

# LIGHT QUARKS ( $u$ , $d$ , $s$ )

OMITTED FROM SUMMARY TABLE

## $u$ -QUARK MASS

The  $u$ -,  $d$ -, and  $s$ -quark masses are estimates of so-called “current-quark masses,” in a mass- independent subtraction scheme such as  $\overline{\text{MS}}$ . The ratios  $m_u/m_d$  and  $m_s/m_d$  are extracted from pion and kaon masses using chiral symmetry. The estimates of  $d$  and  $u$  masses are not without controversy and remain under active investigation. Within the literature there are even suggestions that the  $u$  quark could be essentially massless. The  $s$ -quark mass is estimated from SU(3) splittings in hadron masses.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of “Our Evaluation” were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b>1.5 to 3.0 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$1.7 \pm 0.3$	<sup>1</sup> AUBIN	04A LATT	$\overline{\text{MS}}$ scheme
$2.9 \pm 0.6$	<sup>2</sup> JAMIN	02 THEO	$\overline{\text{MS}}$ scheme
$2.3 \pm 0.4$	<sup>3</sup> NARISON	99 THEO	$\overline{\text{MS}}$ scheme
$3.9 \pm 1.1$	<sup>4</sup> JAMIN	95 THEO	$\overline{\text{MS}}$ scheme
$3.0 \pm 0.7$	<sup>5</sup> NARISON	95C THEO	$\overline{\text{MS}}$ scheme
<sup>1</sup> AUBIN 04A employ a partially quenched lattice calculation of the pseudoscalar meson masses.			
<sup>2</sup> JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain $m_u$ .			
<sup>3</sup> NARISON 99 uses sum rules to order $\alpha_s^3$ for $\phi$ meson decays to get $m_s$ , and finds $m_u$ by combining with sum rule estimates of $m_u + m_d$ and Dashen's formula.			
<sup>4</sup> JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled $m_u(1 \text{ GeV}) = 5.3 \pm 1.5$ to $\mu = 2$ GeV.			
<sup>5</sup> For NARISON 95C, we have rescaled $m_u(1 \text{ GeV}) = 4 \pm 1$ to $\mu = 2$ GeV.			

## $d$ -QUARK MASS

See the comment for the  $u$  quark above.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35. The values of “Our Evaluation” were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b>3 to 7 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			

$3.9 \pm 0.5$	<sup>6</sup> AUBIN	04A LATT $\overline{\text{MS}}$ scheme
$5.2 \pm 0.9$	<sup>7</sup> JAMIN	02 THEO $\overline{\text{MS}}$ scheme
$6.4 \pm 1.1$	<sup>8</sup> NARISON	99 THEO $\overline{\text{MS}}$ scheme
$7.0 \pm 1.1$	<sup>9</sup> JAMIN	95 THEO $\overline{\text{MS}}$ scheme
$7.4 \pm 0.7$	<sup>10</sup> NARISON	95C THEO $\overline{\text{MS}}$ scheme

<sup>6</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses, and one-loop perturbative renormalization constant.

<sup>7</sup> JAMIN 02 first calculates the strange quark mass from QCD sum rules using the scalar channel, and then combines with the quark mass ratios obtained from chiral perturbation theory to obtain  $m_d$ .

<sup>8</sup> NARISON 99 uses sum rules to order  $\alpha_s^3$  for  $\phi$  meson decays to get  $m_s$ , and finds  $m_d$  by combining with sum rule estimates of  $m_u + m_d$  and Dashen's formula.

<sup>9</sup> JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled  $m_d(1 \text{ GeV}) = 9.4 \pm 1.5$  to  $\mu = 2 \text{ GeV}$ .

<sup>10</sup> For NARISON 95C, we have rescaled  $m_d(1 \text{ GeV}) = 10 \pm 1$  to  $\mu = 2 \text{ GeV}$ .

$$\overline{m} = (m_u + m_d)/2$$

See the comments for the  $u$  quark above.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2 \text{ GeV}$ . Results quoted in the literature at  $\mu = 1 \text{ GeV}$  have been rescaled by dividing by 1.35. The values of "Our Evaluation" were determined in part via Figures 1 and 2.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b>2.5 to 5.5 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$2.8 \pm 0.3$	<sup>11</sup> AUBIN	04 LATT $\overline{\text{MS}}$ scheme	
$4.29 \pm 0.14 \pm 0.65$	<sup>12</sup> AOKI	03 LATT $\overline{\text{MS}}$ scheme	
$3.223^{+0.046}_{-0.069}$	<sup>13</sup> AOKI	03B LATT $\overline{\text{MS}}$ scheme	
$4.4 \pm 0.1 \pm 0.4$	<sup>14</sup> BECIREVIC	03 LATT $\overline{\text{MS}}$ scheme	
$4.1 \pm 0.3 \pm 1.0$	<sup>15</sup> CHIU	03 LATT $\overline{\text{MS}}$ scheme	
$3.45^{+0.14}_{-0.20}$	<sup>16</sup> ALIKHAN	02 LATT $\overline{\text{MS}}$ scheme	
$5.3 \pm 0.3$	<sup>17</sup> CHIU	02 LATT $\overline{\text{MS}}$ scheme	
$3.9 \pm 0.6$	<sup>18</sup> MALTMAN	02 THEO $\overline{\text{MS}}$ scheme	
$3.9 \pm 0.6$	<sup>19</sup> MALTMAN	01 THEO $\overline{\text{MS}}$ scheme	
$4.57 \pm 0.18$	<sup>20</sup> AOKI	00 LATT $\overline{\text{MS}}$ scheme	
$4.4 \pm 2$	<sup>21</sup> GOECKELER	00 LATT $\overline{\text{MS}}$ scheme	
$4.23 \pm 0.29$	<sup>22</sup> AOKI	99 LATT $\overline{\text{MS}}$ scheme	
$\geq 2.1$	<sup>23</sup> STEELE	99 THEO $\overline{\text{MS}}$ scheme	
$4.5 \pm 0.4$	<sup>24</sup> BECIREVIC	98 LATT $\overline{\text{MS}}$ scheme	
$4.6 \pm 1.2$	<sup>25</sup> DOSCH	98 THEO $\overline{\text{MS}}$ scheme	
$4.7 \pm 0.9$	<sup>26</sup> PRADES	98 THEO $\overline{\text{MS}}$ scheme	
$2.7 \pm 0.2$	<sup>27</sup> EICKER	97 LATT $\overline{\text{MS}}$ scheme	
$3.6 \pm 0.6$	<sup>28</sup> GOUGH	97 LATT $\overline{\text{MS}}$ scheme	
$3.4 \pm 0.4 \pm 0.3$	<sup>29</sup> GUPTA	97 LATT $\overline{\text{MS}}$ scheme	
$> 3.8$	<sup>30</sup> LELLOUCH	97 THEO $\overline{\text{MS}}$ scheme	
$4.5 \pm 1.0$	<sup>31</sup> BIJNENS	95 THEO $\overline{\text{MS}}$ scheme	

- 11 AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.
- 12 AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.
- 13 AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- 14 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization.
- 15 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- 16 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks.
- 17 CHIU 02 extracts the average light quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- 18 MALTMAN 02 uses finite energy sum rules in the  $ud$  and  $us$  pseudoscalar channels. Other mass values are also obtained by similar methods.
- 19 MALTMAN 01 uses Borel transformed and finite energy sum rules.
- 20 AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action.
- 21 GOECKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using  $\mathcal{O}(a)$  improved Wilson fermions and nonperturbative renormalization.
- 22 AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the staggered quark action employing the regularization independent scheme.
- 23 STEELE 99 obtain a bound on the light quark masses by applying the Holder inequality to a sum rule. We have converted their bound of  $(m_u+m_d)/2 \geq 3$  MeV at  $\mu=1$  GeV to  $\mu=2$  GeV.
- 24 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the  $\overline{\text{MS}}$  scheme is at NNLO.
- 25 DOSCH 98 use sum rule determinations of the quark condensate and chiral perturbation theory to obtain  $9.4 \leq (m_u+m_d)(1 \text{ GeV}) \leq 15.7$  MeV. We have converted to result to  $\mu=2$  GeV.
- 26 PRADES 98 uses finite energy sum rules for the axial current correlator.
- 27 EICKER 97 use lattice gauge computations with two dynamical light flavors.
- 28 GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives  $2.1 < \overline{m} < 3.5$  MeV at  $\mu=2$  GeV.
- 29 GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamic flavors at  $\mu = 2$  GeV is  $2.7 \pm 0.3 \pm 0.3$  MeV.
- 30 LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- 31 BIJNENS 95 determines  $m_u+m_d$  (1 GeV) =  $12 \pm 2.5$  MeV using finite energy sum rules. We have rescaled this to 2 GeV.

## s-QUARK MASS

See the comment for the  $u$  quark above.

We have normalized the  $\overline{\text{MS}}$  masses at a renormalization scale of  $\mu = 2$  GeV. Results quoted in the literature at  $\mu = 1$  GeV have been rescaled by dividing by 1.35.

VALUE (MeV)	DOCUMENT ID	TECN	COMMENT
<b>95 <math>\pm 25</math> OUR EVALUATION</b>			
96 $\begin{smallmatrix} +5 \\ -3 \end{smallmatrix}$ $\begin{smallmatrix} +16 \\ -18 \end{smallmatrix}$	32 BAIKOV	05 THEO	$\overline{\text{MS}}$ scheme

81 $\pm 22$	33 GAMIZ	05 THEO $\overline{MS}$ scheme
93 $\pm 32$	34 NARISON	05 THEO $\overline{MS}$ scheme
76 $\pm 8$	35 AUBIN	04 LATT $\overline{MS}$ scheme
116 $\pm 6 \pm 0.65$	36 AOKI	03 LATT $\overline{MS}$ scheme
$84.5^{+12}_{-1.7}$	37 AOKI	03B LATT $\overline{MS}$ scheme
106 $\pm 2 \pm 8$	38 BECIREVIC	03 LATT $\overline{MS}$ scheme
92 $\pm 9 \pm 16$	39 CHIU	03 LATT $\overline{MS}$ scheme
117 $\pm 17$	40 GAMIZ	03 THEO $\overline{MS}$ scheme
103 $\pm 17$	41 GAMIZ	03 THEO $\overline{MS}$ scheme
88 $+3$ $-6$	42 ALIKHAN	02 LATT $\overline{MS}$ scheme
115 $\pm 8$	43 CHIU	02 LATT $\overline{MS}$ scheme
99 $\pm 16$	44 JAMIN	02 THEO $\overline{MS}$ scheme
100 $\pm 12$	45 MALTMAN	02 THEO $\overline{MS}$ scheme
116 $+20$ $-25$	46 CHEN	01B THEO $\overline{MS}$ scheme
125 $\pm 27$	47 KOERNER	01 THEO $\overline{MS}$ scheme
130 $\pm 15$	48 AOKI	00 LATT $\overline{MS}$ scheme
105 $\pm 4$	49 GOECKELER	00 LATT $\overline{MS}$ scheme
• • • We do not use the following data for averages, fits, limits, etc. • • •		
118 $\pm 14$	50 AOKI	99 LATT $\overline{MS}$ scheme
170 $+44$ $-55$	51 BARATE	99R ALEP $\overline{MS}$ scheme
115 $\pm 8$	52 MALTMAN	99 THEO $\overline{MS}$ scheme
129 $\pm 24$	53 NARISON	99 THEO $\overline{MS}$ scheme
114 $\pm 23$	54 PICH	99 THEO $\overline{MS}$ scheme
111 $\pm 12$	55 BECIREVIC	98 LATT $\overline{MS}$ scheme
148 $\pm 48$	56 CHETYRKIN	98 THEO $\overline{MS}$ scheme
103 $\pm 10$	57 CUCCHIERI	98 LATT $\overline{MS}$ scheme
115 $\pm 19$	58 DOMINGUEZ	98 THEO $\overline{MS}$ scheme
$152.4 \pm 14.1$	59 CHETYRKIN	97 THEO $\overline{MS}$ scheme
$\geq 89$	60 COLANGELO	97 THEO $\overline{MS}$ scheme
140 $\pm 20$	61 EICKER	97 LATT $\overline{MS}$ scheme
95 $\pm 16$	62 GOUGH	97 LATT $\overline{MS}$ scheme
100 $\pm 21 \pm 10$	63 GUPTA	97 LATT $\overline{MS}$ scheme
$> 100$	64 LELLOUCH	97 THEO $\overline{MS}$ scheme
140 $\pm 24$	65 JAMIN	95 THEO $\overline{MS}$ scheme
<p><sup>32</sup> BAIKOV 05 determines <math>\overline{m}_s(M_\tau) = 100^{+5+17}_{-3-19}</math> from sum rules using the strange spectral function in <math>\tau</math> decay. The computations were done to order <math>\alpha_s^3</math>, with an estimate of the <math>\alpha_s^4</math> terms. We have converted the result to <math>\mu = 2</math> GeV.</p> <p><sup>33</sup> GAMIZ 05 determines <math>\overline{m}_s(2 \text{ GeV})</math> from sum rules using the strange spectral function in <math>\tau</math> decay. The computations were done to order <math>\alpha_s^2</math>, with an estimate of the <math>\alpha_s^3</math> terms.</p> <p><sup>34</sup> NARISON 05 determines <math>\overline{m}_s(2 \text{ GeV})</math> from sum rules using the strange spectral function in <math>\tau</math> decay. The computations were done to order <math>\alpha_s^3</math>.</p> <p><sup>35</sup> AUBIN 04 perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with one-loop perturbative renormalization constant.</p> <p><sup>36</sup> AOKI 03 uses quenched lattice simulation of the meson and baryon masses with degenerate light quarks. The extrapolations are done using quenched chiral perturbation theory.</p>		

- Determines  $m_s = 113.8 \pm 2.3^{+5.8}_{-2.9}$  using  $K$  mass as input and  $m_s = 142.3 \pm 5.8^{+22}_{-0}$  using  $\phi$  mass as input. We have performed a weighted average of these values.
- 37 AOKI 03B uses lattice simulation of the meson and baryon masses with two dynamical light quarks. Simulations are performed using the  $\mathcal{O}(a)$  improved Wilson action.
- 38 BECIREVIC 03 perform quenched lattice computation using the vector and axial Ward identities. Uses  $\mathcal{O}(a)$  improved Wilson action and nonperturbative renormalization. They also quote  $\overline{m}/m_s = 24.3 \pm 0.2 \pm 0.6$ .
- 39 CHIU 03 determines quark masses from the pion and kaon masses using a lattice simulation with a chiral fermion action in quenched approximation.
- 40 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is chosen to satisfy CKM unitarity.
- 41 GAMIZ 03 determines  $m_s$  from SU(3) breaking in the  $\tau$  hadronic width. The value of  $V_{us}$  is taken from the PDG.
- 42 ALIKHAN 02 uses lattice simulation of the meson and baryon masses with two dynamical flavors and degenerate light quarks. The above value uses the  $K$ -meson mass to determine  $m_s$ . If the  $\phi$  meson is used, the number changes to  $90^{+5}_{-10}$ .
- 43 CHIU 02 extracts the strange quark mass from quenched lattice simulations using quenched chiral perturbation theory.
- 44 JAMIN 02 calculates the strange quark mass from QCD sum rules using the scalar channel.
- 45 MALTMAN 02 uses finite energy sum rules in the  $ud$  and  $us$  pseudoscalar channels. Other mass values are also obtained by similar methods.
- 46 CHEN 01B uses an analysis of the hadronic spectral function in  $\tau$  decay.
- 47 KOERNER 01 obtain the  $s$  quark mass of  $m_s(m_\tau) = 130 \pm 27(\text{exp}) \pm 9(\text{thy})$  MeV from an analysis of Cabibbo suppressed  $\tau$  decays. We have converted this to  $\mu = 2$  GeV.
- 48 AOKI 00 obtain the light quark masses from a quenched lattice simulation of the meson and baryon spectrum with the Wilson quark action. We have averaged their results of  $m_s = 115.6 \pm 2.3$  and  $m_s = 143.7 \pm 5.8$  obtained using  $m_K$  and  $m_\phi$ , respectively, to normalize the spectrum.
- 49 GOECKELER 00 obtained from a quenched lattice computation of the pseudoscalar meson masses using  $\mathcal{O}(a)$  improved Wilson fermions and nonperturbative renormalization.
- 50 AOKI 99 obtain the light quark masses from a quenched lattice simulation of the meson spectrum with the Staggered quark action employing the regularization independent scheme. We have averaged their results of  $m_s = 106.0 \pm 7.1$  and  $m_s = 129 \pm 12$  obtained using  $m_K$  and  $m_\phi$ , respectively, to normalize the spectrum.
- 51 BARATE 99R obtain the strange quark mass from an analysis of the observed mass spectra in  $\tau$  decay. We have converted their value of  $m_s(m_\tau) = 176^{+46}_{-57}$  MeV to  $\mu = 2$  GeV.
- 52 MALTMAN 99 determines the strange quark mass using finite energy sum rules.
- 53 NARISON 99 uses sum rules to order  $\alpha_s^3$  for  $\phi$  meson decays.
- 54 PICH 99 obtain the  $s$ -quark mass from an analysis of the moments of the invariant mass distribution in  $\tau$  decays.
- 55 BECIREVIC 98 compute the quark mass using the Alpha action in the quenched approximation. The conversion from the regularization independent scheme to the  $\overline{\text{MS}}$  scheme is at NNLO.
- 56 CHETYRKIN 98 uses spectral moments of hadronic  $\tau$  decays to determine  $m_s(1 \text{ GeV}) = 200 \pm 70$  MeV. We have rescaled the result to  $\mu = 2$  GeV.
- 57 CUCCHIERI 98 obtains the quark mass using a quenched lattice computation of the hadronic spectrum.
- 58 DOMINGUEZ 98 uses hadronic spectral function sum rules (to four loops, and including dimension six operators) to determine  $m_s(1 \text{ GeV}) < 155 \pm 25$  MeV. We have rescaled the result to  $\mu = 2$  GeV.
- 59 CHETYRKIN 97 obtains  $205.5 \pm 19.1$  MeV at  $\mu = 1$  GeV from QCD sum rules including fourth-order QCD corrections. We have rescaled the result to 2 GeV.

- <sup>60</sup> COLANGELO 97 is QCD sum rule computation. We have rescaled  $m_s(1 \text{ GeV}) > 120$  to  $\mu = 2 \text{ GeV}$ .
- <sup>61</sup> EICKER 97 use lattice gauge computations with two dynamical light flavors.
- <sup>62</sup> GOUGH 97 use lattice gauge computations in the quenched approximation. Correcting for quenching gives  $54 < m_s < 92 \text{ MeV}$  at  $\mu = 2 \text{ GeV}$ .
- <sup>63</sup> GUPTA 97 use Lattice Monte Carlo computations in the quenched approximation. The value for two light dynamical flavors at  $\mu = 2 \text{ GeV}$  is  $68 \pm 12 \pm 7 \text{ MeV}$ .
- <sup>64</sup> LELLOUCH 97 obtain lower bounds on quark masses using hadronic spectral functions.
- <sup>65</sup> JAMIN 95 uses QCD sum rules at next-to-leading order. We have rescaled  $m_s(1 \text{ GeV}) = 189 \pm 32$  to  $\mu = 2 \text{ GeV}$ .

## LIGHT QUARK MASS RATIOS

### $u/d$ MASS RATIO

VALUE	DOCUMENT ID	TECN	COMMENT
<b>0.3 to 0.6 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
$0.43 \pm 0.08$	<sup>66</sup> AUBIN	04A LATT	$\overline{MS}$ scheme
$0.410 \pm 0.036$	<sup>67</sup> NELSON	03 LATT	$\overline{MS}$ scheme
0.44	<sup>68</sup> GAO	97 THEO	$\overline{MS}$ scheme
$0.553 \pm 0.043$	<sup>69</sup> LEUTWYLER	96 THEO	Compilation
$< 0.3$	<sup>70</sup> CHOI	92 THEO	
0.26	<sup>71</sup> DONOGHUE	92 THEO	
$0.30 \pm 0.07$	<sup>72</sup> DONOGHUE	92B THEO	
0.66	<sup>73</sup> GERARD	90 THEO	
0.4 to 0.65	<sup>74</sup> LEUTWYLER	90B THEO	
0.05 to 0.78	<sup>75</sup> MALTMAN	90 THEO	

- <sup>66</sup> AUBIN 04A perform three flavor dynamical lattice calculation of pseudoscalar meson masses, with continuum estimate of electromagnetic effects in the kaon masses.
- <sup>67</sup> NELSON 03 computes coefficients in the order  $p^4$  chiral Lagrangian using a lattice calculation with three dynamical flavors. The ratio  $m_u/m_d$  is obtained by combining this with the chiral perturbation theory computation of the meson masses to order  $p^4$ .
- <sup>68</sup> GAO 97 uses electromagnetic mass splittings of light mesons.
- <sup>69</sup> LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi(\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .
- <sup>70</sup> CHOI 92 result obtained from the decays  $\psi(2S) \rightarrow J/\psi(1S)\pi$  and  $\psi(2S) \rightarrow J/\psi(1S)\eta$ , and a dilute instanton gas estimate of some unknown matrix elements.
- <sup>71</sup> DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \rightarrow 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ .
- <sup>72</sup> DONOGHUE 92B computes quark mass ratios using  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ , and an estimate of  $L_{14}$  using Weinberg sum rules.
- <sup>73</sup> GERARD 90 uses large  $N$  and  $\eta$ - $\eta'$  mixing.
- <sup>74</sup> LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .
- <sup>75</sup> MALTMAN 90 uses second-order chiral perturbation theory including nonanalytic terms for the meson masses. Uses a criterion of "maximum reasonableness" that certain coefficients which are expected to be of order one are  $\leq 3$ .

**$s/d$  MASS RATIO**

VALUE	DOCUMENT ID	TECN	COMMENT
<b>17 to 22 OUR EVALUATION</b>			
• • • We do not use the following data for averages, fits, limits, etc. • • •			
20.0	76 GAO	97 THEO	$\overline{MS}$ scheme
$18.9 \pm 0.8$	77 LEUTWYLER	96 THEO	Compilation
21	78 DONOGHUE	92 THEO	
18	79 GERARD	90 THEO	
18 to 23	80 LEUTWYLER	90B THEO	

76 GAO 97 uses electromagnetic mass splittings of light mesons.

77 LEUTWYLER 96 uses a combined fit to  $\eta \rightarrow 3\pi$  and  $\psi' \rightarrow J/\psi (\pi, \eta)$  decay rates, and the electromagnetic mass differences of the  $\pi$  and  $K$ .

78 DONOGHUE 92 result is from a combined analysis of meson masses,  $\eta \rightarrow 3\pi$  using second-order chiral perturbation theory including nonanalytic terms, and  $(\psi(2S) \rightarrow J/\psi(1S)\pi)/(\psi(2S) \rightarrow J/\psi(1S)\eta)$ .

79 GERARD 90 uses large  $N$  and  $\eta$ - $\eta'$  mixing.

80 LEUTWYLER 90B determines quark mass ratios using second-order chiral perturbation theory for the meson and baryon masses, including nonanalytic corrections. Also uses Weinberg sum rules to determine  $L_7$ .

 **$m_s/\overline{m}$  MASS RATIO**

$$\overline{m} \equiv (m_u + m_d)/2$$

VALUE	DOCUMENT ID	TECN
<b>25 to 30 OUR EVALUATION</b>		

• • • We do not use the following data for averages, fits, limits, etc. • • •

$27.4 \pm 0.4$  81 AUBIN 04 LATT

81 Three flavor dynamical lattice calculation of pseudoscalar meson masses.

**Q MASS RATIO**

$$Q \equiv \sqrt{(m_s^2 - \overline{m}^2)/(m_d^2 - m_s^2)}; \quad \overline{m} \equiv (m_u + m_d)/2$$

VALUE	DOCUMENT ID	TECN
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• • • We do not use the following data for averages, fits, limits, etc. • • •

$22.8 \pm 0.4$  82 MARTEMYAN.05 THEO

$22.7 \pm 0.8$  83 ANISOVICH 96 THEO

82 MARTEMYANOV 05 determine  $Q$  from  $\eta \rightarrow 3\pi$  decay.

83 ANISOVICH 96 find  $Q$  from  $\eta \rightarrow \pi^+ \pi^- \pi^0$  decay using dispersion relations and chiral perturbation theory.

**LIGHT QUARKS ( $u, d, s$ ) REFERENCES**

BAIKOV	05	PRL 95 012003	P.A. Baikov, K.G. Chetyrkin, J.H. Kuhn
GAMIZ	05	PRL 94 011803	E. Gamiz <i>et al.</i>
MARTEMYAN...	05	PR D71 017501	B.V. Martemyanov, V.S. Sopov
NARISON	05	PL B626 101	S. Narison
AUBIN	04	PR D70 031504R	C. Aubin <i>et al.</i> (HPQCD, MILC, UKQCD Collabs.)
AUBIN	04A	PR D70 114501	C. Aubin <i>et al.</i> (MILC Collab.)
AOKI	03	PR D67 034503	S. Aoki <i>et al.</i> (CP-PACS Collab.)
AOKI	03B	PR D68 054502	S. Aoki <i>et al.</i> (CP-PACS Collab.)
BECIREVIC	03	PL B558 69	D. Becirevic, V. Lubicz, C. Tarantino
CHIU	03	NP B673 217	T.-W. Chiu, T.-H. Hsieh
GAMIZ	03	JHEP 0301 060	E. Gamiz <i>et al.</i>
NELSON	03	PRL 90 021601	D. Nelson, G.T. Fleming, G.W. Kilcup
ALIKHAN	02	PR D65 054505	A. Ali Khan <i>et al.</i> (CP-PACS Collab.)
Also		PR D67 059901 (erratum)	A. Ali Khan <i>et al.</i> (CP-PACS Collab.)

CHIU	02	PL B538 298	T.-W. Chiu, T.-H. Hsieh
JAMIN	02	EPJ C24 237	M. Jamin, J.A. Oller, A. Pich
MALTMAN	02	PR D65 074013	K. Maltman, J. Kambor
CHEN	01B	EPJ C22 31	S. Chen <i>et al.</i>
KOERNER	01	EPJ C20 259	J.G. Koerner, F. Krajewski, A.A. Pivovarov
MALTMAN	01	PL B517 332	K. Maltman, J. Kambor
AOKI	00	PRL 84 238	S. Aoki <i>et al.</i> (CP-PACS Collab.)
GOECKELER	00	PR D62 054504	M. Goeckeler <i>et al.</i>
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BARATE	99R	EPJ C11 599	R. Barate <i>et al.</i> (ALEPH Collab.)
MALTMAN	99	PL B462 195	K. Maltman
NARISON	99	PL B466 345	S. Narison
PICH	99	JHEP 9910 004	A. Pich, J. Prades
STEELE	99	PL B451 201	T.G. Steele, K. Kostuik, J. Kwan
BEĆIREVIC	98	PL B444 401	D. Bećirevic <i>et al.</i>
CHETYRKIN	98	NP B533 473	K.G. Chetyrkin, J.H. Kuehn, A.A. Pivovarov
CUCCHIERI	98	PL B422 212	A. Chuchieri <i>et al.</i>
DOMINGUEZ	98	PL B425 193	C.A. Dominguez, L. Pirovano, K. Schilcher
DOSCH	98	PL B417 173	H.G. Dosch, S. Narison
PRADES	98	NPBPS 64 253	J. Prades
CHETYRKIN	97	PL B404 337	K.G. Chetyrkin, D. Pirjol, K. Schilcher
COLANGELO	97	PL B408 340	P. Colangelo <i>et al.</i>
EICKER	97	PL B407 290	N. Eicker <i>et al.</i> (SESAM Collab.)
GAO	97	PR D56 4115	D.-N. Gao, B.A. Li, M.-L. Yan
GOUGH	97	PRL 79 1622	B. Gough <i>et al.</i>
GUPTA	97	PR D55 7203	R. Gupta, T. Bhattacharya
LELLOUCH	97	PL B414 195	L. Lellouch, E. de Rafael, J. Taron
ANISOVICH	96	PL B375 335	A.V. Anisovich, H. Leutwyler
LEUTWYLER	96	PL B378 313	H. Leutwyler
BIJNENS	95	PL B348 226	J. Bijnens, J. Prades, E. de Rafael (NORD, BOHR+)
JAMIN	95	ZPHY C66 633	M. Jamin, M. Munz (HEIDT, MUNT)
NARISON	95C	PL B358 113	S. Narison (MONP)
CHOI	92	PL B292 159	K.W. Choi (UCSD)
DONOGHUE	92	PRL 69 3444	J.F. Donoghue, B.R. Holstein, D. Wyler (MASA+)
DONOGHUE	92B	PR D45 892	J.F. Donoghue, D. Wyler (MASA, ZURI, UCSBT)
GERARD	90	MPL A5 391	J.M. Gerard (MPIM)
LEUTWYLER	90B	NP B337 108	H. Leutwyler (BERN)
MALTMAN	90	PL B234 158	K. Maltman, T. Goldman, Stephenson Jr. (YORKC+)