## POLARIZATION IN B DECAYS

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We review the notation used in polarization measurements in particle production and decay, with a particular emphasis on the B decays and the CP-violating observables in polarization measurements. We look at several examples of vector-vector and vector-tensor B meson decays, while more details about the theory and experimental results in B decays can be found in a separate mini-review [1] in this *Review*.

Figure 1 illustrates angular observables in an example of the sequential process  $ab \to X \to P_1P_2 \to (p_{11}p_{12})(p_{21}p_{22})$  [2]. The angular distributions are of particular interest because they are sensitive to spin correlations and reveal properties of particles and their interactions, such as quantum numbers and couplings. In the case of a spin-zero particle X, such as Bmeson or a Higgs boson, there are no spin correlations in the production mechanism and the decay chain is to be analyzed. The angular distribution of decay products can be expressed as a function of three helicity angles which describe the alignment of the particles in the decay chain. The analyzer of the Bdaughter polarization is normally chosen for two-body decays, as the direction of the daughters in the center-of-mass of the parent (e.g.,  $\rho \to 2\pi$ ) [3], and for three-body decays as the normal to the decay plane  $(e.g., \omega \to 3\pi)$  [4]. An equivalent set of transversity angles is sometimes used in polarization analyses [5]. The differential decay width depends on complex amplitudes  $A_{\lambda_1\lambda_2}$ , corresponding to the X-daughter helicity states  $\lambda_i$ .

In the case of a spin-zero *B*-meson decay, its daughter helicities are constrained to  $\lambda_1 = \lambda_2 = \lambda$ . Therefore we simplify amplitude notation as  $A_{\lambda}$ . Moreover, most *B*-decay polarization analyses are limited to the case when the spin of one of the *B*-meson daughters is 1. In that case, there are only three independent amplitudes corresponding to  $\lambda = 0$  or  $\pm 1$  [6], where the last two can be expressed in terms of parity-even and parity-odd amplitudes  $A_{\parallel,\perp} = (A_{+1} \pm A_{-1})/\sqrt{2}$ . The overall decay amplitude involves three complex terms proportional to

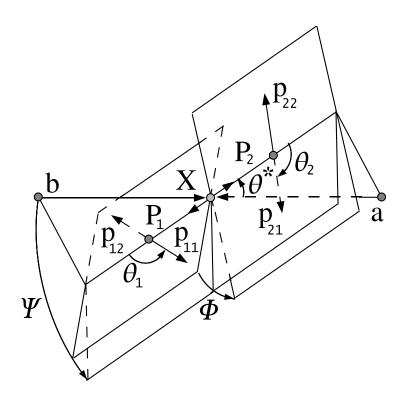


Figure 1: Definition of the production and helicity angles in the sequential process  $ab \rightarrow X \rightarrow P_1P_2 \rightarrow (p_{11}p_{12})(p_{21}p_{22})$ . The three helicity angles include  $\theta_1$  and  $\theta_2$ , defined in the rest frame of the two daughters  $P_1$  and  $P_2$ , and  $\Phi$ , defined in the X frame as the angle between the two decay planes. The two production angles  $\theta^*$ and  $\Psi$  are defined in the X frame, where  $\Psi$  is the angle between the production plane and the average of the two decay planes.

the above amplitudes and the Wigner d functions of helicity angles. The exact angular dependence would depend on the quantum numbers of the *B*-meson daughters and of their decay products, and can be found in the literature [6,7]. The differential decay rate would involve six real quantities  $\alpha_i$ , including interference terms,

$$\frac{d\Gamma}{\Gamma d\cos\theta_1 d\cos\theta_2 d\Phi} = \sum_i \alpha_i \ f_i \left(\cos\theta_1, \,\cos\theta_2, \,\Phi\right), \quad (1)$$

where each  $f_i(\cos\theta_1, \cos\theta_2, \Phi)$  has unique angular dependence specific to particle quantum numbers, and the  $\alpha_i$  parameters are defined as:

$$\alpha_1 = \frac{|A_0|^2}{\Sigma |A_\lambda|^2} = f_L \,, \tag{2}$$

$$\alpha_2 = \frac{|A_{\parallel}|^2 + |A_{\perp}|^2}{\Sigma |A_{\lambda}|^2} = (1 - f_L), \qquad (3)$$

$$\alpha_3 = \frac{|A_{\parallel}|^2 - |A_{\perp}|^2}{\Sigma |A_{\lambda}|^2} = (1 - f_L - 2f_{\perp}), \qquad (4)$$

$$\alpha_4 = \frac{\Im m(A_\perp A_\parallel^*)}{\Sigma |A_\lambda|^2} = \sqrt{f_\perp (1 - f_L - f_\perp)} \sin(\phi_\perp - \phi_\parallel), \quad (5)$$

$$\alpha_5 = \frac{\Re e(A_{\parallel}A_0^*)}{\Sigma |A_{\lambda}|^2} = \sqrt{f_L \left(1 - f_L - f_{\perp}\right)} \cos(\phi_{\parallel}), \qquad (6)$$

$$\alpha_6 = \frac{\Im m(A_\perp A_0^*)}{\Sigma |A_\lambda|^2} = \sqrt{f_\perp f_L} \sin(\phi_\perp) , \qquad (7)$$

where the amplitudes have been expressed with the help of polarization parameters  $f_L$ ,  $f_{\perp}$ ,  $\phi_{\parallel}$ , and  $\phi_{\perp}$  defined in Table 1. Note that the terms proportional to  $\Re e(A_{\perp}A_{\parallel}^*)$ ,  $\Im m(A_{\parallel}A_0^*)$ , and  $\Re e(A_{\perp}A_0^*)$  are absent in Eqs. (2-7). However, these terms may appear for some three-body decays of a *B*-meson daughter, see Ref. 7.

Overall, six real parameters describe three complex amplitudes  $A_0$ ,  $A_{\parallel}$ , and  $A_{\perp}$ . These could be chosen to be the four polarization parameters  $f_L$ ,  $f_{\perp}$ ,  $\phi_{\parallel}$ , and  $\phi_{\perp}$ , one overall size normalization, such as decay rate  $\Gamma$ , or branching fraction  $\mathcal{B}$ , and one overall phase  $\delta_0$ . The phase convention is arbitrary for an isolated B decay mode. However, for several B decays, the relative phase could produce meaningful and observable effects through interference with other B decays with the same final states, such as for  $B \to VK_J^*$  with J = 0, 1, 2, 3, 4, ... The phase could be referenced to the single  $B \to VK_0^*$  amplitude  $A_{00}$ in such a case, as shown in Table 1. Here V stands for any spin-one vector meson.

Moreover, CP violation can be tested in the angular distribution of the decay as the difference between the B and  $\overline{B}$ . Each of the six real parameters describing the three complex amplitudes would have a counterpart CP-asymmetry term, corresponding to three direct-CP asymmetries in three amplitudes, and three CP-violating phase differences, equivalent to the phase measurements from the mixing-induced CP asymmetries

**Table 1:** Rate, polarization, and CP-asymmetry parameters defined for the *B*-meson decays to mesons with non-zero spin. Numerical examples are shown for the  $B^0 \to \varphi K^*(892)^0$  decay. The first six parameters are defined under the assumption of no CP violation in decay, while they are averaged between the  $\overline{B}$  and B parameters in general. The last six parameters involve differences between the  $\overline{B}$  and B meson decay parameters. The phase convention  $\delta_0$ is chosen with respect to a single  $A_{00}$  amplitude from a reference B decay mode, which is  $B^0 \to \varphi K_0^*(1430)^0$  for numerical results.

parameter	definition	average
B	$\Gamma/\Gamma_{\rm total}$	$(9.8 \pm 0.6) \times 10^{-6}$
$f_L$	$ A_0 ^2/\Sigma  A_\lambda ^2$	$0.480 \pm 0.030$
$f_{\perp}$	$ A_{\perp} ^2 / \Sigma  A_{\lambda} ^2$	$0.24\pm0.05$
$\phi_{\parallel}-\pi$	$\arg(A_{\parallel}/A_0) - \pi$	$-0.74\pm0.13$
$\phi_{\perp} - \pi$	$\arg(A_{\perp}/A_0) - \pi$	$-0.75\pm0.13$
$\delta_0 - \pi$	$\arg(A_{00}/A_0) - \pi$	$-0.32\pm0.17$
$A_{CP}$	$(\bar{\Gamma} - \Gamma)/(\bar{\Gamma} + \Gamma)$	$+0.01\pm0.05$
$A^0_{CP}$	$(\bar{f}_L - f_L)/(\bar{f}_L + f_L)$	$+0.04\pm0.06$
$A_{CP}^{\perp}$	$(\bar{f}_\perp - f_\perp)/(\bar{f}_\perp + f_\perp)$	$-0.11\pm0.12$
$\Delta \phi_{\parallel}$	$(ar{\phi_{\parallel}}-\phi_{\parallel})/2$	$+0.11\pm0.22$
$\Delta \phi_{\perp}$	$(\bar{\phi_{\perp}}-\phi_{\perp}-\pi)/2$	$+0.08\pm0.22$
$\Delta \delta_0$	$(ar{\delta_0}-\delta_0)/2$	$+0.27\pm0.16$

in the time evolution of *B*-decays [1]. In Table 1 and Ref. 8, these are chosen to be the direct-*CP* asymmetries in the overall decay rate  $\mathcal{A}_{CP}$ , in the  $f_L$  fraction  $\mathcal{A}_{CP}^0$ , and in the  $f_{\perp}$  fraction  $\mathcal{A}_{CP}^{\perp}$ , and three weak phase differences:

$$\Delta \phi_{\parallel} = \frac{1}{2} \arg(\bar{A}_{\parallel} A_0 / A_{\parallel} \bar{A}_0) , \qquad (8)$$

$$\Delta \phi_{\perp} = \frac{1}{2} \arg(\bar{A}_{\perp} A_0 / A_{\perp} \bar{A}_0) - \frac{\pi}{2}, \qquad (9)$$

$$\Delta \delta_0 = \frac{1}{2} \arg(\bar{A}_{00} A_0 / A_{00} \bar{A}_0) \,. \tag{10}$$

The  $\frac{\pi}{2}$  term in Eq. (9) reflects the fact that  $A_{\perp}$  and  $\bar{A}_{\perp}$  differ in phase by  $\pi$  if CP is conserved. The two parameters  $\Delta \phi_{\parallel}$  and  $\Delta \phi_{\perp}$  are equivalent to triple-product asymmetries constructed from the vectors describing the decay angular distribution [9]. The CP-violating phase difference in the reference decay mode [8] is, in the Wolfenstein CKM quark-mixing phase convention,

$$\Delta\phi_{00} = \frac{1}{2} \arg(A_{00}/\bar{A}_{00}) \,. \tag{11}$$

This can be measured only together with the mixing-induced phase difference for some of the neutral B-meson decays similar to other mixing-induced CP asymmetry measurements [1].

It may not always be possible to have a phase-reference decay mode which would define  $\delta_0$  and  $\Delta \delta_0$  parameters. In that case, it may be possible to define the phase difference directly similarly to Eq. (11):

$$\Delta \phi_0 = \frac{1}{2} \arg(A_0 / \bar{A}_0) \,. \tag{12}$$

One can measure the angles of the CKM unitarity triangle, assuming Standard Model contributions to the  $\Delta \phi_0$  and *B*mixing phases. Examples include measurements of  $\beta = \phi_1$  with  $B \to J/\psi K^*$  and  $\alpha = \phi_2$  with  $B \to \rho \rho$ .

Most of the *B* decays that arise from tree-level  $b \to c$ transitions have the amplitude hierarchy  $|A_0| > |A_+| > |A_-|$ which is expected from analyses based on quark-helicity conservation [10]. The larger the mass of the vector-meson daughters, the weaker the inequality. The *B* meson decays to heavy vector particles with charm, such as  $B \to J/\psi K^*$ ,  $\psi(2S)K^*$ ,  $\chi_{c1}K^*$ ,  $D^*\rho$ ,  $D^*K^*$ ,  $D^*D^*$ , and  $D^*D_s^*$ , show a substantial fraction of the amplitudes corresponding to transverse polarization of the vector mesons  $(A_{\pm 1})$ , in agreement with the factorization prediction. The detailed amplitude analysis of the  $B \to J/\psi K^*$ decays has been performed by the BABAR [11], Belle [12], CDF [13], CLEO [14], and D0 [15] collaborations. Most analyses are performed under the assumption of the absence of direct *CP* violation. The parameter values are given in the particle listing of this *Review*. The difference between the strong phases  $\phi_{\parallel}$  and  $\phi_{\perp}$  deviates significantly from zero. The recent measurements [11,12] of *CP*-violating terms similar to those in  $B \to \varphi K^*$  [8] shown in Table 1 are consistent with zero.

In addition, the mixing-induced *CP*-violating asymmetry is measured in the  $B^0 \to J/\psi K^{*0}$  decay [1,11,12] where angular analysis allows one to separate CP-eigenstate amplitudes. This allows one to resolve the sign ambiguity of the  $\cos 2\beta$  ( $\cos 2\phi_1$ ) term that appears in the time-dependent angular distribution due to interference of parity-even and parity-odd terms. This analysis relies on the knowledge of discrete ambiguities in the strong phases  $\phi_{\parallel}$  and  $\phi_{\perp}$ , as discussed below. The BABAR experiment used a method based on the dependence on the  $K\pi$ invariant mass of the interference between the S- and P-waves to resolve the discrete ambiguity in the determination of the strong phases  $(\phi_{\parallel}, \phi_{\perp})$  in  $B \to J/\psi K^*$  decays [11]. The result is in agreement with the amplitude hierarchy expectation [10]. The CDF [16], D0 [17], and LHCb [18] experiments have studied the  $B_s^0 \to J/\psi\varphi$  decay and provided the lifetime, polarization, and phase measurements.

The amplitude hierarchy  $|A_0| \gg |A_+| \gg |A_-|$  was expected in B decays to light vector particles in both penguin transitions [19,20] and tree-level transitions [10]. There is confirmation by the BABAR and Belle experiments of predominantly longitudinal polarization in the tree-level  $b \rightarrow u$  transition, such as  $B^0 \to \rho^+ \rho^-$  [21],  $B^+ \to \rho^0 \rho^+$  [22], and  $B^+ \to \omega \rho^+$  [23]; this is consistent with the analysis of the quark helicity conservation [10]. Because the longitudinal amplitude dominates the decay, a detailed amplitude analysis is not possible with current B samples, and limits on the transverse amplitude fraction are obtained. The fraction of transverse polarization is large in decays to heavier mesons such as  $B^0 \to a_1(1260)^+ a_1(1260)^-$  [24]. Only limits have been set for  $B^0 \to \omega \rho^0, \omega \omega$  [23]; there is some evidence for  $B^0 \to \rho^0 \rho^0$  [25] decays. The small values for these branching fractions indicates that  $b \to d$  penguin pollution is small in the charmless, strangeless vector-vector B decays.

The interest in the polarization and CP-asymmetry measurements in penguin transition, such as  $b \to s$  decays  $B \to \varphi K^*$ ,  $\rho K^*$ ,  $\omega K^*$ , or  $B^0_s \to \varphi \varphi$ , and  $b \to d$  decay  $B \to K^* \bar{K}^*$ ,

is motivated by their potential sensitivity to physics beyond the Standard Model. The decay amplitudes for  $B \to \varphi K^*$  have been measured by the BABAR and Belle experiments [8,26,27]. The fractions of longitudinal polarization are  $f_L = 0.50 \pm 0.05$ for the  $B^+ \to \varphi K^{*+}$  decay and  $f_L = 0.48 \pm 0.03$  for the  $B^0 \to \varphi K^{*0}$  decay. These indicate significant departure from the naive expectation of predominant longitudinal polarization, suggesting other contributions to the decay amplitude, previously neglected, either within the Standard Model, such as penguin annihilation [28] or QCD rescattering [29], or from physics beyond the Standard Model [30]. The complete set of twelve amplitude parameters measured in the  $B^0 \to \varphi K^{*0}$ decay is given in Table 1. Several other parameters could be constructed from the above twelve parameters, as suggested in Ref. 31.

The discrete ambiguity in the phase  $(\phi_{\parallel}, \phi_{\perp}, \Delta \phi_{\parallel}, \Delta \phi_{\perp})$ measurements has been resolved by BABAR in favor of  $|A_{+}| \gg$  $|A_{-}|$  through interference between the *S*- and *P*-waves of  $K\pi$ . The search for vector-tensor and vector-axialvector  $B \rightarrow$  $\varphi K_{J}^{(*)}$  decays with J = 1, 2, 3, 4 revealed a large fraction of longitudinal polarization in the decay  $B \rightarrow \varphi K_{2}^{*}(1430)$  with  $f_{L} = 0.90^{+0.06}_{-0.07}$  [8,32], but large contribution of transverse amplitude in  $B \rightarrow \varphi K_{1}(1270)$  with  $f_{L} = 0.46^{+0.13}_{-0.15}$  [33].

Like  $B \to \varphi K^*$ , the decays  $B \to \rho K^*$  and  $B \to \omega K^*$  may be sensitive to New Physics. Measurements of the longitudinal polarization fraction in  $B^+ \to \rho^0 K^{*0}$ ,  $B^+ \to \rho^+ K^{*0}$  [34] and in both vector-vector and vector-tensor final states of  $B \to \omega K_J^*$  [23] reveal a large fraction of transverse polarization, indicating an anomaly similar to  $B \to \varphi K^*$  except for a different pattern in vector-tensor final states. A large transverse polarization is also observed in the  $B_s^0 \to \varphi \varphi$  decays by CDF [37] and  $B_s^0 \to K^{*0} \bar{K}^{*0}$  decays by LHCb [36]. At the same time, first measurement of the polarization in the  $b \to d$  penguin decays  $B \to K^* \bar{K}^*$  indicates a large fraction of longitudinal polarization [35]. The polarization pattern in penguin-dominated *B*-meson decays is not fully understood [28,29,30].

The three-body semileptonic *B*-meson decays, such as  $B \rightarrow V\ell_1\ell_2$ , share many features with the two-body  $B \rightarrow VV$  decays.

Their differential decay width can be parameterized with the two helicity angles defined in the V and  $(\ell_1\ell_2)$  frames and with the azimuthal angle, as defined in Fig. 1. However, since the  $(\ell_1\ell_2)$  pair does not come from an on-shell particle, the angular distribution is unique to each point in the dilepton mass  $m_{\ell\ell}$  spectrum. The polarization measurements as a function of  $m_{\ell\ell}$  provide complementary information on physics beyond the Standard Model, as discussed for  $B \to K^* \ell^+ \ell^-$  decay in Ref. 38. The current data in this mode has been analyzed by the BABAR, Belle, and CDF experiments [39].

The examples of the angular distributions and observables in  $B \to K^* \ell^+ \ell^-$  are discussed in Ref. 38. Typically two angular observables have been measured in this decay in certain ranges of the dilepton mass  $m_{\ell\ell}$  [39]. One parameter is the fraction of longitudinal polarization  $F_L$ , which is determined by the  $K^*$ angular distribution and is similar to  $f_L$  defined for exclusive two-body decays. The other parameter is the forward-backward asymmetry of the lepton pair  $A_{FB}$ , which is the asymmetry of the decay rate with positive and negative values of  $\cos \theta_1$ .

In summary, there has been considerable recent interest in the polarization measurements of *B*-meson decays because they reveal both weak- and strong-interaction dynamics [28–30,40]. New measurements will further elucidate the pattern of spin alignment measurements in rare *B* decays, and further test the Standard Model and strong interaction dynamics, including the non-factorizable contributions to the *B*-decay amplitudes.

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