025	V. Khachatryan <i>et al.</i>	(CMS Collab.)
KHACHATRY...	15AL	EPJ C75 235	V. Khachatryan <i>et al.</i>	(CMS Collab.)
KHACHATRY...	15J	PL B746 79	V. Khachatryan <i>et al.</i>	(CMS Collab.)
KHACHATRY...	15R	PL B749 560	V. Khachatryan <i>et al.</i>	(CMS Collab.)
KHACHATRY...	15T	PR D91 092005	V. Khachatryan <i>et al.</i>	(CMS Collab.)
AAD	14BE	EPJ C74 3134	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	14V	PR D90 052005	G. Aad <i>et al.</i>	(ATLAS Collab.)
KHACHATRY...	14A	JHEP 1408 174	V. Khachatryan <i>et al.</i>	(CMS Collab.)
AAD	13A	PL B718 860	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13AD	JHEP 1304 075	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13AQ	PR D88 012004	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13AS	NJP 15 043007	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13C	PRL 110 011802	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13D	JHEP 1301 029	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	13E	PR D87 015010	G. Aad <i>et al.</i>	(ATLAS Collab.)
CHATRCHYAN	13AF	PL B720 63	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	13AQ	PR D87 072005	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	13BM	PRL 111 211804	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
Also		PRL 112 119903 (errat.)	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	13U	JHEP 1302 036	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	13W	JHEP 1303 111	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHEN	13A	CPC 37 063102	J.-B. Chen <i>et al.</i>	(DALI)
EDELHAUSER	13	JHEP 1308 091	L. Edelhauser, T. Flacke, M. Kramer	(AACH, KAIST)

XU	13	JP G40 035107	J. Xu <i>et al.</i>	
AAD	12AD	PL B712 331	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	12BV	JHEP 1209 041	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	12CC	JHEP 1211 138	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	12CP	PL B718 411	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	12X	PL B710 519	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	12Y	PL B710 538	G. Aad <i>et al.</i>	(ATLAS Collab.)
AALTONEN	12V	PR D85 012008	T. Aaltonen <i>et al.</i>	(CDF Collab.)
ABAZOV	12M	PRL 108 131802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
AJELLO	12	JCAP 1202 012	M. Ajello <i>et al.</i>	(Fermi-LAT Collab.)
BAAK	12	EPJ C72 2003	M. Baak <i>et al.</i>	(Gfitter Group)
CHATRCHYAN	12AP	JHEP 1209 094	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	12J	PL B711 15	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	12R	PRL 108 111801	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
FLACKE	12	PR D85 126007	T. Flacke, C. Pasold	(WURZ)
NISHIWAKI	12	PL B707 506	K. Nishiwaki <i>et al.</i>	(KOBE, OSAK)
AAD	11AD	PRL 107 272002	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	11F	PRL 106 121803	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	11S	PL B705 294	G. Aad <i>et al.</i>	(ATLAS Collab.)
AAD	11X	EPJ C71 1744	G. Aad <i>et al.</i>	(ATLAS Collab.)
AALTONEN	11G	PR D83 112008	T. Aaltonen <i>et al.</i>	(CDF Collab.)
AALTONEN	11R	PRL 107 051801	T. Aaltonen <i>et al.</i>	(CDF Collab.)
AALTONEN	11U	PR D83 011102	T. Aaltonen <i>et al.</i>	(CDF Collab.)
AARON	11C	PL B705 52	F. D. Aaron <i>et al.</i>	(H1 Collab.)
ABAZOV	11H	PRL 107 011801	V. M. Abazov <i>et al.</i>	(D0 Collab.)
BEZERRA	11	PR D83 075004	V.B. Bezerra <i>et al.</i>	
CHATRCHYAN	11	JHEP 1105 093	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	11A	JHEP 1105 085	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
CHATRCHYAN	11U	PRL 107 201804	S. Chatrchyan <i>et al.</i>	(CMS Collab.)
SUSHKOV	11	PRL 107 171101	A.O. Sushkov <i>et al.</i>	
AALTONEN	10N	PRL 104 241801	T. Aaltonen <i>et al.</i>	(CDF Collab.)
ABAZOV	10F	PRL 104 241802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABAZOV	10P	PRL 105 221802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
BEZERRA	10	PR D81 055003	V.B. Bezerra <i>et al.</i>	
ABAZOV	09AE	PRL 103 191803	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABAZOV	09D	PRL 102 051601	V.M. Abazov <i>et al.</i>	(D0 Collab.)
MASUDA	09	PRL 102 171101	M. Masuda, M. Sasaki	(ICRR)
AALTONEN	08AC	PRL 101 181602	T. Aaltonen <i>et al.</i>	(CDF Collab.)
AALTONEN	08S	PR D78 012008	T. Aaltonen <i>et al.</i>	(CDF Collab.)
ABAZOV	08J	PRL 100 091802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABAZOV	08S	PRL 101 011601	V.M. Abazov <i>et al.</i>	(D0 Collab.)
DAS	08	PR D78 063011	P.K. Das, V.H.S. Kumar, P.K. Suresh	
GERACI	08	PR D78 022002	A.A. Geraci <i>et al.</i>	(STAN)
TRENKEL	08	PR D77 122001	C. Trenkel	
AALTONEN	07G	PRL 99 171801	T. Aaltonen <i>et al.</i>	(CDF Collab.)
AALTONEN	07H	PRL 99 171802	T. Aaltonen <i>et al.</i>	(CDF Collab.)
DECCA	07A	EPJ C51 963	R.S. Decca <i>et al.</i>	
HAISCH	07	PR D76 034014	U. Haisch, A. Weiler	
KAPNER	07	PRL 98 021101	D.J. Kapner <i>et al.</i>	
SCHAEEL	07A	EPJ C49 411	S. Schaeel <i>et al.</i>	(ALEPH Collab.)
TU	07	PRL 98 201101	L.-C. Tu <i>et al.</i>	
ABDALLAH	06C	EPJ C45 589	J. Abdallah <i>et al.</i>	(DELPHI Collab.)
ABULENCIA,A	06	PRL 97 171802	A. Abulencia <i>et al.</i>	(CDF Collab.)
GERDES	06	PR D73 112008	D. Gerdes <i>et al.</i>	
GOGOLADZE	06	PR D74 093012	I. Gogoladze, C. Macesanu	
ABAZOV	05N	PRL 95 091801	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABAZOV	05V	PRL 95 161602	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABDALLAH	05B	EPJ C38 395	J. Abdallah <i>et al.</i>	(DELPHI Collab.)
ABULENCIA	05A	PRL 95 252001	A. Abulencia <i>et al.</i>	(CDF Collab.)
SMULLIN	05	PR D72 122001	S.J. Smullin <i>et al.</i>	
ACHARD	04E	PL B587 16	P. Achard <i>et al.</i>	(L3 Collab.)
ACOSTA	04C	PRL 92 121802	D. Acosta <i>et al.</i>	(CDF Collab.)
BARBIERI	04	NP B703 127	R. Barbieri <i>et al.</i>	
CASSE	04	PRL 92 111102	M. Casse <i>et al.</i>	
CHEKANOV	04B	PL B591 23	S. Chekanov <i>et al.</i>	(ZEUS Collab.)
HOYLE	04	PR D70 042004	C.D. Hoyle <i>et al.</i>	(WASH)
ABAZOV	03	PRL 90 251802	V.M. Abazov <i>et al.</i>	(D0 Collab.)
ABBIENDI	03D	EPJ C26 331	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ACHARD	03D	PL B572 133	P. Achard <i>et al.</i>	(L3 Collab.)
ADLOFF	03	PL B568 35	C. Adloff <i>et al.</i>	(H1 Collab.)
CHIAVERINI	03	PRL 90 151101	J. Chiaverini <i>et al.</i>	

GIUDICE	03	NP B663 377	G.F. Giudice, A. Strumia	
HANNESTAD	03	PR D67 125008	S. Hannestad, G.G. Raffelt	
Also		PR D69 029901(errat.)	S. Hannestad, G.G. Raffelt	
HEISTER	03C	EPJ C28 1	A. Heister <i>et al.</i>	(ALEPH Collab.)
LONG	03	Nature 421 922	J.C. Long <i>et al.</i>	
ACHARD	02	PL B524 65	P. Achard <i>et al.</i>	(L3 Collab.)
ACHARD	02D	PL B531 28	P. Achard <i>et al.</i>	(L3 Collab.)
HANNESTAD	02	PRL 88 071301	S. Hannestad, G. Raffelt	
ABBOTT	01	PRL 86 1156	B. Abbott <i>et al.</i>	(D0 Collab.)
FAIRBAIRN	01	PL B508 335	M. Fairbairn	
HANHART	01	PL B509 1	C. Hanhart <i>et al.</i>	
HOYLE	01	PRL 86 1418	C.D. Hoyle <i>et al.</i>	
ABBIENDI	00R	EPJ C13 553	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ABREU	00A	PL B491 67	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ABREU	00S	PL B485 45	P. Abreu <i>et al.</i>	(DELPHI Collab.)
ABREU	00Z	EPJ C17 53	P. Abreu <i>et al.</i>	(DELPHI Collab.)
CASSISI	00	PL B481 323	S. Cassisi <i>et al.</i>	
CHANG	00B	PRL 85 3765	L.N. Chang <i>et al.</i>	
CHEUNG	00	PR D61 015005	K. Cheung	
CORNET	00	PR D61 037701	F. Cornet, M. Relano, J. Rico	
GRAESSER	00	PR D61 074019	M.L. Graesser	
HAN	00	PR D62 125018	T. Han, D. Marfatia, R.-J. Zhang	
MATHEWS	00	JHEP 0007 008	P. Mathews, S. Raychaudhuri, K. Sridhar	
MELE	00	PR D61 117901	S. Mele, E. Sanchez	
RIZZO	00	PR D61 016007	T.G. Rizzo, J.D. Wells	
ABBIENDI	99P	PL B465 303	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
ACCIARRI	99M	PL B464 135	M. Acciarri <i>et al.</i>	(L3 Collab.)
ACCIARRI	99R	PL B470 268	M. Acciarri <i>et al.</i>	(L3 Collab.)
ACCIARRI	99S	PL B470 281	M. Acciarri <i>et al.</i>	(L3 Collab.)
BOURILKOV	99	JHEP 9908 006	D. Bourilkov	
HOSKINS	85	PR D32 3084	J.K. Hoskins <i>et al.</i>	
