

# STRANGE MESONS ( $S = \pm 1$ , $C = B = 0$ )

$K^+ = u\bar{s}$ ,  $K^0 = d\bar{s}$ ,  $\bar{K}^0 = \bar{d}s$ ,  $K^- = \bar{u}s$ , similarly for  $K^*$ 's

**$K^\pm$**

$$I(J^P) = \frac{1}{2}(0^-)$$

Mass  $m = 493.677 \pm 0.016$  MeV [<sup>a</sup>] ( $S = 2.8$ )

Mean life  $\tau = (1.2380 \pm 0.0021) \times 10^{-8}$  s ( $S = 1.9$ )

$$c\tau = 3.712 \text{ m}$$

**Slope parameter  $g$**  [<sup>b</sup>]

(See Particle Listings for quadratic coefficients and alternative parametrization related to  $\pi\pi$  scattering)

$$K^\pm \rightarrow \pi^\pm \pi^+ \pi^- g = -0.21134 \pm 0.00017$$

$$(g_+ - g_-) / (g_+ + g_-) = (-1.5 \pm 2.2) \times 10^{-4}$$

$$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0 g = 0.626 \pm 0.007$$

$$(g_+ - g_-) / (g_+ + g_-) = (1.8 \pm 1.8) \times 10^{-4}$$

**$K^\pm$  decay form factors** [<sup>c,d</sup>]

Assuming  $\mu$ -e universality

$$\lambda_+(K_{\mu 3}^+) = \lambda_+(K_{e3}^+) = (2.97 \pm 0.05) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.95 \pm 0.12) \times 10^{-2}$$

Not assuming  $\mu$ -e universality

$$\lambda_+(K_{e3}^+) = (2.98 \pm 0.05) \times 10^{-2}$$

$$\lambda_+(K_{\mu 3}^+) = (2.96 \pm 0.17) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.96 \pm 0.13) \times 10^{-2}$$

$K_{e3}$  form factor quadratic fit

$$\lambda'_+(K_{e3}^\pm) \text{ linear coeff.} = (2.48 \pm 0.17) \times 10^{-2}$$

$$\lambda''_+(K_{e3}^\pm) \text{ quadratic coeff.} = (0.19 \pm 0.09) \times 10^{-2}$$

$$K_{e3}^+ |f_S/f_+| = (-0.3^{+0.8}_{-0.7}) \times 10^{-2}$$

$$K_{e3}^+ |f_T/f_+| = (-1.2 \pm 2.3) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_S/f_+| = (0.2 \pm 0.6) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_T/f_+| = (-0.1 \pm 0.7) \times 10^{-2}$$

$$K^+ \rightarrow e^+ \nu_e \gamma |F_A + F_V| = 0.133 \pm 0.008 \quad (S = 1.3)$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma |F_A + F_V| = 0.165 \pm 0.013$$

$$K^+ \rightarrow e^+ \nu_e \gamma |F_A - F_V| < 0.49$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma |F_A - F_V| = -0.24 \text{ to } 0.04, \text{ CL} = 90\%$$

**Charge Radius**

$$\langle r \rangle = 0.560 \pm 0.031 \text{ fm}$$

 **$\mathcal{CP}$  violation parameters**

$$\begin{aligned}\Delta(K_{\pi ee}^\pm) &= (-2.2 \pm 1.6) \times 10^{-2} \\ \Delta(K_{\pi \mu \mu}^\pm) &= -0.02 \pm 0.12\end{aligned}$$

 **$T$  violation parameters**

$$\begin{aligned}K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad P_T &= (-1.7 \pm 2.5) \times 10^{-3} \\ K^+ \rightarrow \mu^+ \nu_\mu \gamma \quad P_T &= (-0.6 \pm 1.9) \times 10^{-2} \\ K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad \text{Im}(\xi) &= -0.006 \pm 0.008\end{aligned}$$

$K^-$  modes are charge conjugates of the modes below.

<b><math>K^+</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	<i>p</i> (MeV/c)
<b>Leptonic and semileptonic modes</b>			
$K^+ \rightarrow e^+ \nu_e$	$(1.584 \pm 0.020) \times 10^{-5}$		247
$K^+ \rightarrow \mu^+ \nu_\mu$	$(63.55 \pm 0.11) \%$	S=1.2	236
$K^+ \rightarrow \pi^0 e^+ \nu_e$ Called $K_{e3}^+$ .	$(5.07 \pm 0.04) \%$	S=2.1	228
$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$ Called $K_{\mu 3}^+$ .	$(3.353 \pm 0.034) \%$	S=1.8	215
$K^+ \rightarrow \pi^0 \pi^0 e^+ \nu_e$	$(2.2 \pm 0.4) \times 10^{-5}$		206
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$	$(4.09 \pm 0.10) \times 10^{-5}$		203
$K^+ \rightarrow \pi^+ \pi^- \mu^+ \nu_\mu$	$(1.4 \pm 0.9) \times 10^{-5}$		151
$K^+ \rightarrow \pi^0 \pi^0 \pi^0 e^+ \nu_e$	$< 3.5 \times 10^{-6}$ CL=90%		135
<b>Hadronic modes</b>			
$K^+ \rightarrow \pi^+ \pi^0$	$(20.66 \pm 0.08) \%$	S=1.2	205
$K^+ \rightarrow \pi^+ \pi^0 \pi^0$	$(1.761 \pm 0.022) \%$	S=1.1	133
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	$(5.59 \pm 0.04) \%$	S=1.3	125
<b>Leptonic and semileptonic modes with photons</b>			
$K^+ \rightarrow \mu^+ \nu_\mu \gamma$	[e,f] $(6.2 \pm 0.8) \times 10^{-3}$		236
$K^+ \rightarrow \mu^+ \nu_\mu \gamma (\text{SD}^+)$	[c,g] $(1.33 \pm 0.22) \times 10^{-5}$		—
$K^+ \rightarrow \mu^+ \nu_\mu \gamma (\text{SD}^+ \text{INT})$	[c,g] $< 2.7 \times 10^{-5}$ CL=90%		—
$K^+ \rightarrow \mu^+ \nu_\mu \gamma (\text{SD}^- + \text{SD}^- \text{INT})$	[c,g] $< 2.6 \times 10^{-4}$ CL=90%		—
$K^+ \rightarrow e^+ \nu_e \gamma$	$(9.4 \pm 0.4) \times 10^{-6}$		247
$K^+ \rightarrow \pi^0 e^+ \nu_e \gamma$	[e,f] $(2.56 \pm 0.16) \times 10^{-4}$		228
$K^+ \rightarrow \pi^0 e^+ \nu_e \gamma (\text{SD})$	[c,g] $< 5.3 \times 10^{-5}$ CL=90%		228
$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \gamma$	[e,f] $(1.5 \pm 0.4) \times 10^{-5}$		215
$K^+ \rightarrow \pi^0 \pi^0 e^+ \nu_e \gamma$	$< 5 \times 10^{-6}$ CL=90%		206

**Hadronic modes with photons or  $\ell\bar{\ell}$  pairs**

$K^+ \rightarrow \pi^+ \pi^0 \gamma$	[e,f]	( 2.75 $\pm$ 0.15 ) $\times 10^{-4}$	205
$K^+ \rightarrow \pi^+ \pi^0 \gamma$ (DE)	[e,h]	( 4.3 $\pm$ 0.7 ) $\times 10^{-6}$	205
$K^+ \rightarrow \pi^+ \pi^0 \pi^0 \gamma$	[e,f]	( 7.6 $\pm$ 6.0 ) $\times 10^{-6}$	133
$K^+ \rightarrow \pi^+ \pi^+ \pi^- \gamma$	[e,f]	( 1.04 $\pm$ 0.31 ) $\times 10^{-4}$	125
$K^+ \rightarrow \pi^+ \gamma\gamma$	[e]	( 1.10 $\pm$ 0.32 ) $\times 10^{-6}$	227
$K^+ \rightarrow \pi^+ 3\gamma$	[e]	< 1.0 $\times 10^{-4}$ CL=90%	227
$K^\pm \rightarrow \pi^\pm e^+ e^- \gamma$		( 1.19 $\pm$ 0.13 ) $\times 10^{-8}$	227

**Leptonic modes with  $\ell\bar{\ell}$  pairs**

$K^+ \rightarrow e^+ \nu_e \nu \bar{\nu}$		< 6 $\times 10^{-5}$ CL=90%	247
$K^+ \rightarrow \mu^+ \nu_\mu \nu \bar{\nu}$		< 6.0 $\times 10^{-6}$ CL=90%	236
$K^+ \rightarrow e^+ \nu_e e^+ e^-$		( 2.48 $\pm$ 0.20 ) $\times 10^{-8}$	247
$K^+ \rightarrow \mu^+ \nu_\mu e^+ e^-$		( 7.06 $\pm$ 0.31 ) $\times 10^{-8}$	236
$K^+ \rightarrow e^+ \nu_e \mu^+ \mu^-$		( 1.7 $\pm$ 0.5 ) $\times 10^{-8}$	223
$K^+ \rightarrow \mu^+ \nu_\mu \mu^+ \mu^-$		< 4.1 $\times 10^{-7}$ CL=90%	185

**Lepton Family number (*LF*), Lepton number (*L*),  $\Delta S = \Delta Q$  (*SQ*)  
violating modes, or  $\Delta S = 1$  weak neutral current (*S1*) modes**

$K^+ \rightarrow \pi^+ \pi^+ e^- \bar{\nu}_e$	SQ	< 1.2 $\times 10^{-8}$ CL=90%	203
$K^+ \rightarrow \pi^+ \pi^+ \mu^- \bar{\nu}_\mu$	SQ	< 3.0 $\times 10^{-6}$ CL=95%	151
$K^+ \rightarrow \pi^+ e^+ e^-$	S1	( 3.00 $\pm$ 0.09 ) $\times 10^{-7}$	227
$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	S1	( 8.1 $\pm$ 1.4 ) $\times 10^{-8}$ S=2.7	172
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	S1	( 1.7 $\pm$ 1.1 ) $\times 10^{-10}$	227
$K^+ \rightarrow \pi^+ \pi^0 \nu \bar{\nu}$	S1	< 4.3 $\times 10^{-5}$ CL=90%	205
$K^+ \rightarrow \mu^- \nu e^+ e^+$	LF	< 2.0 $\times 10^{-8}$ CL=90%	236
$K^+ \rightarrow \mu^+ \nu_e$	LF	[i] < 4 $\times 10^{-3}$ CL=90%	236
$K^+ \rightarrow \pi^+ \mu^+ e^-$	LF	< 1.3 $\times 10^{-11}$ CL=90%	214
$K^+ \rightarrow \pi^+ \mu^- e^+$	LF	< 5.2 $\times 10^{-10}$ CL=90%	214
$K^+ \rightarrow \pi^- \mu^+ e^+$	L	< 5.0 $\times 10^{-10}$ CL=90%	214
$K^+ \rightarrow \pi^- e^+ e^+$	L	< 6.4 $\times 10^{-10}$ CL=90%	227
$K^+ \rightarrow \pi^- \mu^+ \mu^+$	L	[i] < 3.0 $\times 10^{-9}$ CL=90%	172
$K^+ \rightarrow \mu^+ \bar{\nu}_e$	L	[i] < 3.3 $\times 10^{-3}$ CL=90%	236
$K^+ \rightarrow \pi^0 e^+ \bar{\nu}_e$	L	< 3 $\times 10^{-3}$ CL=90%	228
$K^+ \rightarrow \pi^+ \gamma$	[j]	< 2.3 $\times 10^{-9}$ CL=90%	227

 **$K^0$**  $I(J^P) = \frac{1}{2}(0^-)$ 50%  $K_S$ , 50%  $K_L$ Mass  $m = 497.614 \pm 0.024$  MeV ( $S = 1.6$ ) $m_{K^0} - m_{K^\pm} = 3.937 \pm 0.028$  MeV ( $S = 1.8$ )**Mean Square Charge Radius**

$$\langle r^2 \rangle = -0.077 \pm 0.010 \text{ fm}^2$$

### **T-violation parameters in $K^0$ - $\bar{K}^0$ mixing [d]**

Asymmetry  $A_T$  in  $K^0$ - $\bar{K}^0$  mixing =  $(6.6 \pm 1.6) \times 10^{-3}$

### **CPT-violation parameters [d]**

$\text{Re } \delta = (2.3 \pm 2.7) \times 10^{-4}$

$\text{Im } \delta = (0.4 \pm 2.1) \times 10^{-5}$

$\text{Re}(y)$ ,  $K_{e3}$  parameter =  $(0.4 \pm 2.5) \times 10^{-3}$

$\text{Re}(x_-)$ ,  $K_{e3}$  parameter =  $(-2.9 \pm 2.0) \times 10^{-3}$

$|m_{K^0} - m_{\bar{K}^0}| / m_{\text{average}} < 8 \times 10^{-19}$ , CL = 90% [k]

$(\Gamma_{K^0} - \Gamma_{\bar{K}^0})/m_{\text{average}} = (8 \pm 8) \times 10^{-18}$

### **Tests of $\Delta S = \Delta Q$**

$\text{Re}(x_+)$ ,  $K_{e3}$  parameter =  $(-0.9 \pm 3.0) \times 10^{-3}$

---

**$K_S^0$**

$I(J^P) = \frac{1}{2}(0^-)$

Mean life  $\tau = (0.8953 \pm 0.0005) \times 10^{-10}$  s ( $S = 1.1$ ) Assuming CPT

Mean life  $\tau = (0.8958 \pm 0.0005) \times 10^{-10}$  s Not assuming CPT  
 $c\tau = 2.6842$  cm Assuming CPT

### **CP-violation parameters [l]**

$\text{Im}(\eta_{+-0}) = -0.002 \pm 0.009$

$\text{Im}(\eta_{000}) = (-0.1 \pm 1.6) \times 10^{-2}$

$|\eta_{000}| = |A(K_S^0 \rightarrow 3\pi^0)/A(K_L^0 \rightarrow 3\pi^0)| < 0.018$ , CL = 90%

CP asymmetry  $A$  in  $\pi^+\pi^-e^+e^- = (-1 \pm 4)\%$

<b><math>K_S^0</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	<i>p</i> (MeV/c)
---------------------------------------	--------------------------------	-----------------------------------	---------------------

#### **Hadronic modes**

$\pi^0\pi^0$	$(30.69 \pm 0.05) \%$	209
$\pi^+\pi^-$	$(69.20 \pm 0.05) \%$	206
$\pi^+\pi^-\pi^0$	$(3.5 \pm 1.1) \times 10^{-7}$	133

#### **Modes with photons or $\ell\bar{\ell}$ pairs**

$\pi^+\pi^-\gamma$	$[f,m] \quad (1.79 \pm 0.05) \times 10^{-3}$	206
$\pi^+\pi^-e^+e^-$	$(4.69 \pm 0.30) \times 10^{-5}$	206
$\pi^0\gamma\gamma$	$[m] \quad (4.9 \pm 1.8) \times 10^{-8}$	231
$\gamma\gamma$	$(2.63 \pm 0.17) \times 10^{-6}$	S=3.0

#### **Semileptonic modes**

$\pi^\pm e^\mp\nu_e$	$[n] \quad (7.04 \pm 0.08) \times 10^{-4}$	229
----------------------	--	-----

### **$CP$ violating ( $CP$ ) and $\Delta S = 1$ weak neutral current ( $S1$ ) modes**

$3\pi^0$	$CP$	$< 1.2$	$\times 10^{-7}$	CL=90%	139
$\mu^+ \mu^-$	$S1$	$< 3.2$	$\times 10^{-7}$	CL=90%	225
$e^+ e^-$	$S1$	$< 9$	$\times 10^{-9}$	CL=90%	249
$\pi^0 e^+ e^-$	$S1$	[m] $(3.0 \pm 1.5)$	$\times 10^{-9}$		230
$\pi^0 \mu^+ \mu^-$	$S1$	$(2.9 \pm 1.5)$	$\times 10^{-9}$		177

**$K_L^0$**

$$I(J^P) = \frac{1}{2}(0^-)$$

$$\begin{aligned} m_{K_L} - m_{K_S} &= (0.5292 \pm 0.0009) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad (S = 1.2) \quad \text{Assuming } CPT \\ &= (3.483 \pm 0.006) \times 10^{-12} \text{ MeV} \quad \text{Assuming } CPT \\ &= (0.5290 \pm 0.0015) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad (S = 1.1) \quad \text{Not assuming } \\ &\qquad CPT \\ \text{Mean life } \tau &= (5.116 \pm 0.020) \times 10^{-8} \text{ s} \\ c\tau &= 15.34 \text{ m} \end{aligned}$$

### **Slope parameter $g$ [b]**

(See Particle Listings for quadratic coefficients)

$$K_L^0 \rightarrow \pi^+ \pi^- \pi^0: g = 0.678 \pm 0.008 \quad (S = 1.5)$$

### **$K_L$ decay form factors [d]**

Linear parametrization assuming  $\mu$ -e universality

$$\begin{aligned} \lambda_+(K_{\mu 3}^0) &= \lambda_+(K_{e3}^0) = (2.82 \pm 0.04) \times 10^{-2} \quad (S = 1.1) \\ \lambda_0(K_{\mu 3}^0) &= (1.38 \pm 0.18) \times 10^{-2} \quad (S = 2.2) \end{aligned}$$

Quadratic parametrization assuming  $\mu$ -e universality

$$\begin{aligned} \lambda'_+(K_{\mu 3}^0) &= \lambda'_+(K_{e3}^0) = (2.40 \pm 0.12) \times 10^{-2} \quad (S = 1.2) \\ \lambda''_+(K_{\mu 3}^0) &= \lambda''_+(K_{e3}^0) = (0.20 \pm 0.05) \times 10^{-2} \quad (S = 1.2) \\ \lambda_0(K_{\mu 3}^0) &= (1.16 \pm 0.09) \times 10^{-2} \quad (S = 1.2) \end{aligned}$$

Pole parametrization assuming  $\mu$ -e universality

$$M_V^\mu (K_{\mu 3}^0) = M_V^e (K_{e3}^0) = 878 \pm 6 \text{ MeV} \quad (S = 1.1)$$

$$M_S^\mu (K_{\mu 3}^0) = 1252 \pm 90 \text{ MeV} \quad (S = 2.6)$$

$$K_{e3}^0 \quad |f_S/f_+| = (1.5 \pm 1.4) \times 10^{-2}$$

$$K_{e3}^0 \quad |f_T/f_+| = (5 \pm 4) \times 10^{-2}$$

$$K_{\mu 3}^0 \quad |f_T/f_+| = (12 \pm 12) \times 10^{-2}$$

$$\begin{aligned}
 K_L &\rightarrow \ell^+ \ell^- \gamma, K_L \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{K^*} = -0.205 \pm 0.022 \quad (S = 1.8) \\
 K_L^0 &\rightarrow \ell^+ \ell^- \gamma, K_L^0 \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{DIP} = -1.69 \pm 0.08 \quad (S = 1.7) \\
 K_L &\rightarrow \pi^+ \pi^- e^+ e^-: a_1/a_2 = -0.737 \pm 0.014 \text{ GeV}^2 \\
 K_L &\rightarrow \pi^0 2\gamma: \quad a_V = -0.43 \pm 0.06 \quad (S = 1.5)
 \end{aligned}$$

### **CP-violation parameters [1]**

$$\begin{aligned}
 A_L &= (0.332 \pm 0.006)\% \\
 |\eta_{00}| &= (2.221 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\
 |\eta_{+-}| &= (2.232 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\
 |\epsilon| &= (2.228 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\
 |\eta_{00}/\eta_{+-}| &= 0.9951 \pm 0.0008 [\circ] \quad (S = 1.6) \\
 \text{Re}(\epsilon'/\epsilon) &= (1.65 \pm 0.26) \times 10^{-3} [\circ] \quad (S = 1.6)
 \end{aligned}$$

#### Assuming CPT

$$\begin{aligned}
 \phi_{+-} &= (43.51 \pm 0.05)^\circ \quad (S = 1.1) \\
 \phi_{00} &= (43.52 \pm 0.05)^\circ \quad (S = 1.1) \\
 \phi_\epsilon = \phi_{SW} &= (43.51 \pm 0.05)^\circ \quad (S = 1.1)
 \end{aligned}$$

#### Not assuming CPT

$$\begin{aligned}
 \phi_{+-} &= (43.4 \pm 0.7)^\circ \quad (S = 1.3) \\
 \phi_{00} &= (43.7 \pm 0.8)^\circ \quad (S = 1.2) \\
 \phi_\epsilon &= (43.5 \pm 0.7)^\circ \quad (S = 1.3)
 \end{aligned}$$

CP asymmetry  $A$  in  $K_L^0 \rightarrow \pi^+ \pi^- e^+ e^- = (13.7 \pm 1.5)\%$

$\beta_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = -0.19 \pm 0.07$

$\gamma_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = 0.01 \pm 0.11 \quad (S = 1.6)$

$j$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.0012 \pm 0.0008$

$f$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.004 \pm 0.006$

$|\eta_{+-\gamma}| = (2.35 \pm 0.07) \times 10^{-3}$

$\phi_{+-\gamma} = (44 \pm 4)^\circ$

$|\epsilon'_{+-\gamma}|/\epsilon < 0.3$ , CL = 90%

$|g_{E1}|$  for  $K_L^0 \rightarrow \pi^+ \pi^- \gamma < 0.21$ , CL = 90%

### **T-violation parameters**

$$\text{Im}(\xi) \text{ in } K_{\mu 3}^0 = -0.007 \pm 0.026$$

### ***CPT* invariance tests**

$$\phi_{00} - \phi_{+-} = (0.2 \pm 0.4)^\circ$$

$$\text{Re}(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}) - \frac{A_L}{2} = (-3 \pm 35) \times 10^{-6}$$

### **$\Delta S = -\Delta Q$ in $K_{e3}^0$ decay**

$$\text{Re } x = -0.002 \pm 0.006$$

$$\text{Im } x = 0.0012 \pm 0.0021$$

$K_L^0$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	<i>p</i> (MeV/c)
---------------------	--------------------------------	-----------------------------------	---------------------

#### **Semileptonic modes**

$\pi^\pm e^\mp \nu_e$ Called $K_{e3}^0$ .	[n] (40.55 $\pm 0.12$ ) %	S=1.9	229
$\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[n] (27.04 $\pm 0.07$ ) %	S=1.1	216
$(\pi \mu \text{atom}) \nu$	( 1.05 $\pm 0.11$ ) $\times 10^{-7}$		188
$\pi^0 \pi^\pm e^\mp \nu$	[n] ( 5.20 $\pm 0.11$ ) $\times 10^{-5}$		207
$\pi^\pm e^\mp \nu e^+ e^-$	[n] ( 1.26 $\pm 0.04$ ) $\times 10^{-5}$		229

#### **Hadronic modes, including Charge conjugation×Parity Violating (CPV) modes**

$3\pi^0$	(19.52 $\pm 0.12$ ) %	S=1.7	139
$\pi^+ \pi^- \pi^0$	(12.54 $\pm 0.05$ ) %		133
$\pi^+ \pi^-$	CPV [p] ( 1.966 $\pm 0.010$ ) $\times 10^{-3}$	S=1.6	206
$\pi^0 \pi^0$	CPV ( 8.65 $\pm 0.06$ ) $\times 10^{-4}$	S=1.8	209

#### **Semileptonic modes with photons**

$\pi^\pm e^\mp \nu_e \gamma$	[f,n,q] ( 3.79 $\pm 0.06$ ) $\times 10^{-3}$		229
$\pi^\pm \mu^\mp \nu_\mu \gamma$	( 5.65 $\pm 0.23$ ) $\times 10^{-4}$		216

#### **Hadronic modes with photons or $\ell\bar{\ell}$ pairs**

$\pi^0 \pi^0 \gamma$	< 2.43 $\times 10^{-7}$	CL=90%	209
$\pi^+ \pi^- \gamma$	[f,q] ( 4.15 $\pm 0.15$ ) $\times 10^{-5}$	S=2.8	206
$\pi^+ \pi^- \gamma$ (DE)	( 2.84 $\pm 0.11$ ) $\times 10^{-5}$	S=2.0	206
$\pi^0 2\gamma$	[q] ( 1.273 $\pm 0.034$ ) $\times 10^{-6}$		231
$\pi^0 \gamma e^+ e^-$	( 1.62 $\pm 0.17$ ) $\times 10^{-8}$		230

#### **Other modes with photons or $\ell\bar{\ell}$ pairs**

$2\gamma$	( 5.47 $\pm 0.04$ ) $\times 10^{-4}$	S=1.2	249
$3\gamma$	< 2.4 $\times 10^{-7}$	CL=90%	249
$e^+ e^- \gamma$	( 9.4 $\pm 0.4$ ) $\times 10^{-6}$	S=2.0	249
$\mu^+ \mu^- \gamma$	( 3.59 $\pm 0.11$ ) $\times 10^{-7}$	S=1.3	225
$e^+ e^- \gamma\gamma$	[q] ( 5.95 $\pm 0.33$ ) $\times 10^{-7}$		249
$\mu^+ \mu^- \gamma\gamma$	[q] ( 1.0 $\begin{array}{l} +0.8 \\ -0.6 \end{array}$ ) $\times 10^{-8}$		225

**Charge conjugation  $\times$  Parity ( $CP$ ) or Lepton Family number ( $LF$ )  
violating modes, or  $\Delta S = 1$  weak neutral current ( $S1$ ) modes**

$\mu^+ \mu^-$	$S1$	$( 6.84 \pm 0.11 ) \times 10^{-9}$	225
$e^+ e^-$	$S1$	$( 9 \quad {}^{+6}_{-4} ) \times 10^{-12}$	249
$\pi^+ \pi^- e^+ e^-$	$S1$	$[q] \quad ( 3.11 \pm 0.19 ) \times 10^{-7}$	206
$\pi^0 \pi^0 e^+ e^-$	$S1$	$< 6.6 \times 10^{-9}$ CL=90%	209
$\mu^+ \mu^- e^+ e^-$	$S1$	$( 2.69 \pm 0.27 ) \times 10^{-9}$	225
$e^+ e^- e^+ e^-$	$S1$	$( 3.56 \pm 0.21 ) \times 10^{-8}$	249
$\pi^0 \mu^+ \mu^-$	$CP, S1$	$[r] < 3.8 \times 10^{-10}$ CL=90%	177
$\pi^0 e^+ e^-$	$CP, S1$	$[r] < 2.8 \times 10^{-10}$ CL=90%	230
$\pi^0 \nu \bar{\nu}$	$CP, S1$	$[s] < 6.7 \times 10^{-8}$ CL=90%	231
$\pi^0 \pi^0 \nu \bar{\nu}$	$S1$	$< 4.7 \times 10^{-5}$ CL=90%	209
$e^\pm \mu^\mp$	$LF$	$[n] < 4.7 \times 10^{-12}$ CL=90%	238
$e^\pm e^\pm \mu^\mp \mu^\mp$	$LF$	$[n] < 4.12 \times 10^{-11}$ CL=90%	225
$\pi^0 \mu^\pm e^\mp$	$LF$	$[n] < 7.6 \times 10^{-11}$ CL=90%	217
$\pi^0 \pi^0 \mu^\pm e^\mp$	$LF$	$< 1.7 \times 10^{-10}$ CL=90%	159

 **$K^*(892)$** 

$$I(J^P) = \frac{1}{2}(1^-)$$

$K^*(892)^\pm$  mass  $m = 891.66 \pm 0.26$  MeV

Mass  $m = 895.5 \pm 0.8$  MeV

$K^*(892)^0$  mass  $m = 895.94 \pm 0.22$  MeV (S = 1.4)

$K^*(892)^\pm$  full width  $\Gamma = 50.8 \pm 0.9$  MeV

Full width  $\Gamma = 46.2 \pm 1.3$  MeV

$K^*(892)^0$  full width  $\Gamma = 48.7 \pm 0.8$  MeV (S = 1.7)

<b><math>K^*(892)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$	Confidence level (MeV/c)
$K\pi$	$\sim 100$	%	289
$K^0 \gamma$	$( 2.39 \pm 0.21 ) \times 10^{-3}$		307
$K^\pm \gamma$	$( 9.9 \pm 0.9 ) \times 10^{-4}$		309
$K\pi\pi$	$< 7 \times 10^{-4}$	95%	223

 **$K_1(1270)$** 

$$I(J^P) = \frac{1}{2}(1^+)$$

Mass  $m = 1272 \pm 7$  MeV [t]

Full width  $\Gamma = 90 \pm 20$  MeV [t]

<b><math>K_1(1270)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\rho$	(42 $\pm$ 6) %	45
$K_0^*(1430)\pi$	(28 $\pm$ 4) %	†
$K^*(892)\pi$	(16 $\pm$ 5) %	302
$K\omega$	(11.0 $\pm$ 2.0) %	†
$Kf_0(1370)$	( 3.0 $\pm$ 2.0) %	†
$\gamma K^0$	seen	539

### **$K_1(1400)$**

$$I(J^P) = \frac{1}{2}(1^+)$$

Mass  $m = 1403 \pm 7$  MeV

Full width  $\Gamma = 174 \pm 13$  MeV (S = 1.6)

<b><math>K_1(1400)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K^*(892)\pi$	(94 $\pm$ 6) %	402
$K\rho$	( 1.2 $\pm$ 0.6) %	292
$Kf_0(1370)$	( 2.0 $\pm$ 2.0) %	†
$K\omega$	( 1.0 $\pm$ 1.0) %	284
$K_0^*(1430)\pi$	not seen	†
$\gamma K^0$	seen	613

### **$K^*(1410)$**

$$I(J^P) = \frac{1}{2}(1^-)$$

Mass  $m = 1414 \pm 15$  MeV (S = 1.3)

Full width  $\Gamma = 232 \pm 21$  MeV (S = 1.1)

<b><math>K^*(1410)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K^*(892)\pi$	> 40 %	95%	410
$K\pi$	( 6.6 $\pm$ 1.3) %		612
$K\rho$	< 7 %	95%	305
$\gamma K^0$	seen		619

### **$K_0^*(1430)$ [u]**

$$I(J^P) = \frac{1}{2}(0^+)$$

Mass  $m = 1425 \pm 50$  MeV

Full width  $\Gamma = 270 \pm 80$  MeV

<b><math>K_0^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(93±10) %	619

**$K_2^*(1430)$**   $I(J^P) = \frac{1}{2}(2^+)$

$K_2^*(1430)^{\pm}$  mass  $m = 1425.6 \pm 1.5$  MeV ( $S = 1.1$ )

$K_2^*(1430)^0$  mass  $m = 1432.4 \pm 1.3$  MeV

$K_2^*(1430)^{\pm}$  full width  $\Gamma = 98.5 \pm 2.7$  MeV ( $S = 1.1$ )

$K_2^*(1430)^0$  full width  $\Gamma = 109 \pm 5$  MeV ( $S = 1.9$ )

<b><math>K_2^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
$K\pi$	(49.9±1.2) %		619
$K^*(892)\pi$	(24.7±1.5) %		419
$K^*(892)\pi\pi$	(13.4±2.2) %		372
$K\rho$	( 8.7±0.8) %	$S=1.2$	318
$K\omega$	( 2.9±0.8) %		311
$K^+\gamma$	( 2.4±0.5) $\times 10^{-3}$	$S=1.1$	627
$K\eta$	( 1.5 $^{+3.4}_{-1.0}$ ) $\times 10^{-3}$	$S=1.3$	486
$K\omega\pi$	< 7.2 $\times 10^{-4}$	CL=95%	100
$K^0\gamma$	< 9 $\times 10^{-4}$	CL=90%	626

**$K^*(1680)$**   $I(J^P) = \frac{1}{2}(1^-)$

Mass  $m = 1717 \pm 27$  MeV ( $S = 1.4$ )

Full width  $\Gamma = 322 \pm 110$  MeV ( $S = 4.2$ )

<b><math>K^*(1680)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(38.7±2.5) %	781
$K\rho$	(31.4 $^{+5.0}_{-2.1}$ ) %	570
$K^*(892)\pi$	(29.9 $^{+2.2}_{-5.0}$ ) %	618

**$K_2(1770)$  [v]**  $I(J^P) = \frac{1}{2}(2^-)$

Mass  $m = 1773 \pm 8$  MeV

Full width  $\Gamma = 186 \pm 14$  MeV

<b><math>K_2(1770)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi\pi$		794
$K_2^*(1430)\pi$	dominant	288
$K^*(892)\pi$	seen	654
$Kf_2(1270)$	seen	55
$K\phi$	seen	441
$K\omega$	seen	607

### **$K_3^*(1780)$**

$$I(J^P) = \frac{1}{2}(3^-)$$

Mass  $m = 1776 \pm 7$  MeV ( $S = 1.1$ )

Full width  $\Gamma = 159 \pm 21$  MeV ( $S = 1.3$ )

<b><math>K_3^*(1780)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K\rho$	(31 $\pm$ 9) %		613
$K^*(892)\pi$	(20 $\pm$ 5) %		656
$K\pi$	(18.8 $\pm$ 1.0) %		813
$K\eta$	(30 $\pm$ 13) %		719
$K_2^*(1430)\pi$	< 16 %	95%	291

### **$K_2(1820)$ [w]**

$$I(J^P) = \frac{1}{2}(2^-)$$

Mass  $m = 1816 \pm 13$  MeV

Full width  $\Gamma = 276 \pm 35$  MeV

<b><math>K_2(1820)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K_2^*(1430)\pi$	seen	327
$K^*(892)\pi$	seen	681
$Kf_2(1270)$	seen	186
$K\omega$	seen	638

### **$K_4^*(2045)$**

$$I(J^P) = \frac{1}{2}(4^+)$$

Mass  $m = 2045 \pm 9$  MeV ( $S = 1.1$ )

Full width  $\Gamma = 198 \pm 30$  MeV

<b><math>K_4^*(2045)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(9.9±1.2) %	958
$K^*(892)\pi\pi$	(9 ± 5) %	802
$K^*(892)\pi\pi\pi$	(7 ± 5) %	768
$\rho K\pi$	(5.7±3.2) %	741
$\omega K\pi$	(5.0±3.0) %	738
$\phi K\pi$	(2.8±1.4) %	594
$\phi K^*(892)$	(1.4±0.7) %	363

## NOTES

[a] See the note in the  $K^\pm$  Particle Listings.

[b] The definition of the slope parameter  $g$  of the  $K \rightarrow 3\pi$  Dalitz plot is as follows (see also “Note on Dalitz Plot Parameters for  $K \rightarrow 3\pi$  Decays” in the  $K^\pm$  Particle Listings):

$$|M|^2 = 1 + g(s_3 - s_0)/m_{\pi^+}^2 + \dots$$

[c] See the “Note on  $\pi^\pm \rightarrow \ell^\pm \nu \gamma$  and  $K^\pm \rightarrow \ell^\pm \nu \gamma$  Form Factors” in the  $\pi^\pm$  Particle Listings for definitions and details.

[d] For more details and definitions of parameters see the Particle Listings.

[e] See the  $K^\pm$  Particle Listings for the energy limits used in this measurement.

[f] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ 's.

[g] Structure-dependent part.

[h] Direct-emission branching fraction.

[i] Derived from an analysis of neutrino-oscillation experiments.

[j] Violates angular-momentum conservation.

[k] Derived from measured values of  $\phi_{+-}$ ,  $\phi_{00}$ ,  $|\eta|$ ,  $|m_{K_L^0} - m_{K_S^0}|$ , and  $\tau_{K_S^0}$ , as described in the introduction to “Tests of Conservation Laws.”

[l] The  $CP$ -violation parameters are defined as follows (see also “Note on  $CP$  Violation in  $K_S \rightarrow 3\pi$ ” and “Note on  $CP$  Violation in  $K_L^0$  Decay” in the Particle Listings):

$$\eta_{+-} = |\eta_{+-}| e^{i\phi_{+-}} = \frac{A(K_L^0 \rightarrow \pi^+ \pi^-)}{A(K_S^0 \rightarrow \pi^+ \pi^-)} = \epsilon + \epsilon'$$

$$\eta_{00} = |\eta_{00}| e^{i\phi_{00}} = \frac{A(K_L^0 \rightarrow \pi^0 \pi^0)}{A(K_S^0 \rightarrow \pi^0 \pi^0)} = \epsilon - 2\epsilon'$$

$$\delta = \frac{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) - \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)}{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) + \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)},$$

$$\text{Im}(\eta_{+-0})^2 = \frac{\Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0)^{\text{CP viol.}}}{\Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)},$$

$$\text{Im}(\eta_{000})^2 = \frac{\Gamma(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0)}{\Gamma(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0)}.$$

where for the last two relations *CPT* is assumed valid, *i.e.*,  $\text{Re}(\eta_{+-0}) \simeq 0$  and  $\text{Re}(\eta_{000}) \simeq 0$ .

- [m] See the  $K_S^0$  Particle Listings for the energy limits used in this measurement.
- [n] The value is for the sum of the charge states or particle/antiparticle states indicated.
- [o]  $\text{Re}(\epsilon'/\epsilon) = \epsilon'/\epsilon$  to a very good approximation provided the phases satisfy *CPT* invariance.
- [p] This mode includes gammas from inner bremsstrahlung but not the direct emission mode  $K_L^0 \rightarrow \pi^+ \pi^- \gamma$ (DE).
- [q] See the  $K_L^0$  Particle Listings for the energy limits used in this measurement.
- [r] Allowed by higher-order electroweak interactions.
- [s] Violates *CP* in leading order. Test of direct *CP* violation since the indirect *CP*-violating and *CP*-conserving contributions are expected to be suppressed.
- [t] This is only an educated guess; the error given is larger than the error on the average of the published values. See the Particle Listings for details.
- [u] See the “Note on  $f_0(1370)$ ” in the  $f_0(1370)$  Particle Listings and in the 1994 edition.
- [v] See the note in the  $L(1770)$  Particle Listings in Reviews of Modern Physics **56** S1 (1984), p. S200. See also the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .
- [w] See the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .