

# Light Quarks ( $u, d, s$ )

OMITTED FROM SUMMARY TABLE

See the related review(s):

[Quark Masses](#)

NODE=Q123

## $u$ -QUARK MASS

NODE=Q123UM

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The  $u$ -,  $d$ -, and  $s$ -quark masses are estimates of so-called “current-quark masses,” in a mass- independent subtraction scheme such as  $\overline{\text{MS}}$ . The ratios  $m_u/m_d$  and  $m_s/m_d$  are extracted from pion and kaon masses using chiral symmetry. The estimates of  $d$  and  $u$  masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the  $u$  quark could be essentially massless. The  $s$ -quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of “Our Evaluation” were determined in part via Figures 2 and 3 in the “Quark masses” review.

$\overline{\text{MS}}$ MASS (MeV)	CL%	DOCUMENT ID	TECN
<b>2.16 <math>\pm 0.07</math> (CL = 90%) OUR EVALUATION</b>		See the ideogram below.	

NODE=Q123UM

→ UNCHECKED ←

OCCUR=2

2.6 $\pm 0.4$	<sup>1</sup> DOMINGUEZ 19	THEO
2.130 $\pm 0.041$	<sup>2</sup> BAZAVOV 18	LATT
2.27 $\pm 0.06 \pm 0.06$	<sup>3</sup> FODOR 16	LATT
2.36 $\pm 0.24$	<sup>4</sup> CARRASCO 14	LATT
2.24 $\pm 0.10 \pm 0.34$	<sup>5</sup> BLUM 10	LATT
2.01 $\pm 0.14$	<sup>6</sup> MCNEILE 10	LATT
• • • We do not use the following data for averages, fits, limits, etc. • • •		
2.57 $\pm 0.26 \pm 0.07$	<sup>7</sup> AOKI 12	LATT
2.15 $\pm 0.03 \pm 0.10$	<sup>8</sup> DURR 11	LATT
1.9 $\pm 0.2$	<sup>9</sup> BAZAVOV 10	LATT
2.01 $\pm 0.14$	<sup>6</sup> DAVIES 10	LATT
2.9 $\pm 0.2$	<sup>10</sup> DOMINGUEZ 09	THEO
2.9 $\pm 0.8$	<sup>11</sup> DEANDREA 08	THEO
3.02 $\pm 0.33$	<sup>12</sup> BLUM 07	LATT
2.7 $\pm 0.4$	<sup>13</sup> JAMIN 06	THEO
1.9 $\pm 0.2$	<sup>14</sup> MASON 06	LATT
2.8 $\pm 0.2$	<sup>15</sup> NARISON 06	THEO
1.7 $\pm 0.3$	<sup>16</sup> AUBIN 04A	LATT

<sup>1</sup> DOMINGUEZ 19 determine the quark mass from a QCD finite energy sum rule for the divergence of the axial current.

NODE=Q123UM;LINKAGE=L

<sup>2</sup> BAZAVOV 18 determine the quark masses using a lattice computation with staggered fermions and four active quark flavors.

NODE=Q123UM;LINKAGE=K

<sup>3</sup> FODOR 16 is a lattice simulation with  $n_f = 2 + 1$  dynamical flavors and includes partially quenched QED effects.

NODE=Q123UM;LINKAGE=I

<sup>4</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using  $2 + 1 + 1$  dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.

NODE=Q123UM;LINKAGE=C

<sup>5</sup> BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use  $2+1$  dynamical quark flavors.

NODE=Q123UM;LINKAGE=BU

<sup>6</sup> DAVIES 10 and MCNEILE 10 determine  $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with  $n_f = 2 + 1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_u$  is obtained from this using the value of  $m_c$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios,  $m_s/\overline{m}$  and  $m_u/m_d$ .

NODE=Q123UM;LINKAGE=DA

<sup>7</sup> AOKI 12 is a lattice computation using  $1 + 1 + 1$  dynamical quark flavors.

NODE=Q123UM;LINKAGE=H

<sup>8</sup> DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $n_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual  $m_u$ ,  $m_d$  values are obtained using the lattice determination of the average mass  $m_{ud}$  and of the ratio  $m_s/m_{ud}$  and the value of  $Q = (m_s^2 - m_{ud}^2) / (m_d^2 - m_u^2)$  as determined from  $\eta \rightarrow 3\pi$  decays.

NODE=Q123UM;LINKAGE=DU

<sup>9</sup> BAZAVOV 10 is a lattice computation using  $2+1$  dynamical quark flavors.

NODE=Q123UM;LINKAGE=F

<sup>10</sup> DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .

NODE=Q123UM;LINKAGE=DM

- 11 DEANDREA 08 determine  $m_u - m_d$  from  $\eta \rightarrow 3\pi^0$ , and combine with the PDG 06 lattice average value of  $m_u + m_d = 7.6 \pm 1.6$  to determine  $m_u$  and  $m_d$ .
- 12 BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- 13 JAMIN 06 determine  $m_u(2 \text{ GeV})$  by combining the value of  $m_s$  obtained from the spectral function for the scalar  $K\pi$  form factor with other determinations of the quark mass ratios.
- 14 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order. The quark masses  $m_u$  and  $m_d$  were determined from their  $(m_u + m_d)/2$  measurement and AUBIN 04A  $m_u/m_d$  value.
- 15 NARISON 06 uses sum rules for  $e^+e^- \rightarrow \text{hadrons}$  to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- 16 AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.

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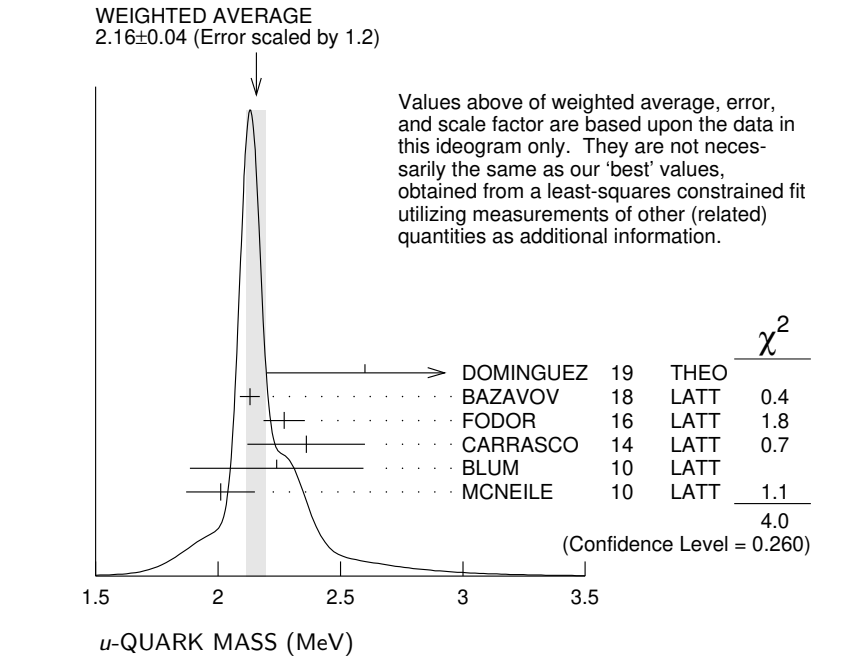
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**d-QUARK MASS**

NODE=Q123DM

See the comment for the  $u$  quark above.

NODE=Q123DM

We have normalized the  $\overline{M_S}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 2 and 3 in the "Quark masses" review.

NODE=Q123DM

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$\overline{M_S}$ MASS (MeV)	CL%	DOCUMENT ID	TECN
<b>4.70 ±0.07 (CL = 90%) OUR EVALUATION</b>		See the ideogram below.	
5.3 ±0.4		1 DOMINGUEZ	19 THEO
4.675±0.056		2 BAZAVOV	18 LATT
4.67 ±0.06 ±0.06		3 FODOR	16 LATT
5.03 ±0.26		4 CARRASCO	14 LATT
4.65 ±0.15 ±0.32		5 BLUM	10 LATT
4.77 ±0.15		6 MCNEILE	10 LATT
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
3.68 ±0.29 ±0.10		7 AOKI	12 LATT
4.79 ±0.07 ±0.12		8 DURR	11 LATT
4.6 ±0.3		9 BAZAVOV	10 LATT
4.79 ±0.16		6 DAVIES	10 LATT
5.3 ±0.4		10 DOMINGUEZ	09 THEO
4.7 ±0.8		11 DEANDREA	08 THEO
5.49 ±0.39		12 BLUM	07 LATT
4.8 ±0.5		13 JAMIN	06 THEO
4.4 ±0.3		14 MASON	06 LATT
5.1 ±0.4		15 NARISON	06 THEO
3.9 ±0.5		16 AUBIN	04A LATT

- <sup>1</sup> DOMINGUEZ 19 determine the quark mass from a QCD finite energy sum rule for the divergence of the axial current.
- <sup>2</sup> BAZAVOV 18 determine the quark masses using a lattice computation with staggered fermions and four active quark flavors.
- <sup>3</sup> FODOR 16 is a lattice simulation with  $n_f = 2 + 1$  dynamical flavors and includes partially quenched QED effects.
- <sup>4</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using  $2 + 1 + 1$  dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.
- <sup>5</sup> BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use  $2+1$  dynamical quark flavors.
- <sup>6</sup> DAVIES 10 and MCNEILE 10 determine  $\bar{m}_c(\mu)/\bar{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with  $n_f = 2 + 1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_d$  is obtained from this using the value of  $m_c$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratios,  $m_s/\bar{m}$  and  $m_u/m_d$ .
- <sup>7</sup> AOKI 12 is a lattice computation using  $1 + 1 + 1$  dynamical quark flavors.
- <sup>8</sup> DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $n_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed. The individual  $m_u$ ,  $m_d$  values are obtained using the lattice determination of the average mass  $m_{ud}$  and of the ratio  $m_s/m_{ud}$  and the value of  $Q = (m_s^2 - m_{ud}^2) / (m_d^2 - m_u^2)$  as determined from  $\eta \rightarrow 3\pi$  decays.
- <sup>9</sup> BAZAVOV 10 is a lattice computation using  $2+1$  dynamical quark flavors.
- <sup>10</sup> DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .
- <sup>11</sup> DEANDREA 08 determine  $m_u - m_d$  from  $\eta \rightarrow 3\pi^0$ , and combine with the PDG 06 lattice average value of  $m_u + m_d = 7.6 \pm 1.6$  to determine  $m_u$  and  $m_d$ .
- <sup>12</sup> BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- <sup>13</sup> JAMIN 06 determine  $m_d(2 \text{ GeV})$  by combining the value of  $m_s$  obtained from the spectral function for the scalar  $K\pi$  form factor with other determinations of the quark mass ratios.
- <sup>14</sup> MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order. The quark masses  $m_u$  and  $m_d$  were determined from their  $(m_u + m_d)/2$  measurement and AUBIN 04A  $m_u/m_d$  value.
- <sup>15</sup> NARISON 06 uses sum rules for  $e^+ e^- \rightarrow \text{hadrons}$  to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- <sup>16</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.

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NODE=Q123DM;LINKAGE=DE

NODE=Q123DM;LINKAGE=BL

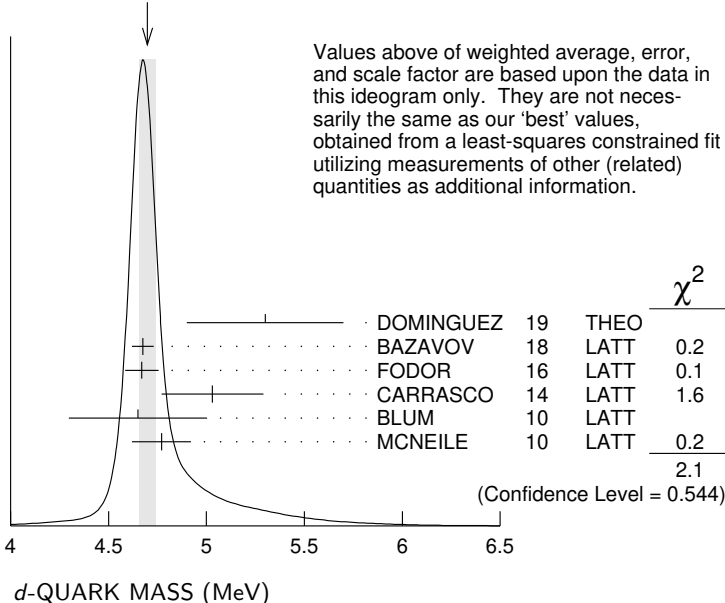
NODE=Q123DM;LINKAGE=JM

NODE=Q123DM;LINKAGE=MA

NODE=Q123DM;LINKAGE=NA

NODE=Q123DM;LINKAGE=AU

WEIGHTED AVERAGE  
4.70±0.04 (Error scaled by 1.0)



$$\bar{m} = (m_u + m_d)/2$$

NODE=Q123MR4

See the comments for the  $u$  quark above.

NODE=Q123MR4

We have normalized the  $\overline{M_S}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 2 and 3 in the "Quark masses" review.

$\overline{M_S}$ MASS (MeV)	CL%	DOCUMENT ID	TECN
<b>3.49 <math>\pm</math> 0.07 (CL = 90%) OUR EVALUATION</b>		See the ideogram below.	

NODE=Q123MR4

→ UNCHECKED ←

3.636 $\pm$ 0.066 <sup>+0.060</sup> <sub>-0.057</sub>	1	ALEXANDROU21	LATT
3.54 $\pm$ 0.12 $\pm$ 0.09	2	BRUNO	20 LATT
3.9 $\pm$ 0.3	3	DOMINGUEZ	19 THEO
4.7 <sup>+0.8</sup> <sub>-0.7</sub>	4	YUAN	17 THEO
3.70 $\pm$ 0.17	5	CARRASCO	14 LATT
3.45 $\pm$ 0.12	6	ARTHUR	13 LATT
3.469 $\pm$ 0.047 $\pm$ 0.048	7	DURR	11 LATT
3.6 $\pm$ 0.2	8	BLOSSIER	10 LATT
3.39 $\pm$ 0.06	9	MCNEILE	10 LATT
• • • We do not use the following data for averages, fits, limits, etc. • • •			
3.59 $\pm$ 0.21	10	AOKI	11A LATT
3.40 $\pm$ 0.07	9	DAVIES	10 LATT
4.1 $\pm$ 0.2	11	DOMINGUEZ	09 THEO
3.72 $\pm$ 0.41	12	ALLTON	08 LATT
3.85 $\pm$ 0.12 $\pm$ 0.4	13	BLOSSIER	08 LATT
$\geq$ 4.85 $\pm$ 0.20	14	DOMINGUEZ...	08B THEO
3.55 <sup>+0.65</sup> <sub>-0.28</sub>	15	ISHIKAWA	08 LATT
4.026 $\pm$ 0.048	16	NAKAMURA	08 LATT
4.25 $\pm$ 0.35	17	BLUM	07 LATT
4.08 $\pm$ 0.25 $\pm$ 0.42	18	GOCKELER	06 LATT
4.7 $\pm$ 0.2 $\pm$ 0.3	19	GOCKELER	06A LATT
3.2 $\pm$ 0.3	20	MASON	06 LATT
3.95 $\pm$ 0.3	21	NARISON	06 THEO
2.8 $\pm$ 0.3	22	AUBIN	04 LATT
4.29 $\pm$ 0.14 $\pm$ 0.65	23	AOKI	03 LATT
3.223 $\pm$ 0.3	24	AOKI	03B LATT
4.4 $\pm$ 0.1 $\pm$ 0.4	25	BECIREVIC	03 LATT
4.1 $\pm$ 0.3 $\pm$ 1.0	26	CHIU	03 LATT

<sup>1</sup> ALEXANDROU 21 determines the quark mass using a lattice calculation of the meson and baryon masses with a twisted mass fermion action. The simulations are carried out using 2+1+1 dynamical quarks with  $m_u = m_d \neq m_s \neq m_c$ , including gauge ensembles close to the physical pion point.

NODE=Q123MR4;LINKAGE=J

<sup>2</sup> BRUNO 20 determines the light quark mass using a lattice calculation with  $n_f = 2+1$  flavors of Wilson fermions. The scale has been set from  $f_\pi$  and  $f_K$ . The tuning was done using the masses of the lightest ( $\pi$ ) and strange ( $K$ ) pseudoscalar mesons.

NODE=Q123MR4;LINKAGE=K

<sup>3</sup> DOMINGUEZ 19 determine the quark mass from a QCD finite energy sum rule for the divergence of the axial current.

NODE=Q123MR4;LINKAGE=H

<sup>4</sup> YUAN 17 determine  $\overline{m}$  using QCD sum rules in the isospin  $I=0$  scalar channel. At the end of the "Numerical Results" section of YUAN 17 the authors discuss the significance of their larger value of the light quark mass compared to previous determinations.

NODE=Q123MR4;LINKAGE=G

<sup>5</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using 2 + 1 + 1 dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.

NODE=Q123MR4;LINKAGE=E

<sup>6</sup> ARTHUR 13 is a lattice computation using 2+1 dynamical domain wall fermions. Masses at  $\mu = 3$  GeV have been converted to  $\mu = 2$  GeV using conversion factors given in their paper.

NODE=Q123MR4;LINKAGE=F

<sup>7</sup> DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $n_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

NODE=Q123MR4;LINKAGE=DU

<sup>8</sup> BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using  $n_f=2$  dynamical twisted-mass Wilson fermions.

NODE=Q123MR4;LINKAGE=BS

<sup>9</sup> DAVIES 10 and MCNEILE 10 determine  $\overline{m}_c(\mu)/\overline{m}_s(\mu) = 11.85 \pm 0.16$  using a lattice computation with  $n_f = 2 + 1$  dynamical fermions of the pseudoscalar meson masses. Mass  $\overline{m}$  is obtained from this using the value of  $m_c$  from ALLISON 08 or MCNEILE 10 and the BAZAVOV 10 values for the light quark mass ratio,  $m_s/\overline{m}$ .

NODE=Q123MR4;LINKAGE=DA

<sup>10</sup> AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using  $n_f = 2 + 1$  dynamical flavors of domain wall fermions.

NODE=Q123MR4;LINKAGE=OK

<sup>11</sup> DOMINGUEZ 09 use QCD finite energy sum rules for the two-point function of the divergence of the axial vector current computed to order  $\alpha_s^4$ .

NODE=Q123MR4;LINKAGE=DM

- 12 ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- 13 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- 14 DOMINGUEZ-CLARIMON 08B obtain an inequality from sum rules for the scalar two-point correlator.
- 15 ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization.
- 16 NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization.
- 17 BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.
- 18 GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $n_f = 2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\bar{m}(2 \text{ GeV}) = 4.08 \pm 0.25 \pm 0.19 \pm 0.23 \text{ MeV}$ , where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly.
- 19 GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $n_f = 2$  dynamical light quark flavors, and non-perturbative renormalization.
- 20 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order.
- 21 NARISON 06 uses sum rules for  $e^+e^- \rightarrow \text{hadrons}$  to order  $\alpha_s^3$  to determine  $m_s$  combined with other determinations of the quark mass ratios.
- 22 AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- 23 AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.
- 24 The errors given in AOKI 03B were  $^{+0.046}_{-0.069}$ . We changed them to  $\pm 0.3$  for calculating the overall best values. AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- 25 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization.
- 26 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.

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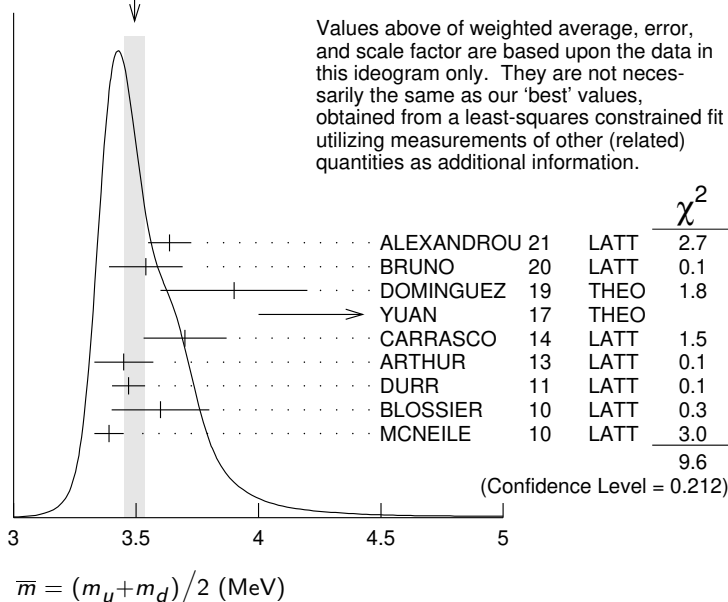
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NODE=Q123MR4;LINKAGE=BE

NODE=Q123MR4;LINKAGE=CH

WEIGHTED AVERAGE  
3.49±0.04 (Error scaled by 1.2)



### $m_u/m_d$ MASS RATIO

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<b>0.462 ± 0.020</b>	<b>(CL = 90%)</b>	<b>OUR EVALUATION</b>		See the ideogram below.
0.485 ± 0.011 ± 0.016		<sup>1</sup> FODOR	16 LATT	
0.4482 <sup>+0.0173</sup> <sub>-0.0206</sub>		<sup>2</sup> BASAK	15 LATT	
0.470 ± 0.056		<sup>3</sup> CARRASCO	14 LATT	
0.42 ± 0.01 ± 0.04		<sup>4</sup> BAZAVOV	10 LATT	
0.4818 ± 0.0096 ± 0.0860		<sup>5</sup> BLUM	10 LATT	

NODE=Q123MR0

NODE=Q123MR0

→ UNCHECKED ←

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.698 ± 0.051	<sup>6</sup> AOKI	12	LATT
0.550 ± 0.031	<sup>7</sup> BLUM	07	LATT
0.43 ± 0.08	<sup>8</sup> AUBIN	04A	LATT
0.410 ± 0.036	<sup>9</sup> NELSON	03	LATT
0.553 ± 0.043	<sup>10</sup> LEUTWYLER	96	THEO Compilation

<sup>1</sup> FODOR 16 is a lattice simulation with  $n_f = 2 + 1$  dynamical flavors and includes partially quenched QED effects.

<sup>2</sup> BASAK 15 is a lattice computation using 2+1 dynamical quark flavors.

<sup>3</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using  $2 + 1 + 1$  dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.

<sup>4</sup> BAZAVOV 10 is a lattice computation using 2+1 dynamical quark flavors.

<sup>5</sup> BLUM 10 is a lattice computation using 2+1 dynamical quark flavors.

<sup>6</sup> AOKI 12 is a lattice computation using  $1 + 1 + 1$  dynamical quark flavors.

<sup>7</sup> BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors.

<sup>8</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.

<sup>9</sup> NELSON 03 computes coefficients in the order  $p^4$  chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio  $m_u/m_d$  is obtained by combining this with the chiral perturbation theory computation of the meson masses to order  $p^4$ .

<sup>10</sup> LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi (\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .

NODE=Q123MR0;LINKAGE=S

NODE=Q123MR0;LINKAGE=O  
NODE=Q123MR0;LINKAGE=K

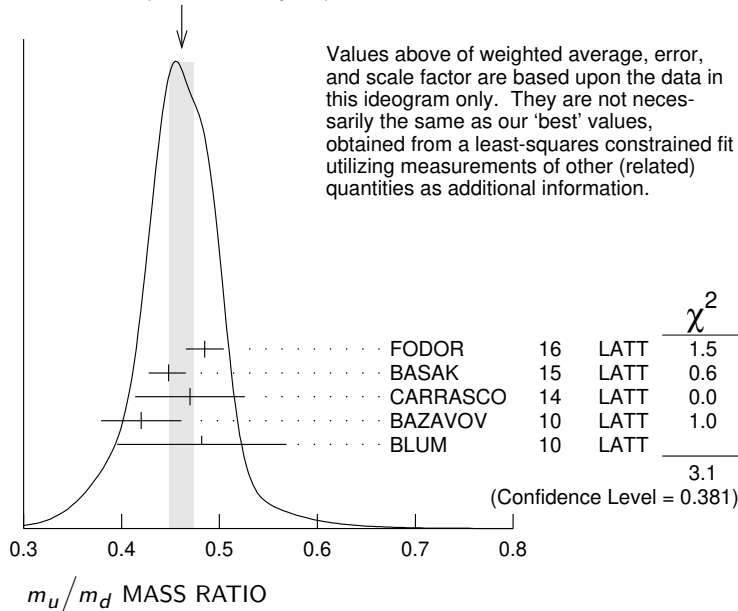
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NODE=Q123MR0;LINKAGE=Q  
NODE=Q123MR0;LINKAGE=BL

NODE=Q123MR0;LINKAGE=AU

NODE=Q123MR0;LINKAGE=N

NODE=Q123MR0;LINKAGE=M

WEIGHTED AVERAGE  
0.462±0.013 (Error scaled by 1.0)



## s-QUARK MASS

NODE=Q123SM

See the comment for the  $u$  quark above.

NODE=Q123SM

We have normalized the  $\overline{MS}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35.

$\overline{MS}$ MASS (MeV)	CL%	DOCUMENT ID	TECN
<b>93.5 ± 0.8 (CL = 90%) OUR EVALUATION</b>		See the ideogram below.	
98.7 ± 2.4 $\begin{smallmatrix} + 4.0 \\ - 3.2 \end{smallmatrix}$		<sup>1</sup> ALEXANDROU21	LATT
95.7 ± 2.5 ± 2.4		<sup>2</sup> BRUNO	20 LATT
92.47 ± 0.69		<sup>3</sup> BAZAVOV	18 LATT
93.85 ± 0.75		<sup>4</sup> LYTLE	18 LATT
87.6 ± 6.0		<sup>5</sup> ANANTHANA..	16 THEO
99.6 ± 4.3		<sup>6</sup> CARRASCO	14 LATT
94.4 ± 2.3		<sup>7</sup> ARTHUR	13 LATT
94 ± 9		<sup>8</sup> BODENSTEIN	13 THEO
95.5 ± 1.1 ± 1.5		<sup>9</sup> DURR	11 LATT

NODE=Q123SM

→ UNCHECKED ←

• • • We do not use the following data for averages, fits, limits, etc. • • •

93.6 ± 0.8	10	CHAKRABORTY	15	LATT
102 ± 3 ± 1	11	FRITZSCH	12	LATT
96.2 ± 2.7	12	AOKI	11A	LATT
95 ± 6	13	BLOSSIER	10	LATT
97.6 ± 2.9 ± 5.5	14	BLUM	10	LATT
92.4 ± 1.5	15	DAVIES	10	LATT
92.2 ± 1.3	15	MCNEILE	10	LATT
107.3 ± 11.7	16	ALLTON	08	LATT
105 ± 3 ± 9	17	BLOSSIER	08	LATT
102 ± 8	18	DOMINGUEZ	08A	THEO
90.1 +17.2 - 6.1	19	ISHIKAWA	08	LATT
105.6 ± 1.2	20	NAKAMURA	08	LATT
119.5 ± 9.3	21	BLUM	07	LATT
105 ± 6 ± 7	22	CHETYRKIN	06	THEO
111 ± 6 ± 10	23	GOCKELER	06	LATT
119 ± 5 ± 8	24	GOCKELER	06A	LATT
92 ± 9	25	JAMIN	06	THEO
87 ± 6	26	MASON	06	LATT
104 ± 15	27	NARISON	06	THEO
≥ 71 ± 4, ≤ 151 ± 14	28	NARISON	06	THEO
96 + 5 +16 - 3 -18	29	BAIKOV	05	THEO
81 ± 22	30	GAMIZ	05	THEO
125 ± 28	31	GORBUNOV	05	THEO
93 ± 32	32	NARISON	05	THEO
76 ± 8	33	AUBIN	04	LATT
116 ± 6 ± 0.65	34	AOKI	03	LATT
84.5 +12 - 1.7	35	AOKI	03B	LATT
106 ± 2 ± 8	36	BECIREVIC	03	LATT
92 ± 9 ± 16	37	CHIU	03	LATT
117 ± 17	38	GAMIZ	03	THEO
103 ± 17	39	GAMIZ	03	THEO

OCCUR=2

OCCUR=2

NODE=Q123SM;LINKAGE=CA

NODE=Q123SM;LINKAGE=EA

NODE=Q123SM;LINKAGE=Z

NODE=Q123SM;LINKAGE=AA

NODE=Q123SM;LINKAGE=Y

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NODE=Q123SM;LINKAGE=W

NODE=Q123SM;LINKAGE=FR

NODE=Q123SM;LINKAGE=OK

NODE=Q123SM;LINKAGE=BS

NODE=Q123SM;LINKAGE=BU

<sup>1</sup> ALEXANDROU 21 determines the quark mass using a lattice calculation of the meson and baryon masses with a twisted mass fermion action. The simulations are carried out using 2+1+1 dynamical quarks with  $m_u = m_d \neq m_s \neq m_c$ , including gauge ensembles close to the physical pion point.

<sup>2</sup> BRUNO 20 determines the light quark mass using a lattice calculation with  $n_f = 2+1$  flavors of Wilson fermions. The scale has been set from  $f_\pi$  and  $f_K$ . The tuning was done using the masses of the lightest ( $\pi$ ) and strange ( $K$ ) pseudoscalar mesons.

<sup>3</sup> BAZAVOV 18 determine the quark masses using a lattice computation with staggered fermions and four active quark flavors.

<sup>4</sup> LYTLE 18 combined with CHAKRABORTY 2015 determine  $\bar{m}_s(3 \text{ GeV}) = 84.78 \pm 0.65 \text{ MeV}$  from a lattice simulation with  $n_f = 2+1+1$  flavors. They also determine the quoted value  $\bar{m}_s(2 \text{ GeV})$  for  $n_f = 4$  dynamical flavors.

<sup>5</sup> ANANTHANARAYAN 16 determine  $\bar{m}_s(2 \text{ GeV}) = 106.70 \pm 9.36 \text{ MeV}$  and  $74.47 \pm 7.77 \text{ MeV}$  from fits to ALEPH and OPAL  $\tau$  decay data, respectively. We have used the weighted average of the two.

<sup>6</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using 2 + 1 + 1 dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.

<sup>7</sup> ARTHUR 13 is a lattice computation using 2+1 dynamical domain wall fermions. Masses at  $\mu = 3 \text{ GeV}$  have been converted to  $\mu = 2 \text{ GeV}$  using conversion factors given in their paper.

<sup>8</sup> BODENSTEIN 13 determines  $m_s$  from QCD finite energy sum rules, and the perturbative computation of the pseudoscalar correlator to five-loop order.

<sup>9</sup> DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $n_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.

<sup>10</sup> CHAKRABORTY 15 is a lattice QCD computation that determines  $m_c$  and  $m_c/m_s$  using pseudoscalar mesons masses tuned on gluon field configurations with 2+1+1 dynamical flavors of HISQ quarks with  $u/d$  masses down to the physical value.

<sup>11</sup> FRITZSCH 12 determine  $m_s$  using a lattice computation with  $n_f = 2$  dynamical flavors.

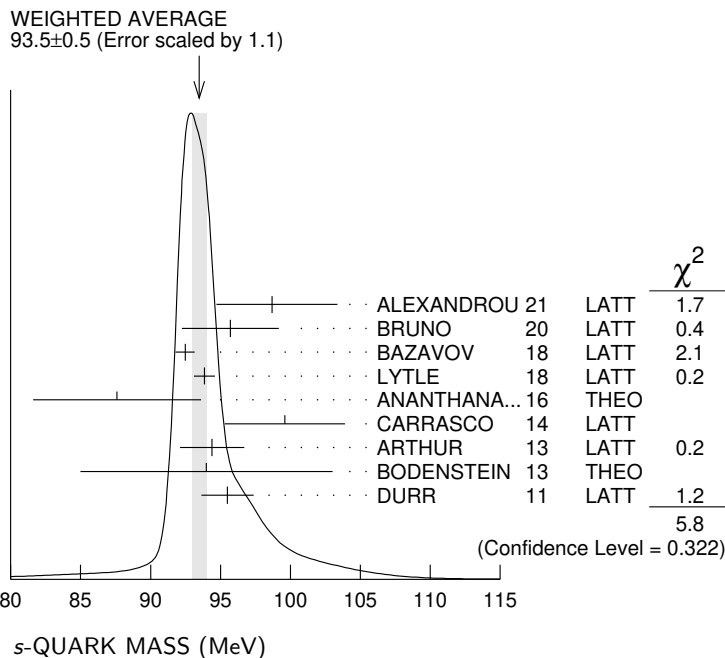
<sup>12</sup> AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using  $n_f = 2 + 1$  dynamical flavors of domain wall fermions.

<sup>13</sup> BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using  $n_f=2$  dynamical twisted-mass Wilson fermions.

<sup>14</sup> BLUM 10 determines light quark masses using a QCD plus QED lattice computation of the electromagnetic mass splittings of the low-lying hadrons. The lattice simulations use 2+1 dynamical quark flavors.

- 15 DAVIES 10 and MCNEILE 10 determine  $\overline{m}_C(\mu)/\overline{m}_S(\mu) = 11.85 \pm 0.16$  using a lattice computation with  $n_f = 2 + 1$  dynamical fermions of the pseudoscalar meson masses. Mass  $m_S$  is obtained from this using the value of  $m_C$  from ALLISON 08 or MCNEILE 10. NODE=Q123SM;LINKAGE=DA
- 16 ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization. NODE=Q123SM;LINKAGE=LT
- 17 BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization. NODE=Q123SM;LINKAGE=BO
- 18 DOMINGUEZ 08A make determination from QCD finite energy sum rules for the pseudoscalar two-point function computed to order  $\alpha_s^4$ . NODE=Q123SM;LINKAGE=DO
- 19 ISHIKAWA 08 use a lattice computation of the light meson spectrum with 2+1 dynamical flavors of  $\mathcal{O}(a)$  improved Wilson quarks, and one-loop perturbative renormalization. NODE=Q123SM;LINKAGE=IS
- 20 NAKAMURA 08 do a lattice computation using quenched domain wall fermions and non-perturbative renormalization. NODE=Q123SM;LINKAGE=NM
- 21 BLUM 07 determine quark masses from the pseudoscalar meson masses using a QED plus QCD lattice computation with two dynamical quark flavors. NODE=Q123SM;LINKAGE=BL
- 22 CHETYRKIN 06 use QCD sum rules in the pseudoscalar channel to order  $\alpha_s^4$ . NODE=Q123SM;LINKAGE=HE
- 23 GOCKELER 06 use an unquenched lattice computation of the axial Ward Identity with  $n_f = 2$  dynamical light quark flavors, and non-perturbative renormalization, to obtain  $\overline{m}_S(2 \text{ GeV}) = 111 \pm 6 \pm 4 \pm 6 \text{ MeV}$ , where the first error is statistical, the second and third are systematic due to the fit range and force scale uncertainties, respectively. We have combined the systematic errors linearly. NODE=Q123SM;LINKAGE=CK
- 24 GOCKELER 06A use an unquenched lattice computation of the pseudoscalar meson masses with  $n_f = 2$  dynamical light quark flavors, and non-perturbative renormalization. NODE=Q123SM;LINKAGE=GO
- 25 JAMIN 06 determine  $\overline{m}_S(2 \text{ GeV})$  from the spectral function for the scalar  $K\pi$  form factor. NODE=Q123SM;LINKAGE=JM
- 26 MASON 06 extract light quark masses from a lattice simulation using staggered fermions with an improved action, and three dynamical light quark flavors with degenerate  $u$  and  $d$  quarks. Perturbative corrections were included at NNLO order. NODE=Q123SM;LINKAGE=MA
- 27 NARISON 06 uses sum rules for  $e^+e^- \rightarrow \text{hadrons}$  to order  $\alpha_s^3$ . NODE=Q123SM;LINKAGE=NI
- 28 NARISON 06 obtains the quoted range from positivity of the spectral functions. NODE=Q123SM;LINKAGE=NR
- 29 BAIKOV 05 determines  $\overline{m}_S(M_\tau) = 100^{+5+17}_{-3-19}$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ , with an estimate of the  $\alpha_s^4$  terms. We have converted the result to  $\mu = 2 \text{ GeV}$ . NODE=Q123SM;LINKAGE=BA
- 30 GAMIZ 05 determines  $\overline{m}_S(2 \text{ GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^2$ , with an estimate of the  $\alpha_s^3$  terms. NODE=Q123SM;LINKAGE=GA
- 31 GORBUNOV 05 use hadronic tau decays to N3LO, including power corrections. NODE=Q123SM;LINKAGE=GB
- 32 NARISON 05 determines  $\overline{m}_S(2 \text{ GeV})$  from sum rules using the strange spectral function in  $\tau$  decay. The computations were done to order  $\alpha_s^3$ . NODE=Q123SM;LINKAGE=NA
- 33 AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant. NODE=Q123SM;LINKAGE=AU
- 34 AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory. Determines  $m_s = 113.8 \pm 2.3^{+5.8}_{-2.9}$  using  $K$  mass as input and  $m_s = 142.3 \pm 5.8^{+22}_0$  using  $\phi$  mass as input. We have performed a weighted average of these values. NODE=Q123SM;LINKAGE=AO
- 35 AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action. NODE=Q123SM;LINKAGE=AI
- 36 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization. They also quote  $\overline{m}/m_s = 24.3 \pm 0.2 \pm 0.6$ . NODE=Q123SM;LINKAGE=BE
- 37 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation. NODE=Q123SM;LINKAGE=CH
- 38 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is chosen to satisfy CKM unitarity. NODE=Q123SM;LINKAGE=G1
- 39 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is taken from the PDG. NODE=Q123SM;LINKAGE=G2





## OTHER LIGHT QUARK MASS RATIOS

### $m_s/m_d$ MASS RATIO

VALUE	DOCUMENT ID	TECN	COMMENT
<b>17–22 OUR EVALUATION</b>			
20.0	<sup>1</sup> GAO	97	THEO
18.9±0.8	<sup>2</sup> LEUTWYLER	96	THEO Compilation
21	<sup>3</sup> DONOGHUE	92	THEO
18	<sup>4</sup> GERARD	90	THEO
18 to 23	<sup>5</sup> LEUTWYLER	90B	THEO

- <sup>1</sup> GAO 97 uses electromagnetic mass splittings of light mesons.  
<sup>2</sup> LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi (\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .  
<sup>3</sup> DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \rightarrow 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ .  
<sup>4</sup> GERARD 90 uses large  $N$  and  $\eta$ - $\eta'$  mixing.  
<sup>5</sup> LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .

### $m_s/\bar{m}$ MASS RATIO

$$\bar{m} \equiv (m_u + m_d)/2$$

VALUE	CL%	DOCUMENT ID	TECN
<b>27.33<sup>+0.18</sup><sub>-0.14</sub> (CL = 90%) OUR EVALUATION</b>			See the ideogram below.

27.17±0.32 <sup>+0.56</sup> <sub>-0.38</sub>	<sup>1</sup> ALEXANDROU21	LATT
27.0 ±1.0 ±0.4	<sup>2</sup> BRUNO	20 LATT
27.35±0.05 <sup>+0.10</sup> <sub>-0.07</sub>	<sup>3</sup> BAZAVOV	14A LATT
26.66±0.32	<sup>4</sup> CARRASCO	14 LATT
27.36±0.54	<sup>5</sup> ARTHUR	13 LATT
27.53±0.20±0.08	<sup>6</sup> DURR	11 LATT

• • • We do not use the following data for averages, fits, limits, etc. • • •

26.8 ±1.4	<sup>7</sup> AOKI	11A LATT
27.3 ±0.9	<sup>8</sup> BLOSSIER	10 LATT
28.8 ±1.65	<sup>9</sup> ALLTON	08 LATT
27.3 ±0.3 ±1.2	<sup>10</sup> BLOSSIER	08 LATT
23.5 ±1.5	<sup>11</sup> OLLER	07A THEO
27.4 ±0.4	<sup>12</sup> AUBIN	04 LATT

NODE=Q123220

NODE=Q123MR1  
 NODE=Q123MR1  
 → UNCHECKED ←

NODE=Q123MR1;LINKAGE=L  
 NODE=Q123MR1;LINKAGE=M

NODE=Q123MR1;LINKAGE=J

NODE=Q123MR1;LINKAGE=C1  
 NODE=Q123MR1;LINKAGE=G

NODE=Q123MR5

NODE=Q123MR5  
 NODE=Q123MR5

→ UNCHECKED ←

- <sup>1</sup> ALEXANDROU 21 determines the quark mass using a lattice calculation of the meson and baryon masses with a twisted mass fermion action. The simulations are carried out using 2+1+1 dynamical quarks with  $m_u = m_d \neq m_s \neq m_c$ , including gauge ensembles close to the physical pion point.
- <sup>2</sup> BRUNO 20 determines the light quark mass using a lattice calculation with  $n_f = 2+1$  flavors of Wilson fermions. The scale has been set from  $f_\pi$  and  $f_K$ . The tuning was done using the masses of the lightest ( $\pi$ ) and strange ( $K$ ) pseudoscalar mesons.
- <sup>3</sup> BAZAVOV 14A is a lattice computation using 4 dynamical flavors of HISQ fermions.
- <sup>4</sup> CARRASCO 14 is a lattice QCD computation of light quark masses using 2 + 1 + 1 dynamical quarks, with  $m_u = m_d \neq m_s \neq m_c$ . The  $u$  and  $d$  quark masses are obtained separately by using the  $K$  meson mass splittings and lattice results for the electromagnetic contributions.
- <sup>5</sup> ARTHUR 13 is a lattice computation using 2+1 dynamical domain wall fermions.
- <sup>6</sup> DURR 11 determine quark mass from a lattice computation of the meson spectrum using  $n_f = 2 + 1$  dynamical flavors. The lattice simulations were done at the physical quark mass, so that extrapolation in the quark mass was not needed.
- <sup>7</sup> AOKI 11A determine quark masses from a lattice computation of the hadron spectrum using  $n_f = 2 + 1$  dynamical flavors of domain wall fermions.
- <sup>8</sup> BLOSSIER 10 determines quark masses from a computation of the hadron spectrum using  $n_f=2$  dynamical twisted-mass Wilson fermions.
- <sup>9</sup> ALLTON 08 use a lattice computation of the  $\pi$ ,  $K$ , and  $\Omega$  masses with 2+1 dynamical flavors of domain wall quarks, and non-perturbative renormalization.
- <sup>10</sup> BLOSSIER 08 use a lattice computation of pseudoscalar meson masses and decay constants with 2 dynamical flavors and non-perturbative renormalization.
- <sup>11</sup> OLLER 07A use unitarized chiral perturbation theory to order  $p^4$ .
- <sup>12</sup> Three flavor dynamical lattice calculation of pseudoscalar meson masses.

NODE=Q123MR5;LINKAGE=D

NODE=Q123MR5;LINKAGE=E

NODE=Q123MR5;LINKAGE=B

NODE=Q123MR5;LINKAGE=A

NODE=Q123MR5;LINKAGE=C

NODE=Q123MR5;LINKAGE=DU

NODE=Q123MR5;LINKAGE=OK

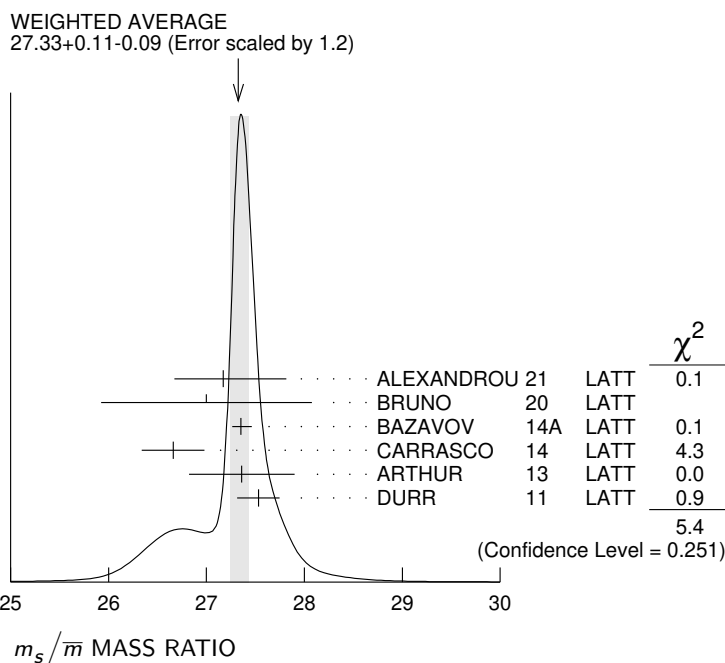
NODE=Q123MR5;LINKAGE=BS

NODE=Q123MR5;LINKAGE=LT

NODE=Q123MR5;LINKAGE=BO

NODE=Q123MR5;LINKAGE=OL

NODE=Q123MR5;LINKAGE=AU



## Q MASS RATIO

$$Q \equiv \sqrt{(m_s^2 - \bar{m}^2)/(m_d^2 - m_u^2)}; \quad \bar{m} \equiv (m_u + m_d)/2$$

VALUE DOCUMENT ID TECN

• • • We do not use the following data for averages, fits, limits, etc. • • •

22.1±0.7	<sup>1</sup> COLANGELO	18	THEO
22.0±0.7	<sup>2</sup> COLANGELO	17	THEO
21.6±1.1	<sup>3</sup> GUO	17	THEO
23.4±0.4±0.5	<sup>4</sup> FODOR	16	LATT
21.4±0.4	<sup>5</sup> GUO	15F	THEO
22.8±0.4	<sup>6</sup> MARTEMYA...	05	THEO
22.7±0.8	<sup>7</sup> ANISOVICH	96	THEO

<sup>1</sup> COLANGELO 18 obtain  $Q$  from a dispersive analysis of  $\eta \rightarrow 3\pi$  decay.

<sup>2</sup> COLANGELO 17 obtain  $Q$  from a dispersive analysis of KLOE collaboration data on  $\eta \rightarrow \pi^+ \pi^- \pi^0$  decays and chiral perturbation theory input.

<sup>3</sup> GUO 17 determine  $Q$  from a dispersive model fit to KLOE and WASA-at-COSY data on  $\eta \rightarrow \pi^+ \pi^- \pi^0$  decay and matching to chiral perturbation theory.

<sup>4</sup> FODOR 16 is a lattice simulation with  $n_f = 2 + 1$  dynamical flavors and includes partially quenched QED effects.

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NODE=Q123MR3

NODE=Q123MR3

NODE=Q123MR3;LINKAGE=G

NODE=Q123MR3;LINKAGE=C

NODE=Q123MR3;LINKAGE=F

NODE=Q123MR3;LINKAGE=A

- <sup>5</sup> GUO 15F determine  $Q$  from a Khuri-Treiman analysis of  $\eta \rightarrow 3\pi$  decays.  
<sup>6</sup> MARTEMYANOV 05 determine  $Q$  from  $\eta \rightarrow 3\pi$  decay.  
<sup>7</sup> ANISOVICH 96 find  $Q$  from  $\eta \rightarrow \pi^+ \pi^- \pi^0$  decay using dispersion relations and chiral perturbation theory.

NODE=Q123MR3;LINKAGE=E  
 NODE=Q123MR3;LINKAGE=MA  
 NODE=Q123MR3;LINKAGE=D

## LIGHT QUARKS ( $u, d, s$ ) REFERENCES

NODE=Q123

ALEXANDROU 21	PR D104 074515	C. Alexandrou <i>et al.</i>	(ETM Collab.)	REFID=61083
BRUNO 20	EPJ C80 169	M. Bruno <i>et al.</i>	(ALPHA Collab.)	REFID=61088
DOMINGUEZ 19	JHEP 1902 057	C.A. Dominguez, A. Mes, K. Schilcher	(CAPE, MAINZ)	REFID=59648
BAZAVOV 18	PR D98 054517	A. Bazavov <i>et al.</i>	(Fermilab Lattice, MILC, TUMQCD)	REFID=59445
COLANGELO 18	EPJ C78 947	G. Colangelo <i>et al.</i>		REFID=59329
LYTLE 18	PR D98 014513	A.T. Lytle <i>et al.</i>	(HPQCD Collab.)	REFID=59647
COLANGELO 17	PRL 118 022001	G. Colangelo <i>et al.</i>	(BERN, IND, JLAB)	REFID=57655
GUO 17	PL B771 497	P. Guo <i>et al.</i>		REFID=57788
YUAN 17	PR D96 014034	J.-M. Yuan <i>et al.</i>		REFID=58020
ANANTHANARAYAN...15	PR D94 116014	B. Ananthanarayan, D. Das	(BANG, AHMED)	REFID=57627
FODOR 16	PRL 117 082001	Z. Fodor <i>et al.</i>	(BMW Collab.)	REFID=57459
BASAK 15	JPCS 640 012052	S. Basak <i>et al.</i>	(MILC Collab.)	REFID=57136
CHAKRABORTY...15	PR D91 054508	B. Chakraborty <i>et al.</i>	(HPQCD Collab.)	REFID=56729
GUO 15F	PR D92 054016	P. Guo <i>et al.</i>		REFID=57789
BAZAVOV 14A	PR D90 074509	A. Bazavov <i>et al.</i>	(Fermi-LAT and MILC Collabs.)	REFID=57134
CARRASCO 14	NP B887 19	N. Carrasco <i>et al.</i>	(European Twisted Mass Collab.)	REFID=56204
ARTHUR 13	PR D87 094514	R. Arthur <i>et al.</i>	(RBC and UKQCD Collabs.)	REFID=57135
BODENSTEIN 13	JHEP 1307 138	S. Bodenstein, C.A. Dominguez, K. Schilcher		REFID=55043;ERROR=1
AOKI 12	PR D86 034507	S. Aoki <i>et al.</i>	(PACS-CS Collab.)	REFID=57137
FRITZSCH 12	NP B865 397	P. Fritzsch <i>et al.</i>	(ALPHA Collab.)	REFID=54481
AOKI 11A	PR D83 074508	Y. Aoki <i>et al.</i>	(RBC-UKQCD Collab.)	REFID=54039
DURR 11	PL B701 265	S. Durr <i>et al.</i>	(BMW Collab.)	REFID=16699
BAZAVOV 10	RMP 82 1349	A. Bazavov <i>et al.</i>	(MILC Collab.)	REFID=53244
BLOSSIER 10	PR D82 114513	B. Blossier <i>et al.</i>	(ETM Collab.)	REFID=53591
BLUM 10	PR D82 094508	T. Blum <i>et al.</i>		REFID=53494
DAVIES 10	PRL 104 132003	C.T.H. Davies <i>et al.</i>	(HPQCD Collab.)	REFID=53243
MCNEILE 10	PR D82 034512	C. McNeile <i>et al.</i>	(HPQCD Collab.)	REFID=53407
DOMINGUEZ 09	PR D79 014009	C.A. Dominguez <i>et al.</i>		REFID=52641
ALLISON 08	PR D78 054513	I. Allison <i>et al.</i>	(HPQCD Collab.)	REFID=53238
ALLTON 08	PR D78 114509	C. Allton <i>et al.</i>	(RBC and UKQCD Collabs.)	REFID=52624
BLOSSIER 08	JHEP 0804 020	B. Blossier <i>et al.</i>	(ETM Collab.)	REFID=52319
DEANDREA 08	PR D78 034032	A. Deandrea, A. Nehme, P. Talavera		REFID=52423
DOMINGUEZ 08A	JHEP 0805 020	C.A. Dominguez <i>et al.</i>		REFID=52322
DOMINGUEZ...08B	PL B660 49	A. Dominguez-Clarimon, E. de Rafael, J. Taron		REFID=52453
ISHIKAWA 08	PR D78 011502	T. Ishikawa <i>et al.</i>	(CP-PACS and JLQCD Collabs.)	REFID=52411
NAKAMURA 08	PR D78 034502	Y. Nakamura <i>et al.</i>	(CP-PACS Collab.)	REFID=52424
BLUM 07	PR D76 114508	T. Blum <i>et al.</i>	(RBC Collab.)	REFID=52101
OLLER 07A	EPJ A34 371	J.A. Oller, L. Roca		REFID=52478
CHETYRKIN 06	EPJ C46 721	K.G. Chetyrkin, A. Khodjamirian		REFID=51389
GOCKELER 06	PR D73 054508	M. Gockeler <i>et al.</i>	(QCDSF and UKQCD Collabs.)	REFID=51300
GOCKELER 06A	PL B639 307	M. Gockeler <i>et al.</i>	(QCDSF and UKQCD Collabs.)	REFID=51372
JAMIN 06	PR D74 074009	M. Jamin, J.A. Oller, A. Pich		REFID=51469
MASON 06	PR D73 114501	Q. Mason <i>et al.</i>	(HPQCD Collab.)	REFID=53059
NARISON 06	PR D74 034013	S. Narison		REFID=51336
PDG 06	JP G33 1	W.-M. Yao <i>et al.</i>	(PDG Collab.)	REFID=51004
BAIKOV 05	PRL 95 012003	P.A. Baikov, K.G. Chetyrkin, J.H. Kuhn		REFID=50684
GAMIZ 05	PRL 94 011803	E. Gamiz <i>et al.</i>		REFID=50477
GORBUNOV 05	PR D71 013002	D.S. Gorbunov, A.A. Pivovarov		REFID=51601
MARTEMYA...05	PR D71 017501	B.V. Martemyanov, V.S. Sopov		REFID=50391
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AUBIN 04	PR D70 031504	C. Aubin <i>et al.</i>	(HPQCD, MILC, UKQCD Collabs.)	REFID=50047
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AOKI 03	PR D67 034503	S. Aoki <i>et al.</i>	(CP-PACS Collab.)	REFID=49337
AOKI 03B	PR D68 054502	S. Aoki <i>et al.</i>	(CP-PACS Collab.)	REFID=49569
BECIREVIC 03	PL B558 69	D. Becirevic, V. Lubicz, C. Tarantino		REFID=49366;ERROR=2
CHIU 03	NP B673 217	T.-W. Chiu, T.-H. Hsieh		REFID=50028
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GAO 97	PR D56 4115	D.-N. Gao, B.A. Li, M.-L. Yan		REFID=45669
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DONOGHUE 92	PRL 69 3444	J.F. Donoghue, B.R. Holstein, D. Wyler	(MASA+)	REFID=43123
GERARD 90	MPL A5 391	J.M. Gerard	(MPIM)	REFID=43397
LEUTWYLER 90B	NP B337 108	H. Leutwyler	(BERN)	REFID=43411