

$f_4(2050)$ 

$$I^G(J^{PC}) = 0^+(4^{++})$$

NODE=M016

 $f_4(2050)$  MASS

NODE=M016M

NODE=M016M

VALUE (MeV)	EVTs	DOCUMENT ID	TECN	COMMENT
<b>2018±11 OUR AVERAGE</b>		Error includes scale factor of 2.1. See the ideogram below.		
1960±15		AMELIN	06 VES	36 $\pi^- p \rightarrow \omega \omega n$
2005±10		<sup>1</sup> BINON	05 GAMS	33 $\pi^- p \rightarrow \eta \eta n$
1998±15		ALDE	98 GAM4	100 $\pi^- p \rightarrow \pi^0 \pi^0 n$
2060±20		ALDE	90 GAM2	38 $\pi^- p \rightarrow \omega \omega n$
2038±30		AUGUSTIN	87 DM2	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
2086±15		BALTRUSAIT..	87 MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
2000±60		ALDE	86D GAM4	100 $\pi^- p \rightarrow n 2\eta$
2020±20	40k	<sup>2</sup> BINON	84B GAM2	38 $\pi^- p \rightarrow n 2\pi^0$
2015±28		<sup>3</sup> CASON	82 STRC	8 $\pi^+ p \rightarrow \Delta^{++} \pi^0 \pi^0$
2031 <sup>+25</sup> <sub>-36</sub>		ETKIN	82B MPS	23 $\pi^- p \rightarrow n 2K_S^0$
2020±30	700	APEL	75 NICE	40 $\pi^- p \rightarrow n 2\pi^0$
2050±25		BLUM	75 ASPK	18.4 $\pi^- p \rightarrow n K^+ K^-$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
1966±25		<sup>4</sup> ANISOVICH	09 RVUE	0.0 $\bar{p} p, \pi N$
1885 <sup>+14+218</sup> <sub>-13-25</sub>		<sup>5</sup> UEHARA	09 BELL	10.6 $e^+ e^- \rightarrow e^+ e^- \pi^0 \pi^0$
2018± 6		ANISOVICH	00J SPEC	2.0 $\bar{p} p \rightarrow \eta \pi^0 \pi^0, \pi^0 \pi^0,$ $\eta \eta, \eta \eta', \pi \pi$
~ 2000		<sup>6</sup> MARTIN	98 RVUE	$\bar{N} N \rightarrow \pi \pi$
~ 2010		<sup>7</sup> MARTIN	97 RVUE	$\bar{N} N \rightarrow \pi \pi$
~ 2040		<sup>8</sup> OAKDEN	94 RVUE	0.36-1.55 $\bar{p} p \rightarrow \pi \pi$
~ 1990		<sup>9</sup> OAKDEN	94 RVUE	0.36-1.55 $\bar{p} p \rightarrow \pi \pi$
1978± 5		<sup>10</sup> ALPER	80 CNTR	62 $\pi^- p \rightarrow K^+ K^- n$
2040±10		<sup>10</sup> ROZANSKA	80 SPRK	18 $\pi^- p \rightarrow p \bar{p} n$
1935±13		<sup>10</sup> CORDEN	79 OMEG	12-15 $\pi^- p \rightarrow n 2\pi$
1988± 7		EVANGELIS...	79B OMEG	10 $\pi^- p \rightarrow K^+ K^- n$
1922±14		<sup>11</sup> ANTIPOV	77 CIBS	25 $\pi^- p \rightarrow p 3\pi$

OCCUR=2

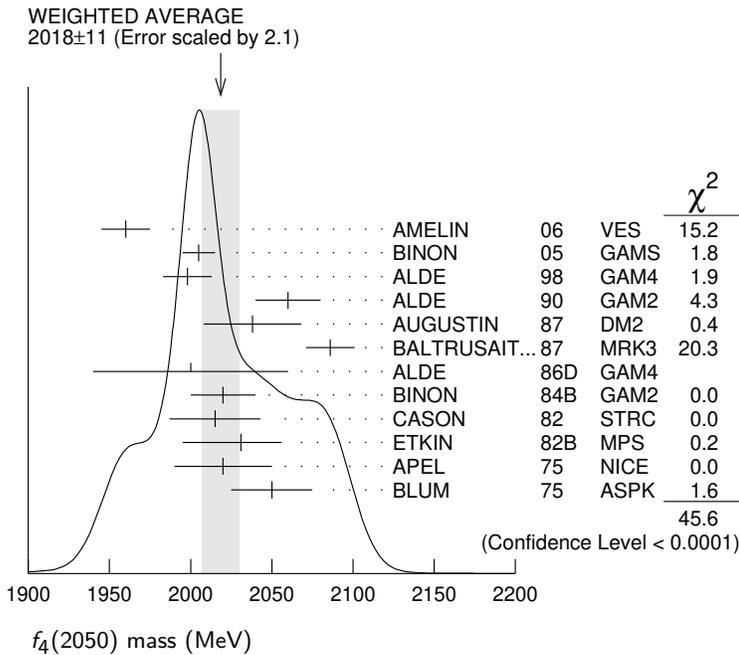
<sup>1</sup> From the first PWA solution.<sup>2</sup> From a partial-wave analysis of the data.<sup>3</sup> From an amplitude analysis of the reaction  $\pi^+ \pi^- \rightarrow 2\pi^0$ .<sup>4</sup> K matrix pole.<sup>5</sup> Taking into account the  $f_2(1950)$ . Helicity-2 production favored.<sup>6</sup> Energy-dependent analysis.<sup>7</sup> Single energy analysis.<sup>8</sup> From solution A of amplitude analysis of data on  $\bar{p} p \rightarrow \pi \pi$ . See however KLOET 96 who fit  $\pi^+ \pi^-$  only and find waves only up to  $J = 3$  to be important but not significantly resonant.<sup>9</sup> From solution B of amplitude analysis of data on  $\bar{p} p \rightarrow \pi \pi$ . See however KLOET 96 who fit  $\pi^+ \pi^-$  only and find waves only up to  $J = 3$  to be important but not significantly resonant.<sup>10</sup>  $I(J^P) = 0(4^+)$  from amplitude analysis assuming one-pion exchange.<sup>11</sup> Width errors enlarged by us to  $4\Gamma/\sqrt{N}$ ; see the note with the  $K^*(892)$  mass.

NODE=M016M;LINKAGE=BI  
 NODE=M016M;LINKAGE=N  
 NODE=M016M;LINKAGE=NN  
 NODE=M016M;LINKAGE=KM  
 NODE=M016M;LINKAGE=UE  
 NODE=M016M;LINKAGE=RB  
 NODE=M016M;LINKAGE=BR  
 NODE=M016M;LINKAGE=B

NODE=M016M;LINKAGE=BB

NODE=M016M;LINKAGE=M

NODE=M016M;LINKAGE=T



**$f_4(2050)$  WIDTH**

NODE=M016W

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>237± 18 OUR AVERAGE</b>		Error includes scale factor of 1.9. See the ideogram below.		
290± 20		AMELIN	06 VES	36 $\pi^- p \rightarrow \omega \omega n$
340± 80		12 BINON	05 GAMS	33 $\pi^- p \rightarrow \eta \eta n$
395± 40		ALDE	98 GAM4	100 $\pi^- p \rightarrow \pi^0 \pi^0 n$
170± 60		ALDE	90 GAM2	38 $\pi^- p \rightarrow \omega \omega n$
304± 60		AUGUSTIN	87 DM2	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
210± 63		BALTRUSAIT..	87 MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
400±100		ALDE	86D GAM4	100 $\pi^- p \rightarrow n 2 \eta$
240± 40	40k	13 BINON	84B GAM2	38 $\pi^- p \rightarrow n 2 \pi^0$
190± 14		DENNEY	83 LASS	10 $\pi^+ n / \pi^+ p$
186 <sup>+103</sup> <sub>-58</sub>		14 CASON	82 STRC	8 $\pi^+ p \rightarrow \Delta^{++} \pi^0 \pi^0$
305 <sup>+36</sup> <sub>-119</sub>		ETKIN	82B MPS	23 $\pi^- p \rightarrow n 2 K_S^0$
180± 60	700	APEL	75 NICE	40 $\pi^- p \rightarrow n 2 \pi^0$
225 <sup>+120</sup> <sub>-70</sub>		BLUM	75 ASPK	18.4 $\pi^- p \rightarrow n K^+ K^-$

NODE=M016W

- • • We do not use the following data for averages, fits, limits, etc. • • •
- 260± 40      15 ANISOVICH    09 RVUE    0.0  $\bar{p} p, \pi N$
- 453± 20<sup>+31</sup><sub>-129</sub>      16 UEHARA        09 BELL    10.6  $e^+ e^- \rightarrow e^+ e^- \pi^0 \pi^0$
- 182± 7        ANISOVICH    00J SPEC    2.0  $\bar{p} p \rightarrow \eta \pi^0 \pi^0, \pi^0 \pi^0,$   
 $\eta \eta, \eta \eta', \pi \pi$
- ~ 170        17 MARTIN       98 RVUE     $N \bar{N} \rightarrow \pi \pi$
- ~ 200        18 MARTIN       97 RVUE     $\bar{N} N \rightarrow \pi \pi$
- ~ 60         19 OAKDEN       94 RVUE    0.36-1.55  $\bar{p} p \rightarrow \pi \pi$
- ~ 80         20 OAKDEN       94 RVUE    0.36-1.55  $\bar{p} p \rightarrow \pi \pi$
- 243± 16      21 ALPER         80 CNTR    62  $\pi^- p \rightarrow K^+ K^- n$
- 140± 15      21 ROZANSKA    80 SPRK    18  $\pi^- p \rightarrow p \bar{p} n$
- 263± 57      21 CORDEN       79 OMEG    12-15  $\pi^- p \rightarrow n 2 \pi$
- 100± 28      EVANGELIS... 79B OMEG    10  $\pi^- p \rightarrow K^+ K^- n$
- 107± 56      22 ANTIPOV     77 CIBS    25  $\pi^- p \rightarrow p 3 \pi$

OCCUR=2

12 From the first PWA solution.  
 13 From a partial-wave analysis of the data.  
 14 From an amplitude analysis of the reaction  $\pi^+ \pi^- \rightarrow 2 \pi^0$ .  
 15 K matrix pole.  
 16 Taking into account the  $f_2(1950)$ . Helicity-2 production favored.  
 17 Energy-dependent analysis.  
 18 Single energy analysis.

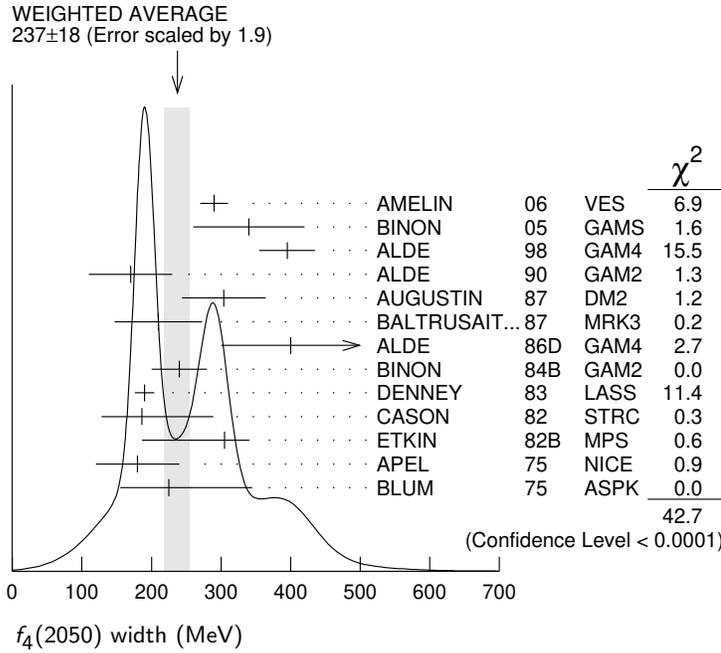
NODE=M016W;LINKAGE=BI  
 NODE=M016W;LINKAGE=N  
 NODE=M016W;LINKAGE=NN  
 NODE=M016W;LINKAGE=KM  
 NODE=M016W;LINKAGE=UE  
 NODE=M016W;LINKAGE=RB  
 NODE=M016W;LINKAGE=BR

- 19 From solution A of amplitude analysis of data on  $\bar{p}p \rightarrow \pi\pi$ . See however KLOET 96 who fit  $\pi^+\pi^-$  only and find waves only up to  $J = 3$  to be important but not significantly resonant.
- 20 From solution B of amplitude analysis of data on  $\bar{p}p \rightarrow \pi\pi$ . See however KLOET 96 who fit  $\pi^+\pi^-$  only and find waves only up to  $J = 3$  to be important but not significantly resonant.
- 21  $I(J^P) = 0(4^+)$  from amplitude analysis assuming one-pion exchange.
- 22 Width errors enlarged by us to  $4\Gamma/\sqrt{N}$ ; see the note with the  $K^*(892)$  mass.

NODE=M016W;LINKAGE=BW

NODE=M016W;LINKAGE=BB

NODE=M016W;LINKAGE=M  
NODE=M016W;LINKAGE=T



**f<sub>4</sub>(2050) DECAY MODES**

NODE=M016215;NODE=M016

Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$ $\omega\omega$	seen
$\Gamma_2$ $\pi\pi$	(17.0±1.5) %
$\Gamma_3$ $K\bar{K}$	( 6.8 <sup>+3.4</sup> <sub>-1.8</sub> ) × 10 <sup>-3</sup>
$\Gamma_4$ $\eta\eta$	( 2.1±0.8) × 10 <sup>-3</sup>
$\Gamma_5$ $4\pi^0$	< 1.2 %
$\Gamma_6$ $\gamma\gamma$	seen
$\Gamma_7$ $a_2(1320)\pi$	seen

DESIG=6  
DESIG=1  
DESIG=2  
DESIG=3  
DESIG=5  
DESIG=4;OUR EVAL;→ UNCHECKED ←  
DESIG=7

**f<sub>4</sub>(2050)  $\Gamma(i)\Gamma(\gamma\gamma)/\Gamma(\text{total})$**

NODE=M016220

$\Gamma(K\bar{K}) \times \Gamma(\gamma\gamma)/\Gamma_{\text{total}}$	$\Gamma_3\Gamma_6/\Gamma$
VALUE (keV) CL% DOCUMENT ID TECN COMMENT	
••• We do not use the following data for averages, fits, limits, etc. •••	
<0.29 95 ALTHOFF 85B TASS $\gamma\gamma \rightarrow K\bar{K}\pi$	

NODE=M016G2  
NODE=M016G2

$\Gamma(\pi\pi) \times \Gamma(\gamma\gamma)/\Gamma_{\text{total}}$	$\Gamma_2\Gamma_6/\Gamma$
VALUE (eV) CL% EVTS DOCUMENT ID TECN COMMENT	
••• We do not use the following data for averages, fits, limits, etc. •••	
23.1 <sup>+3.6+70.5</sup> <sub>-3.3-15.6</sub> 23 UEHARA 09 BELL 10.6 $e^+e^- \rightarrow e^+e^-\pi^0\pi^0$	
<1100 95 13 ± 4 OEST 90 JADE $e^+e^- \rightarrow e^+e^-\pi^0\pi^0$	

NODE=M016G3  
NODE=M016G3

<sup>23</sup> Taking into account the  $f_2(1950)$ . Helicity-2 production favored.

NODE=M016G3;LINKAGE=UE

**f<sub>4</sub>(2050) BRANCHING RATIOS**

NODE=M016225

$\Gamma(\omega\omega)/\Gamma_{\text{total}}$	$\Gamma_1/\Gamma$
VALUE DOCUMENT ID TECN COMMENT	
seen AMELIN 06 VES 36 $\pi^-p \rightarrow \omega\omega n$	
••• We do not use the following data for averages, fits, limits, etc. •••	
not seen BARBERIS 00F 450 $pp \rightarrow pf\omega\omega p_S$	

NODE=M016R7  
NODE=M016R7

$\Gamma(\omega\omega)/\Gamma(\pi\pi)$				$\Gamma_1/\Gamma_2$	
VALUE	DOCUMENT ID	TECN	COMMENT		
<b>1.5±0.3</b>	ALDE	90	GAM2 38 $\pi^- p \rightarrow \omega\omega n$		NODE=M016R5 NODE=M016R5
$\Gamma(\pi\pi)/\Gamma_{total}$				$\Gamma_2/\Gamma$	
VALUE	DOCUMENT ID	TECN	COMMENT		
<b>0.170±0.015 OUR AVERAGE</b>					NODE=M016R1 NODE=M016R1
0.18 ±0.03	24 BINON	83C	GAM2 38 $\pi^- p \rightarrow n4\gamma$		
0.16 ±0.03	24 CASON	82	STRC 8 $\pi^+ p \rightarrow \Delta^{++}\pi^0\pi^0$		
0.17 ±0.02	24 CORDEN	79	OMEG 12-15 $\pi^- p \rightarrow n2\pi$		
<sup>24</sup> Assuming one pion exchange.					NODE=M016R1;LINKAGE=A
$\Gamma(K\bar{K})/\Gamma(\pi\pi)$				$\Gamma_3/\Gamma_2$	
VALUE	DOCUMENT ID	TECN	COMMENT		
<b>0.04<sup>+0.02</sup><sub>-0.01</sub></b>	ETKIN	82B	MPS 23 $\pi^- p \rightarrow n2K_S^0$		NODE=M016R2 NODE=M016R2
$\Gamma(\eta\eta)/\Gamma_{total}$				$\Gamma_4/\Gamma$	
VALUE (units 10 <sup>-3</sup> )	DOCUMENT ID	TECN	COMMENT		
<b>2.1±0.8</b>	ALDE	86D	GAM4 100 $\pi^- p \rightarrow n4\gamma$		NODE=M016R3 NODE=M016R3
$\Gamma(4\pi^0)/\Gamma_{total}$				$\Gamma_5/\Gamma$	
VALUE	DOCUMENT ID	TECN	COMMENT		
<b>&lt;0.012</b>	ALDE	87	GAM4 100 $\pi^- p \rightarrow 4\pi^0 n$		NODE=M016R4 NODE=M016R4
$\Gamma(a_2(1320)\pi)/\Gamma_{total}$				$\Gamma_7/\Gamma$	
VALUE	DOCUMENT ID	TECN	COMMENT		
<b>seen</b>	AMELIN	00	VES 37 $\pi^- p \rightarrow \eta\pi^+\pi^- n$		NODE=M016R6 NODE=M016R6

### $f_4(2050)$ REFERENCES

					NODE=M016
ANISOVICH	09	IJMP A24 2481	V.V. Anisovich, A.V. Sarantsev	(PNPI)	REFID=52719
UEHARA	09	PR D79 052009	S. Uehara <i>et al.</i>	(BELLE Collab.)	REFID=52761
AMELIN	06	PAN 69 690	D.V. Amelin <i>et al.</i>	(VES Collab.)	REFID=51574
BINON	05	PAN 68 960	F. Binon <i>et al.</i>		REFID=50780
AMELIN	00	NP A668 83	D. Amelin <i>et al.</i>	(VES Collab.)	REFID=47432
ANISOVICH	00J	PL B491 47	A.V. Anisovich <i>et al.</i>	(RAL, LOQM, PNPI+)	REFID=47950
BARBERIS	00F	PL B484 198	D. Barberis <i>et al.</i>	(WA 102 Collab.)	REFID=47962
ALDE	98	EPJ A3 361	D. Alde <i>et al.</i>	(GAM4 Collab.)	REFID=46605
Also		PAN 62 405	D. Alde <i>et al.</i>	(GAMS Collab.)	REFID=46914
MARTIN	98	PR C57 3492	B.R. Martin <i>et al.</i>		REFID=46373
MARTIN	97	PR C56 1114	B.R. Martin, G.C. Oades	(LOUC, AARH)	REFID=45685
KLOET	96	PR D53 6120	W.M. Kloet, F. Myhrer	(RUTG, NORD)	REFID=45212
OAKDEN	94	NP A574 731	M.N. Oakden, M.R. Pennington	(DURH)	REFID=45210
ALDE	90	PL B241 600	D.M. Alde <i>et al.</i>	(SERP, BELG, LANL, LAPP+)	REFID=40935
OEST	90	ZPHY C47 343	T. Oest <i>et al.</i>	(JADE Collab.)	REFID=41358
ALDE	87	PL B198 286	D.M. Alde <i>et al.</i>	(LANL, BRUX, SERP, LAPP)	REFID=40221
AUGUSTIN	87	ZPHY C36 369	J.E. Augustin <i>et al.</i>	(LALO, CLER, FRAS+)	REFID=40268
BALTRUSAIT...	87	PR D35 2077	R.M. Baltrusaitis <i>et al.</i>	(Mark III Collab.)	REFID=40010
ALDE	86D	NP B269 485	D.M. Alde <i>et al.</i>	(BELG, LAPP, SERP, CERN+)	REFID=20765
ALTHOFF	85B	ZPHY C29 189	M. Althoff <i>et al.</i>	(TASSO Collab.)	REFID=21349
BINON	84B	LNC 39 41	F.G. Binon <i>et al.</i>	(SERP, BELG, LAPP)	REFID=21780
BINON	83C	SJNP 38 723	F.G. Binon <i>et al.</i>	(SERP, BRUX+)	REFID=40288
DENNEY	83	PR D28 2726	D.L. Denney <i>et al.</i>	(IOWA, MICH)	REFID=20754
CASON	82	PRL 48 1316	N.M. Cason <i>et al.</i>	(NDAM, ANL)	REFID=20746
ETKIN	82B	PR D25 1786	A. Etkin <i>et al.</i>	(BNL, CUNY, TUFTS, VAND)	REFID=20390
ALPER	80	PL 94B 422	B. Alper <i>et al.</i>	(AMST, CERN, CRAC, MPIM+)	REFID=21665
ROZANSKA	80	NP B162 505	M. Rozanska <i>et al.</i>	(MPIM, CERN)	REFID=21774
CORDEN	79	NP B157 250	M.J. Corden <i>et al.</i>	(BIRM, RHEL, TELA+)	REFID=20374
EVANGELIS...	79B	NP B154 381	C. Evangelista <i>et al.</i>	(BARI, BONN, CERN+)	REFID=21967
ANTIPOV	77	NP B119 45	Y.M. Antipov <i>et al.</i>	(SERP, GEVA)	REFID=20728
APEL	75	PL 57B 398	W.D. Apel <i>et al.</i>	(KARLK, KARLE, PISA, SERP+)	REFID=20720
BLUM	75	PL 57B 403	W. Blum <i>et al.</i>	(CERN, MPIM) JP	REFID=21651