

POLARIZATION IN B DECAYS

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We review the notation used in polarization measurements in particle production and decay, with a particular emphasis on the B decays and the CP -violating observables in polarization measurements. We look at several examples of vector-vector and vector-tensor B meson decays, while more details about the theory and experimental results in B decays can be found in a separate mini-review [1] in this *Review*.

Figure 1 illustrates angular observables in an example of the sequential process $ab \rightarrow X \rightarrow P_1 P_2 \rightarrow (p_{11} p_{12})(p_{21} p_{22})$ [2]. The angular distributions are of particular interest because they are sensitive to spin correlations and reveal properties of particles and their interactions, such as quantum numbers and couplings. In the case of a spin-zero particle X , such as B meson or a Higgs boson, there are no spin correlations in the production mechanism and the decay chain is to be analyzed. The angular distribution of decay products can be expressed as a function of three helicity angles which describe the alignment of the particles in the decay chain. The analyzer of the B -daughter polarization is normally chosen for two-body decays, as the direction of the daughters in the center-of-mass of the parent (*e.g.*, $\rho \rightarrow 2\pi$) [3], and for three-body decays as the normal to the decay plane (*e.g.*, $\omega \rightarrow 3\pi$) [4]. An equivalent set of transversity angles is sometimes used in polarization analyses [5]. The differential decay width depends on complex amplitudes $A_{\lambda_1 \lambda_2}$, corresponding to the X -daughter helicity states λ_i .

In the case of a spin-zero B -meson decay, its daughter helicities are constrained to $\lambda_1 = \lambda_2 = \lambda$. Therefore we simplify amplitude notation as A_λ . Moreover, most B -decay polarization analyses are limited to the case when the spin of one of the B -meson daughters is 1. In that case, there are only three independent amplitudes corresponding to $\lambda = 0$ or ± 1 [6], where the last two can be expressed in terms of parity-even and parity-odd amplitudes $A_{\parallel, \perp} = (A_{+1} \pm A_{-1})/\sqrt{2}$. The overall decay amplitude involves three complex terms proportional to

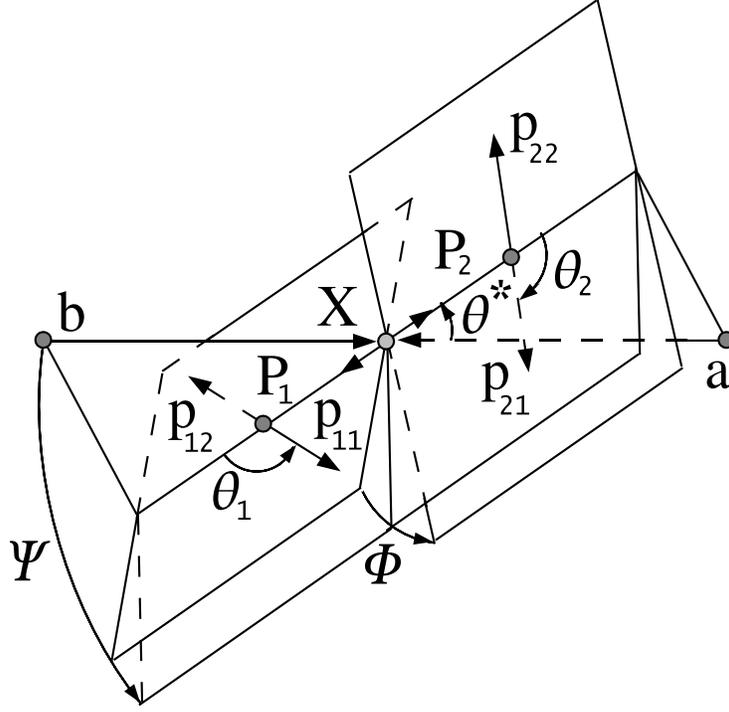


Figure 1: Definition of the production and helicity angles in the sequential process $ab \rightarrow X \rightarrow P_1 P_2 \rightarrow (p_{11} p_{12})(p_{21} p_{22})$. The three helicity angles include θ_1 and θ_2 , defined in the rest frame of the two daughters P_1 and P_2 , and Φ , defined in the X frame as the angle between the two decay planes. The two production angles θ^* and Ψ are defined in the X frame, where Ψ is the angle between the production plane and the average of the two decay planes.

the above amplitudes and the Wigner d functions of helicity angles. The exact angular dependence would depend on the quantum numbers of the B -meson daughters and of their decay products, and can be found in the literature [6,7]. The differential decay rate would involve six real quantities α_i , including interference terms,

$$\frac{d\Gamma}{\Gamma d \cos \theta_1 d \cos \theta_2 d \Phi} = \sum_i \alpha_i f_i(\cos \theta_1, \cos \theta_2, \Phi), \quad (1)$$

where each $f_i(\cos \theta_1, \cos \theta_2, \Phi)$ has unique angular dependence specific to particle quantum numbers, and the α_i parameters

are defined as:

$$\alpha_1 = \frac{|A_0|^2}{\Sigma|A_\lambda|^2} = f_L, \quad (2)$$

$$\alpha_2 = \frac{|A_\parallel|^2 + |A_\perp|^2}{\Sigma|A_\lambda|^2} = (1 - f_L), \quad (3)$$

$$\alpha_3 = \frac{|A_\parallel|^2 - |A_\perp|^2}{\Sigma|A_\lambda|^2} = (1 - f_L - 2f_\perp), \quad (4)$$

$$\alpha_4 = \frac{\Im m(A_\perp A_\parallel^*)}{\Sigma|A_\lambda|^2} = \sqrt{f_\perp(1 - f_L - f_\perp)} \sin(\phi_\perp - \phi_\parallel), \quad (5)$$

$$\alpha_5 = \frac{\Re e(A_\parallel A_0^*)}{\Sigma|A_\lambda|^2} = \sqrt{f_L(1 - f_L - f_\perp)} \cos(\phi_\parallel), \quad (6)$$

$$\alpha_6 = \frac{\Im m(A_\perp A_0^*)}{\Sigma|A_\lambda|^2} = \sqrt{f_\perp f_L} \sin(\phi_\perp), \quad (7)$$

where the amplitudes have been expressed with the help of polarization parameters f_L , f_\perp , ϕ_\parallel , and ϕ_\perp defined in Table 1. Note that the terms proportional to $\Re e(A_\perp A_\parallel^*)$, $\Im m(A_\parallel A_0^*)$, and $\Re e(A_\perp A_0^*)$ are absent in Eqs. (2-7). However, these terms may appear for some three-body decays of a B -meson daughter, see Ref. 7.

Overall, six real parameters describe three complex amplitudes A_0 , A_\parallel , and A_\perp . These could be chosen to be the four polarization parameters f_L , f_\perp , ϕ_\parallel , and ϕ_\perp , one overall size normalization, such as decay rate Γ , or branching fraction \mathcal{B} , and one overall phase δ_0 . The phase convention is arbitrary for an isolated B decay mode. However, for several B decays, the relative phase could produce meaningful and observable effects through interference with other B decays with the same final states, such as for $B \rightarrow VK_J^*$ with $J = 0, 1, 2, 3, 4, \dots$. The phase could be referenced to the single $B \rightarrow VK_0^*$ amplitude A_{00} in such a case, as shown in Table 1. Here V stands for any spin-one vector meson.

Moreover, CP violation can be tested in the angular distribution of the decay as the difference between the B and \bar{B} . Each of the six real parameters describing the three complex amplitudes would have a counterpart CP -asymmetry term, corresponding to three direct- CP asymmetries in three amplitudes, and three CP -violating phase differences, equivalent to the phase measurements from the mixing-induced CP asymmetries

Table 1: Rate, polarization, and CP -asymmetry parameters defined for the B -meson decays to mesons with non-zero spin. Numerical examples are shown for the $B^0 \rightarrow \varphi K^*(892)^0$ decay. The first six parameters are defined under the assumption of no CP violation in decay, while they are averaged between the \bar{B} and B parameters in general. The last six parameters involve differences between the \bar{B} and B meson decay parameters. The phase convention δ_0 is chosen with respect to a single A_{00} amplitude from a reference B decay mode, which is $B^0 \rightarrow \varphi K_0^*(1430)^0$ for numerical results.

| parameter | definition | average |
|--------------------------|---|--------------------------------|
| \mathcal{B} | $\Gamma/\Gamma_{\text{total}}$ | $(9.8 \pm 0.6) \times 10^{-6}$ |
| f_L | $ A_0 ^2/\Sigma A_\lambda ^2$ | 0.480 ± 0.030 |
| f_\perp | $ A_\perp ^2/\Sigma A_\lambda ^2$ | 0.24 ± 0.05 |
| $\phi_\parallel - \pi$ | $\arg(A_\parallel/A_0) - \pi$ | -0.74 ± 0.13 |
| $\phi_\perp - \pi$ | $\arg(A_\perp/A_0) - \pi$ | -0.75 ± 0.13 |
| $\delta_0 - \pi$ | $\arg(A_{00}/A_0) - \pi$ | -0.32 ± 0.17 |
| \mathcal{A}_{CP} | $(\bar{\Gamma} - \Gamma)/(\bar{\Gamma} + \Gamma)$ | $+0.01 \pm 0.05$ |
| \mathcal{A}_{CP}^0 | $(\bar{f}_L - f_L)/(\bar{f}_L + f_L)$ | $+0.04 \pm 0.06$ |
| \mathcal{A}_{CP}^\perp | $(\bar{f}_\perp - f_\perp)/(\bar{f}_\perp + f_\perp)$ | -0.11 ± 0.12 |
| $\Delta\phi_\parallel$ | $(\bar{\phi}_\parallel - \phi_\parallel)/2$ | $+0.11 \pm 0.22$ |
| $\Delta\phi_\perp$ | $(\bar{\phi}_\perp - \phi_\perp - \pi)/2$ | $+0.08 \pm 0.22$ |
| $\Delta\delta_0$ | $(\bar{\delta}_0 - \delta_0)/2$ | $+0.27 \pm 0.16$ |

in the time evolution of B -decays [1]. In Table 1 and Ref. 8, these are chosen to be the direct- CP asymmetries in the overall decay rate \mathcal{A}_{CP} , in the f_L fraction \mathcal{A}_{CP}^0 , and in the f_\perp fraction \mathcal{A}_{CP}^\perp , and three weak phase differences:

$$\Delta\phi_\parallel = \frac{1}{2}\arg(\bar{A}_\parallel A_0/A_\parallel \bar{A}_0), \quad (8)$$

$$\Delta\phi_\perp = \frac{1}{2}\arg(\bar{A}_\perp A_0/A_\perp \bar{A}_0) - \frac{\pi}{2}, \quad (9)$$

$$\Delta\delta_0 = \frac{1}{2}\arg(\bar{A}_{00} A_0/A_{00} \bar{A}_0). \quad (10)$$

The $\frac{\pi}{2}$ term in Eq. (9) reflects the fact that A_{\perp} and \bar{A}_{\perp} differ in phase by π if CP is conserved. The two parameters $\Delta\phi_{\parallel}$ and $\Delta\phi_{\perp}$ are equivalent to triple-product asymmetries constructed from the vectors describing the decay angular distribution [9]. The CP -violating phase difference in the reference decay mode [8] is, in the Wolfenstein CKM quark-mixing phase convention,

$$\Delta\phi_{00} = \frac{1}{2}\arg(A_{00}/\bar{A}_{00}). \quad (11)$$

This can be measured only together with the mixing-induced phase difference for some of the neutral B -meson decays similar to other mixing-induced CP asymmetry measurements [1].

It may not always be possible to have a phase-reference decay mode which would define δ_0 and $\Delta\delta_0$ parameters. In that case, it may be possible to define the phase difference directly similarly to Eq. (11):

$$\Delta\phi_0 = \frac{1}{2}\arg(A_0/\bar{A}_0). \quad (12)$$

One can measure the angles of the CKM unitarity triangle, assuming Standard Model contributions to the $\Delta\phi_0$ and B -mixing phases. Examples include measurements of $\beta = \phi_1$ with $B \rightarrow J/\psi K^*$ and $\alpha = \phi_2$ with $B \rightarrow \rho\rho$.

Most of the B decays that arise from tree-level $b \rightarrow c$ transitions have the amplitude hierarchy $|A_0| > |A_+| > |A_-|$ which is expected from analyses based on quark-helicity conservation [10]. The larger the mass of the vector-meson daughters, the weaker the inequality. The B meson decays to heavy vector particles with charm, such as $B \rightarrow J/\psi K^*$, $\psi(2S)K^*$, $\chi_{c1}K^*$, $D^*\rho$, D^*K^* , D^*D^* , and $D^*D_s^*$, show a substantial fraction of the amplitudes corresponding to transverse polarization of the vector mesons ($A_{\pm 1}$), in agreement with the factorization prediction. The detailed amplitude analysis of the $B \rightarrow J/\psi K^*$ decays has been performed by the BABAR [11], Belle [12], CDF [13], CLEO [14], and D0 [15] collaborations. Most analyses are performed under the assumption of the absence of direct CP violation. The parameter values are given in the particle listing of this *Review*. The difference between the strong

phases ϕ_{\parallel} and ϕ_{\perp} deviates significantly from zero. The recent measurements [11,12] of CP -violating terms similar to those in $B \rightarrow \varphi K^*$ [8] shown in Table 1 are consistent with zero.

In addition, the mixing-induced CP -violating asymmetry is measured in the $B^0 \rightarrow J/\psi K^{*0}$ decay [1,11,12] where angular analysis allows one to separate CP -eigenstate amplitudes. This allows one to resolve the sign ambiguity of the $\cos 2\beta$ ($\cos 2\phi_1$) term that appears in the time-dependent angular distribution due to interference of parity-even and parity-odd terms. This analysis relies on the knowledge of discrete ambiguities in the strong phases ϕ_{\parallel} and ϕ_{\perp} , as discussed below. The BABAR experiment used a method based on the dependence on the $K\pi$ invariant mass of the interference between the S - and P -waves to resolve the discrete ambiguity in the determination of the strong phases ($\phi_{\parallel}, \phi_{\perp}$) in $B \rightarrow J/\psi K^*$ decays [11]. The result is in agreement with the amplitude hierarchy expectation [10]. The CDF [13,16] and D0 [15,17] experiments have studied the $B_s^0 \rightarrow J/\psi \varphi$ decay and provided the lifetime, polarization, and phase measurements.

The amplitude hierarchy $|A_0| \gg |A_+| \gg |A_-|$ was expected in B decays to light vector particles in both penguin transitions [18,19] and tree-level transitions [10]. There is confirmation by the BABAR and BELLE experiments of predominantly longitudinal polarization in the tree-level $b \rightarrow u$ transition, such as $B^0 \rightarrow \rho^+ \rho^-$ [20], $B^+ \rightarrow \rho^0 \rho^+$ [21], and $B^+ \rightarrow \omega \rho^+$ [22]; this is consistent with the analysis of the quark helicity conservation [10]. Because the longitudinal amplitude dominates the decay, a detailed amplitude analysis is not possible with current B samples, and limits on the transverse amplitude fraction are obtained. Only limits have been set for $B^0 \rightarrow \omega \rho^0, \omega \omega$ [22]; there is some evidence for $B^0 \rightarrow \rho^0 \rho^0$ [23] decays. The small values for these branching fractions indicates that $b \rightarrow d$ penguin pollution is small in the charmless, strangeless vector-vector B decays.

The interest in the polarization and CP -asymmetry measurements in penguin transition, such as $b \rightarrow s$ decays $B \rightarrow \varphi K^*, \rho K^*, \omega K^*$, or $B_s^0 \rightarrow \varphi \varphi$, and $b \rightarrow d$ decay $B \rightarrow K^* \bar{K}^*$, is motivated by their potential sensitivity to physics beyond the

Standard Model. The decay amplitudes for $B \rightarrow \varphi K^*$ have been measured by the BABAR and Belle experiments [8,24,25]. The fractions of longitudinal polarization $f_L = 0.50 \pm 0.05$ for the $B^+ \rightarrow \varphi K^{*+}$ decay, and $f_L = 0.48 \pm 0.03$ for the $B^0 \rightarrow \varphi K^{*0}$ decay, indicate significant departure from the naive expectation of predominant longitudinal polarization, and suggest other contributions to the decay amplitude, previously neglected, either within the Standard Model, such as penguin annihilation [27] or QCD rescattering [28], or from physics beyond the Standard Model [29]. The complete set of twelve amplitude parameters measured in the $B^0 \rightarrow \varphi K^{*0}$ decay are given in Table 1. Several other parameters could be constructed from the above twelve parameters, as suggested in Ref. 30.

The discrete ambiguity in the phase $(\phi_{\parallel}, \phi_{\perp}, \Delta\phi_{\parallel}, \Delta\phi_{\perp})$ measurements has been resolved by BABAR in favor of $|A_+| \gg |A_-|$ through interference between the S - and P -waves of $K\pi$. The search for vector-tensor and vector-axialvector $B \rightarrow \varphi K_J^{(*)}$ decays with $J = 1, 2, 3, 4$ revealed a large fraction of longitudinal polarization in the decay $B \rightarrow \varphi K_2^*(1430)$ with $f_L = 0.90_{-0.07}^{+0.06}$ [8,31], but large contribution of transverse amplitude in $B \rightarrow \varphi K_1(1270)$ with $f_L = 0.46_{-0.15}^{+0.13}$ [32].

Like $B \rightarrow \varphi K^*$, the decays $B \rightarrow \rho K^*$ and $B \rightarrow \omega K^*$ may be sensitive to New Physics. Measurements of the longitudinal polarization fraction in $B^+ \rightarrow \rho^0 K^{*0}$, $B^+ \rightarrow \rho^+ K^{*0}$ [33] and in both vector-vector and vector-tensor final states of $B \rightarrow \omega K_J^*$ [22] reveal a large fraction of transverse polarization, indicating an anomaly similar to $B \rightarrow \varphi K^*$ except for different pattern in vector-tensor final states. At the same time, first measurement of the polarization in the $b \rightarrow d$ penguin decays $B \rightarrow K^* \bar{K}^*$ indicates a large fraction of longitudinal polarization [34]. There is also evidence for the $B_s^0 \rightarrow \varphi\varphi$ decay [35]. The polarization pattern in penguin-dominated B -meson decays is not fully understood [27,28,29].

The three-body smilpeptonic B -meson decays, such as $B \rightarrow V l_1 l_2$, share many features with the two-body $B \rightarrow VV$ decays. Their differential decay width can be parameterized with the two helicity angles defined in the V and $(l_1 l_2)$ frames and with the azimuthal angle, as defined in Fig. 1. However, since the

$(l_1 l_2)$ pair does not come from an on-shell particle, the angular distribution is unique to each point in the dilepton mass m_{ll} spectrum. The polarization measurements as a function of m_{ll} provide complementary information on physics beyond the Standard Model, as discussed for $B \rightarrow K^* l^+ l^-$ decay in Ref. 36, though the current data in this mode [37] are not yet sufficient for precise tests.

The examples of the angular distributions and observables in $B \rightarrow K^* l^+ l^-$ are discussed in Ref. 36. With the present statistics only two angular observables have been measured in this decay when integrated over certain ranges of the dilepton mass m_{ll} [37]. One parameter is the fraction of longitudinal polarization F_L , which is determined by the K^* angular distribution and is similar to f_L defined for exclusive two-body decays. The other parameter is the forward-backward asymmetry of the lepton pair A_{FB} , which is the asymmetry of the decay rate with positive and negative values of $\cos \theta_1$.

In summary, there has been considerable recent interest in the polarization measurements of B -meson decays because they reveal both weak- and strong-interaction dynamics [27–29,38]. New measurements will further elucidate the pattern of spin alignment measurements in rare B decays, and further test the Standard Model and strong interaction dynamics, including the non-factorizable contributions to the B -decay amplitudes.

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