# 83. $D_s^+$ Branching Fractions

Updated September 2019 by J.L. Rosner (University of Chicago) and C.G. Wohl (LBNL).

Figure 83.1 shows a partial breakdown of the  $D_s^+$  branching fractions. The rest of this note is about how the figure was constructed. The values shown make heavy use of CLEO measurements of inclusive branching fractions [1]. For references to other data cited in the following, see the Listings.

### 83.1. Modes with leptons

The bottom  $(18.0 \pm 1.0)\%$  of Fig. 83.1 shows the fractions for the modes that include leptons. The measured  $K^0e^+\nu_e$  and  $K^{*0}e^+\nu_e$  fractions have been doubled to take account of the corresponding  $\mu^+\nu_\mu$  fractions. The sum of the exclusive  $Xe^+\nu_e$  fractions is  $(6.0 \pm 0.3)\%$ , consistent with an inclusive semileptonic measurement of  $(6.5 \pm 0.4)\%$ . There seems to be little missing here.

### 83.2. Inclusive hadronic $K\overline{K}$ fractions

The Cabibbo-favored  $c \to s$  decay in  $D_s^+$  decay produces a final state with both an s and an  $\bar{s}$ ; and thus modes with a  $K\overline{K}$  pair or with an  $\eta$ ,  $\omega$ ,  $\eta'$ , or  $\phi$  predominate (as may already be seen in Fig. 83.1 in the semileptonic fractions). We consider the  $K\overline{K}$  modes first. A complete picture of the exclusive  $K\overline{K}$  charge modes is not yet possible, because branching fractions for many of those modes have not yet been measured. However, CLEO has measured the inclusive  $K^+$ ,  $K^-$ ,  $K_S^0$ ,  $K^+K^-$ ,  $K^+K_S^0$ ,  $K^-K_S^0$ , and  $2K_S^0$  fractions (these include modes with leptons) [1]. And each of these inclusive fractions with a  $K_S^0$  is equal to the corresponding fraction with a  $K_L^0$ :  $f(K^+K_L^0) = f(K^+K_S^0)$ ,  $f(2K_L^0) = f(2K_S^0)$ , etc. Therefore, of all inclusive fractions pairing a  $K^+$ ,  $K_S^0$ , or  $K_L^0$  with a  $K^-$ ,  $K_S^0$ , or  $K_L^0$ , we know all but  $f(K_S^0K_L^0)$ .

We can get that fraction. The total  $K_S^0$  fraction is

$$f(K_S^0) = f(K^+ K_S^0) + f(K^- K_S^0) + 2f(2K_S^0) + f(K_S^0 K_L^0) + f(\text{single } K_S^0) ,$$

where  $f(\text{single }K_S^0)$  is the sum of the branching fractions for modes such as  $K_S^0\pi^+2\pi^0$  with a  $K_S^0$  and no second K. The  $K_S^0\pi^+2\pi^0$  mode is in fact the only unmeasured single- $K_S^0$  mode (throughout, we shall assume that fractions for modes with a K or  $K\overline{K}$  and more than three pions are negligible), and we shall take its fraction to be the same as for the  $K_S^02\pi^+\pi^-$  mode,  $(0.30\pm0.11)\%$ . Any reasonable deviation from this value would be too small to matter much in the following. Adding the several small single- $K_S^0$  branching fractions, including those from semileptonic modes, we get  $f(\text{single }K_S^0)=(1.7\pm0.2)\%$ .

Using this, we have:

$$\begin{split} f(K_S^0 K_L^0) &= f(K_S^0) - f(K^+ K_S^0) - f(K^- K_S^0) \\ &- 2 f(2 K_S^0) - f(\text{single } K_S^0) \\ &= (19.0 \pm 1.1) - (5.8 \pm 0.5) - (1.9 \pm 0.4) \\ &- 2 \times (1.7 \pm 0.3) - (1.7 \pm 0.2) \\ &= (6.2 \pm 1.4)\% \; . \end{split}$$

M. Tanabashi *et al.* (Particle Data Group), Phys. Rev. D **98**, 030001 (2018) and 2019 update

December 6, 2019 12:03



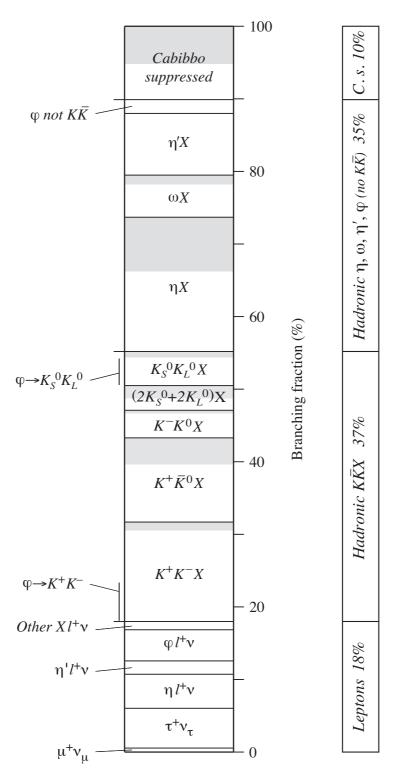


Figure 83.1: A partial breakdown of  $D_s^+$  branching fractions. The hadronic bins in the left column show inclusive fractions. Shading within a bin shows how much of the inclusive fraction is not yet accounted for by adding up all the relevant exclusive fractions. The inclusive hadronic  $\phi$  fraction is spread over three bins, in proportion to its decay fractions into  $K^+K^-$ ,  $K_S^0K_L^0$ , and no- $K\bar{K}$  modes.

Here and below we treat the errors as uncorrelated, although often they are not. However, our main aim is to get numbers for Fig. 83.1; errors are secondary.

There is a check on our result: The  $\phi$  inclusive branching fraction is  $(15.7 \pm 1.0)\%$ , of which 34%, or  $(5.34 \pm 0.34)\%$  of  $D_s^+$  decays, produces a  $K_S^0 K_L^0$ . Our  $f(K_S^0 K_L^0) = (6.2 \pm 1.4)\%$  has to be at least this large—and it is, within the sizable error.

We now have all the inclusive  $K\overline{K}$  fractions. We use  $f(K^+\overline{K}^0) = 2$   $f(K^+K_S^0)$ , and likewise for  $f(K^-K^0)$ . For  $K^+K^-$  and  $K_S^0K_L^0$ , we subtract off the contributions from  $\phi \ell^+ \nu$  decay to get the purely hadronic  $K\overline{K}$  inclusive fractions:

$$f(K^+K^-, \text{hadronic}) = (15.8 \pm 0.7) - (2.1 \pm 0.3)$$

$$= (13.7 \pm 0.8)\%$$

$$f(K^+\overline{K}^0, \text{hadronic}) = (11.6 \pm 1.0)\%$$

$$f(K^-K^0, \text{hadronic}) = (3.8 \pm 0.8)\%$$

$$f(2K_S^0 + 2K_L^0, \text{hadronic}) = (3.4 \pm 0.6)\%$$

$$f(K_S^0K_L^0, \text{hadronic}) = (6.2 \pm 1.4) - (1.5 \pm 0.2)$$

$$= (4.7 \pm 1.4)\%$$

The fractions are shown in Fig. 83.1. They total  $(37.2 \pm 2.2)\%$  of  $D_s^+$  decays.

We can add more information to the figure by summing up measured branching fractions for exclusive modes within each bin:

 $K^+K^-$  modes—The sum of measured  $K^+K^-\pi^+$ ,  $K^+K^-\pi^+\pi^0$ , and  $K^+K^-2\pi^+\pi^-$  branching fractions is  $(12.6\pm0.6)\%$ . That leaves  $(1.1\pm1.0)\%$  for the  $K^+K^-\pi^+2\pi^0$  mode, which is the only other  $K^+K^-$  mode with three or fewer pions. In Fig. 83.1, this unmeasured part of the  $K^+K^-$  bin is shaded.

 $K^+\overline{K}^0$  modes—Two times the sum of the measured  $K^+K^0_S$ ,  $K^+K^0_S\pi^0$ , and  $K^+K^0_S\pi^+\pi^-$  branching fractions is  $(8.0\pm0.5)\%$ . This leaves  $(3.6\pm1.1)\%$  for the unmeasured  $K^+\overline{K}^0$  modes (there are three such modes with three or fewer pions). This is shaded in the figure.

 $K^-K^0$  modes—Twice the  $K^-K^0_S 2\pi^+$  fraction is  $(3.4 \pm 0.2)\%$ , which leaves about  $(0.4 \pm 0.8)\%$  for  $K^-K^0 2\pi^+\pi^0$ , the only other  $K^-K^0$  mode with three or fewer pions.

 $2K_S^0+2K_L^0$  modes—The  $2K_S^0\pi^+$  and  $2K_S^02\pi^+\pi^-$  fractions sum to  $(0.86\pm0.07)\%$ ; this times two (for the corresponding  $2K_L^0$  modes) is  $(1.72\pm0.14)\%$ . This leaves about  $(1.7\pm0.7)\%$  for other  $2K_S^0+2K_L^0$  modes.

 $K^0_S K^0_L$  modes—Most of the  $K^0_S K^0_L$  fraction is accounted for by  $\phi$  decays (see below).

## 4 83. $D_s^+$ branching fractions

### 83.3. Inclusive hadronic $\eta, \omega, \eta'$ , and $\phi$ fractions

These are easier. We start with the inclusive branching fractions, and then, to avoid double counting, subtract: (1) fractions for modes with leptons; (2)  $\eta$  mesons that are included in the inclusive  $\eta'$  fraction; and (3)  $K^+K^-$  and  $K_S^0K_L^0$  from  $\phi$  decays:

$$f(\eta \text{ hadronic}) = f(\eta \text{ inclusive}) - 0.65 f(\eta' \text{ inclusive})$$

$$-f(\eta \ell^+ \nu) = (18.5 \pm 3.0)\%$$

$$f(\omega \text{ hadronic}) = f(\omega \text{ inclusive}) - 0.026 f(\eta' \text{ inclusive})$$

$$= (5.8 \pm 1.4)\%$$

$$f(\eta' \text{ hadronic}) = f(\eta' \text{ inclusive}) - f(\eta' \ell^+ \nu)$$

$$= (8.5 \pm 1.5)\%$$

$$f(\phi \text{ hadronic}, \not \to K\overline{K}) = 0.17 \left[ f(\phi \text{ inclusive}) - f(\phi \ell^+ \nu) \right]$$

$$= (1.9 \pm 0.2)\%.$$

The factors 0.65, 0.026, and 0.17 are the  $\eta' \to \eta$ ,  $\eta' \to \omega$ , and  $\phi \not\to K\overline{K}$  branching fractions. Figure 83.1 shows the results; the sum is  $(34.7 \pm 3.6)\%$ , which is about equal to the hadronic  $K\overline{K}$  total.

Note that the bin marked  $\phi$  near the top of Fig. 83.1 includes neither the  $\phi \ell^+ \nu$  decays nor the 83% of other  $\phi$  decays that produce a  $K\overline{K}$  pair. There is twice as much  $\phi$  in the  $K_S^0 K_L^0$  bin, and nearly three times as much in the  $K^+ K^-$  bin. These contributions are indicated in those bins.

Again, we can show how much of each bin is accounted for by measured exclusive branching fractions:

 $\eta$  modes—The sum of  $\eta \pi^+$ ,  $\eta \pi^+ \pi^0$  (nearly all  $\eta \rho^+$ ), and  $\eta K^+$  branching fractions is  $(11.1 \pm 1.2)\%$ , which leaves a good part of the inclusive hadronic  $\eta$  fraction,  $(18.5 \pm 3.0)\%$ , to be accounted for. This is shaded in the figure.

 $\omega$  modes—The sum of  $\omega \pi^+$ ,  $\omega \pi^+ \pi^0$ , and  $\omega 2\pi^+ \pi^-$  fractions is  $(4.6 \pm 0.9)\%$ , which is nearly as large as the inclusive hadronic  $\omega$  fraction,  $(5.8 \pm 1.4)\%$ .

 $\eta'$  modes—The sum of  $\eta'\pi^+$ ,  $\eta'\rho^+$ , and  $\eta'K^+$  fractions is  $(9.9 \pm 1.5)\%$ , which is larger than but not in serious disagreement with the inclusive hadronic  $\eta'$  fraction,  $(8.5 \pm 1.5)\%$ .

### 83.4. Cabibbo-suppressed modes

The sum of the fractions for modes with a  $K\bar{K}$ ,  $\eta$ ,  $\omega$ ,  $\eta'$ , or leptons is  $(89.9 \pm 4.4)\%$ . The remaining  $(10.1 \pm 4.4)\%$  is to Cabibbo-suppressed modes, mainly single-K+ pions and multiple-pion modes (see below). However, it should be noted that some small parts of the modes already discussed are Cabibbo-suppressed. For example, the  $(1.1 \pm 0.2)\%$  of  $D_s^+$  decays to  $K^0\ell\nu$  or  $K^{*0}\ell\nu$  is already in the  $X\ell\nu$  bin in Fig. 83.1. And the inclusive measurements of  $\eta$ ,  $\omega$ , and  $\eta'$  fractions do not distinguish between (and therefore include

both) Cabibbo-allowed and -suppressed modes. We shall not try to make a separation here.

 $K^0+pions$ —Above, we found that  $f(\text{single }K^0_S)=(1.7\pm0.2)\%$ . Subtracting semileptonic fractions with a  $K^0_S$  leaves  $(1.3\pm0.2)\%$ . The hadronic single- $K^0$  fraction is twice this, about  $(2.6\pm0.4)\%$ . The sum of measured  $K^0\pi^+$ ,  $K^0\pi^+\pi^0$ , and  $K^02\pi^+\pi^-$  fractions is  $(1.8\pm0.3)\%$ , about two-thirds as much.

 $K^+ + pions$ —The  $K^+\pi^0$  and  $K^+\pi^+\pi^-$  fractions sum to  $(0.72 \pm 0.05)\%$ . The total  $K^+$  fraction wanted here is probably in the 1-to-2% range.

Multi-pions—The  $2\pi^+\pi^-$ ,  $\pi^+2\pi^0$ , and  $3\pi^+2\pi^-$  fractions total  $(2.5\pm0.2)\%$ . Modes not measured might double this.

The sum of the actually measured fractions is, including the semileptonics,  $(4.9\pm0.3)\%$ . The error on our Cabibbo-suppressed total,  $(10.1\pm4.4)\%$  is too large to know how much we might be missing.

#### References:

1. S. Dobbs *et al.*, Phys. Rev. **D79**, 112008 (2009).