

## 84. $V_{ud}$ , $V_{us}$ , the Cabibbo Angle, and CKM Unitarity

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The Cabibbo-Kobayashi-Maskawa (CKM) [1,2] three-generation quark mixing matrix written in terms of the Wolfenstein parameters  $(\lambda, A, \rho, \eta)$  [3] nicely illustrates the orthonormality constraint of unitarity and central role played by  $\lambda$ .

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4). \quad (84.1)$$

That cornerstone is a carryover from the two-generation Cabibbo angle,  $\lambda = \sin(\theta_{\text{Cabibbo}}) = V_{us}$ . Its value is a critical ingredient in determinations of the other parameters and in tests of CKM unitarity.

For many years, the precise value of  $\lambda$  was somewhat controversial, with kaon decays suggesting [4]  $\lambda \simeq 0.220$ , while indirect determinations via nuclear  $\beta$ -decays implied a somewhat larger  $\lambda \simeq 0.225 - 0.230$ . This difference resulted in a 2 – 2.5 sigma deviation from the unitarity requirement

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1, \quad (84.2)$$

a potential signal [5] for new physics effects. Below, we discuss the current status of  $V_{ud}$ ,  $V_{us}$ , and their associated unitarity test in Eq. (84.2). (Since  $|V_{ub}|^2 \simeq 1.7 \times 10^{-5}$  is negligibly small, it is ignored in this discussion.) Eq. (84.2) is currently the most stringent test of unitarity in the CKM matrix.

### 84.1. $V_{ud}$

The value of  $V_{ud}$  has been obtained from superallowed nuclear, neutron, and pion decays. Currently, the most precise determination of  $V_{ud}$  comes from a set of superallowed nuclear beta-decays [5] ( $0^+ \rightarrow 0^+$  transitions). Measuring their half-lives,  $t$ , and  $Q$  values that give the decay rate factor,  $f$ , leads to a precise determination of  $V_{ud}$  via the master formula [6–10]

$$|V_{ud}|^2 = \frac{2984.48(5) \text{ sec}}{ft(1 + \Delta)}, \quad (84.3)$$

where  $\Delta$  denotes the entire effect of electroweak radiative corrections (RC), nuclear structure, and isospin violating nuclear effects.  $\Delta$  is nucleus-dependent, ranging from about +3.0% to +3.6% for the best measured superallowed decays. It includes a universal  $\pm 0.04\%$  theoretical uncertainty for all beta decays coming from the radiative corrections.

The most recent analysis of 14 precisely measured superallowed transitions by Hardy and Towner [11] gives a weighted average of

$$V_{ud} = 0.97420(10)_{\text{exp.,nucl.}(18)\text{RC}} \text{ (superallowed)}, \quad (84.4)$$

which, assuming unitarity, corresponds to  $\lambda = 0.2256(9)$ . This recent determination of  $V_{ud}$  has shifted upward slightly compared to the 2016 value of 0.97417(21).

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Combined measurements of the neutron lifetime,  $\tau_n$ , and the ratio of axial-vector/vector couplings,  $g_A \equiv G_A/G_V$ , via neutron decay asymmetries can also be used to determine  $V_{ud}$ :

$$|V_{ud}|^2 = \frac{4908.7(1.9) \text{ sec}}{\tau_n(1 + 3g_A^2)}, \quad (84.5)$$

where the error stems from uncertainties in the electroweak radiative corrections [7,8] due to hadronic loop effects. Using the world averages from the 2016 *Review*, updated with a recent measurement [12] of  $\tau_n = 877.7(7)_{(-1)}^{(+3)}$  sec

$$\begin{aligned} \tau_n^{\text{ave}} &= 879.3(9) \text{ sec} \quad (\times 2.1 \text{ PDG scale factor}) \\ g_A^{\text{ave}} &= 1.2723(23) \quad (\times 2.2 \text{ PDG scale factor}) \end{aligned} \quad (84.6)$$

leads to

$$V_{ud} = 0.9763(5)_{\tau_n(15)} g_A(2)_{\text{RC}}, \quad (84.7)$$

with the error dominated by  $g_A$  uncertainties. We note that the  $g_A$  adopted in Eq. (84.6) leads to a value of  $V_{ud}$  that is somewhat high by 1.3 sigma, but roughly in accord with the superallowed nuclear beta decay result in Eq. (84.4). The value of  $V_{ud}$  in Eq. (84.4) together with the new  $\tau_n^{\text{ave}}$  in Eq. (84.6) suggest, via Eq. (84.5),  $g_A \sim 1.276$ . Future neutron studies [13] are expected to resolve any current inconsistencies and significantly reduce the uncertainties in  $g_A$  and  $\tau_n$ .

The PIBETA experiment at PSI measured the very small ( $\mathcal{O}(10^{-8})$ ) branching ratio for  $\pi^+ \rightarrow \pi^0 e^+ \nu_e$  with about  $\pm 0.5\%$  precision. Their result gives [14]

$$V_{ud} = 0.9749(26) \left[ \frac{BR(\pi^+ \rightarrow e^+ \nu_e(\gamma))}{1.2352 \times 10^{-4}} \right]^{\frac{1}{2}} \quad (84.8)$$

which is normalized using the very precisely determined theoretical prediction for  $BR(\pi^+ \rightarrow e^+ \nu_e(\gamma)) = 1.2352(5) \times 10^{-4}$  [6], rather than the experimental branching ratio from this *Review* of  $1.230(4) \times 10^{-4}$  which would lower the value to  $V_{ud} = 0.9728(30)$ . Theoretical uncertainties in the pion  $\beta$ -decay determination are very small; however, much higher statistics would be required to make this approach competitive with others.

### 84.2. $V_{us}$

$|V_{us}|$  may be determined from kaon decays, hyperon decays, and tau decays. Previous determinations have most often used  $K\ell 3$  decays:

$$\Gamma_{K\ell 3} = \frac{G_F^2 M_K^5}{192\pi^3} S_{EW} (1 + \delta_K^\ell + \delta_{SU2}) C^2 |V_{us}|^2 f_+^\ell(0) I_K^\ell. \quad (84.9)$$

Here,  $\ell$  refers to either  $e$  or  $\mu$ ,  $G_F$  is the Fermi constant,  $M_K$  is the kaon mass,  $S_{EW}$  is the short-distance radiative correction,  $\delta_K^\ell$  is the mode-dependent long-distance radiative correction,  $f_+^\ell(0)$  is the calculated form factor at zero momentum transfer for the  $\ell\nu$  system, and  $I_K^\ell$  is the phase-space integral, which depends on measured semileptonic

form factors. For charged kaon decays,  $\delta_{SU2}$  is the deviation from one of the ratio of  $f_+(0)$  for the charged to neutral kaon decay; it is zero for the neutral kaon.  $C^2$  is 1 (1/2) for neutral (charged) kaon decays. Most early determinations of  $|V_{us}|$  were based solely on  $K \rightarrow \pi e \nu$  decays;  $K \rightarrow \pi \mu \nu$  decays were not used because of large uncertainties in  $I_K^\mu$ . The experimental measurements are the semileptonic decay widths (based on the semileptonic branching fractions and lifetime) and form factors (allowing calculation of the phase space integrals). Theory is needed for  $S_{EW}$ ,  $\delta_K^\ell$ ,  $\delta_{SU2}$ , and  $f_+(0)$ .

Many measurements during the last decade have resulted in a significant shift in  $V_{us}$ . Most importantly, the  $K \rightarrow \pi e \nu$  branching fractions are significantly different than earlier PDG averages, probably as a result of inadequate treatment of radiation in older experiments. This effect was first observed by BNL E865 [15] in the charged kaon system and then by KTeV [16,17] in the neutral kaon system; subsequent measurements were made by KLOE [18–21], NA48 [22–24], and ISTRA+ [25]. Current averages (*e.g.*, by the PDG [26] or Flavianet [27]) of the semileptonic branching fractions are based only on recent, high-statistics experiments where the treatment of radiation is clear. In addition to measurements of branching fractions, new measurements of lifetimes [28] and form factors [29–33], have resulted in improved precision for all of the experimental inputs to  $V_{us}$ . Precise measurements of form factors for  $K_{\mu 3}$  decay make it possible to use both semileptonic decay modes to extract  $V_{us}$ .

Following the analysis of Moulson [34] and the Flavianet group [27], one finds, after including the isospin violating up-down mass difference effect,  $\delta_{SU2}$ , the values of  $|V_{us}|f_+(0)$  in Table 84.1. The average of these measurements, including correlation effects [34], gives

$$f_+(0)|V_{us}| = 0.2165(4). \quad (84.10)$$

Lattice QCD calculations of  $f_+(0)$  have been carried out for 2, 2+1, and 2+1+1 quark flavors and range from about 0.96 to 0.97. Here, we use recent FLAG averages [35] for 2+1 and 2+1+1 flavors:

$$\begin{aligned} f_+(0) &= 0.9677(27) \quad N_f = 2 + 1 \\ f_+(0) &= 0.9704(32) \quad N_f = 2 + 1 + 1 \end{aligned} \quad (84.11)$$

One finds from Eq. (84.10) and Eq. (84.11),

$$\begin{aligned} |V_{us}| &= 0.2238(4)_{\text{exp+RC}}(6)_{\text{lattice}} \quad (N_f = 2 + 1, K_{\ell 3} \text{ decays}) \\ &= 0.2231(4)_{\text{exp+RC}}(7)_{\text{lattice}} \quad (N_f = 2 + 1 + 1, K_{\ell 3} \text{ decays}) \end{aligned} \quad (84.12)$$

A value of  $V_{us}$  can also be obtained from a comparison of the radiative inclusive decay rates for  $K \rightarrow \mu \nu(\gamma)$  and  $\pi \rightarrow \mu \nu(\gamma)$  combined with a lattice gauge theory calculation of  $f_{K^+}/f_{\pi^+}$  via

$$\frac{|V_{us}|f_{K^+}}{|V_{ud}|f_{\pi^+}} = 0.23871(20) \left[ \frac{\Gamma(K \rightarrow \mu \nu(\gamma))}{\Gamma(\pi \rightarrow \mu \nu(\gamma))} \right]^{\frac{1}{2}} \quad (84.13)$$

**Table 84.1:**  $|V_{us}|f_+(0)$  from  $K_{\ell 3}$ .

| Decay Mode                                   | $ V_{us} f_+(0)$    |
|----------------------------------------------|---------------------|
| $K^\pm e 3$                                  | $0.2171 \pm 0.0008$ |
| $K^\pm \mu 3$                                | $0.2170 \pm 0.0011$ |
| $K_L e 3$                                    | $0.2163 \pm 0.0006$ |
| $K_L \mu 3$                                  | $0.2166 \pm 0.0006$ |
| $K_S e 3$                                    | $0.2155 \pm 0.0013$ |
| Average (including correlation effects [34]) | $0.2165 \pm 0.0004$ |

with the small error coming from electroweak radiative corrections and isospin breaking effects [36]. Employing

$$\frac{\Gamma(K \rightarrow \mu\nu(\gamma))}{\Gamma(\pi \rightarrow \mu\nu(\gamma))} = 1.3367(29), \quad (84.14)$$

which includes  $\Gamma(K \rightarrow \mu\nu(\gamma)) = 5.134(11) \times 10^7 s^{-1}$  [34,37], leads to

$$\frac{|V_{us}|f_{K^+}}{|V_{ud}|f_{\pi^+}} = 0.2760(4). \quad (84.15)$$

Employing the FLAG [35] lattice QCD averages,

$$\begin{aligned} \frac{f_{K^+}}{f_{\pi^+}} &= 1.192(5) \quad N_f = 2 + 1 \\ &= 1.1933(29) \quad N_f = 2 + 1 + 1. \end{aligned} \quad (84.16)$$

along with the value of  $|V_{ud}|$  in Eq. (84.4) leads to

$$\begin{aligned} |V_{us}| &= 0.2256(10) \quad (N_f = 2 + 1, K_{\mu 2} \text{ decays}) \\ &= 0.2253(7) \quad (N_f = 2 + 1 + 1, K_{\mu 2} \text{ decays}) \end{aligned} \quad (84.17)$$

Together, weighted averages of the  $K_{\ell 3}$  (Eq. (84.12)) and  $K_{\mu 2}$  (Eq. (84.17)) values give similar results for  $N_f = 2 + 1$  and  $2 + 1 + 1$  flavors:

$$\begin{aligned} |V_{us}| &= 0.2244(6) \quad N_f = 2 + 1 \\ |V_{us}| &= 0.2243(5) \quad N_f = 2 + 1 + 1. \end{aligned} \quad (84.18)$$

Note that the differences between  $K_{\ell 3}$  and  $K_{\mu 2}$  values for  $V_{us}$  differ by 1.5 and 2 sigma, respectively, for  $N_f = 2 + 1$  and  $2 + 1 + 1$  flavors. One might, therefore, scale the uncertainties in Eq. (84.18) accordingly.

It should be mentioned that hyperon decay fits suggest [38]

$$|V_{us}| = 0.2250(27) \text{ (Hyperon Decays)} \quad (84.19)$$

modulo SU(3) breaking effects that could shift that value up or down. We note that a representative effort [39] that incorporates SU(3) breaking found  $V_{us} = 0.226(5)$ . Strangeness changing tau decays, averaging both inclusive and exclusive measurements, give [40]

$$|V_{us}| = 0.2202(15) \text{ (Tau Decays)} , \quad (84.20)$$

which differs by about 3 sigma from the kaon determination discussed above, and would, if combined with  $V_{ud}$  from super-allowed beta decays, lead to a 3 sigma deviation from unitarity. This discrepancy results mainly from the inclusive tau decay results that rely on Finite Energy Sum Rule techniques and assumptions, as well as experimental uncertainties. Recent investigation of that approach suggests a larger value for  $V_{us}$ , which is more in accord with other determinations [41].

Employing the values of  $V_{ud}$  and  $V_{us}$  from Eq. (84.4) and Eq. (84.18), respectively, leads to the unitarity consistency check

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994(4)(2). \quad (84.21)$$

where the first error is the uncertainty from  $|V_{ud}|^2$  and the second error is the uncertainty from  $|V_{us}|^2$  for  $N_f = 2 + 1 + 1$ . For  $N_f = 2 + 1$ , the sum of the squares remains the same, but the  $V_{us}$  error increases to (3). If scale factors are included, both  $|V_{us}|^2$  uncertainties roughly increase to (4).

### 84.3. CKM Unitarity Constraints

The current good experimental agreement with unitarity,  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994(5)$ , provides strong confirmation of Standard Model radiative corrections (which range between 3-4% depending on the nucleus used) at better than the 50 sigma level [42]. In addition, it implies constraints on “New Physics” effects at both the tree and quantum loop levels. Those effects could be in the form of contributions to nuclear beta decays,  $K$  decays and/or muon decays, with the last of these providing normalization via the muon lifetime [43], which is used to obtain the Fermi constant,  $G_\mu = 1.1663787(6) \times 10^{-5} \text{GeV}^{-2}$ .

In the following sections, we illustrate the implications of CKM unitarity for (1) exotic muon decays [44] (beyond ordinary muon decay  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ ) and (2) new heavy quark mixing  $V_{uD}$  [45]. Other examples in the literature [46,47] include  $Z_\chi$  boson quantum loop effects, supersymmetry, leptoquarks, compositeness etc.

#### Exotic Muon Decays

If additional lepton flavor violating decays such as  $\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_\mu$  (wrong neutrinos) occur, they would cause confusion in searches for neutrino oscillations at, for example, muon storage rings/neutrino factories or other neutrino sources from muon decays.

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Calling the rate for all such decays  $\Gamma(\text{exotic } \mu \text{ decays})$ , they should be subtracted before the extraction of  $G_\mu$  and normalization of the CKM matrix. Since that is not done and unitarity works, one has (at one-sided 95% CL)

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - BR(\text{exotic } \mu \text{ decays}) \geq 0.9986 \quad (84.22)$$

or

$$BR(\text{exotic } \mu \text{ decays}) \leq 0.0014 . \quad (84.23)$$

This bound is a factor of 10 better than the direct experimental bound on  $\mu^+ \rightarrow e^+ \bar{\nu}_e \nu_\mu$ .

### New Heavy Quark Mixing

Heavy  $D$  quarks naturally occur in fourth quark generation models and some heavy quark “new physics” scenarios such as  $E_6$  grand unification. Their mixing with ordinary quarks gives rise to  $V_{uD}$ , which is constrained by unitarity (one sided 95% CL)

$$\begin{aligned} |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 &= 1 - |V_{uD}|^2 \geq 0.9986 \\ |V_{uD}| &\leq 0.04 . \end{aligned} \quad (84.24)$$

A similar constraint applies to heavy neutrino mixing and the couplings  $V_{\mu N}$  and  $V_{eN}$ .

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