



$$I(J^P) = \frac{1}{2}(0^-)$$

## $K_S^0$ MEAN LIFE

For earlier measurements, beginning with BOLDT 58B, see our 1986 edition, Physics Letters **170B** 130 (1986).

OUR FIT is described in the note on "CP violation in  $K_L$  decays" in the  $K_L^0$  Particle Listings. The result labeled "OUR FIT Assuming CPT" ["OUR FIT Not assuming CPT"] includes all measurements except those with the comment "Not assuming CPT" ["Assuming CPT"]. Measurements with neither comment do not assume CPT and enter both fits.

VALUE ( $10^{-10}$ s)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.8954 ± 0.0004 OUR FIT</b>		Error includes scale factor of 1.1. Assuming CPT		
<b>0.89564 ± 0.00033 OUR FIT</b>		Not assuming CPT		
0.89589 ± 0.00070		1,2 ABOUZAID	11 KTEV	Not assuming CPT
0.89623 ± 0.00047		1,3 ABOUZAID	11 KTEV	Assuming CPT
0.89562 ± 0.00029 ± 0.00043	20M	4 AMBROSINO	11 KLOE	Not assuming CPT
0.89598 ± 0.00048 ± 0.00051	16M	LAI	02C NA48	
0.8971 ± 0.0021		BERTANZA	97 NA31	
0.8941 ± 0.0014 ± 0.0009		SCHWINGEN...	95 E773	Assuming CPT
0.8929 ± 0.0016		GIBBONS	93 E731	Assuming CPT
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.8965 ± 0.0007		5 ALAVI-HARATI03	KTEV	Assuming CPT
0.8958 ± 0.0013		6 ALAVI-HARATI03	KTEV	Not assuming CPT
0.8920 ± 0.0044	214k	GROSSMAN	87 SPEC	
0.905 ± 0.007		7 ARONSON	82B SPEC	
0.881 ± 0.009	26k	ARONSON	76 SPEC	
0.8926 ± 0.0032 ± 0.0002		8 CARITHERS	75 SPEC	
0.8937 ± 0.0048	6M	GEWENIGER	74B ASPK	
0.8958 ± 0.0045	50k	9 SKJEGGESTAD	72 HBC	
0.856 ± 0.008	19994	10 DONALD	68B HBC	
0.872 ± 0.009	20000	9,10 HILL	68 DBC	

1 The two ABOUZAID 11 values use the same full KTeV dataset from 1996, 1997, and 1999. The first enters the "assuming CPT" fit and the second enters the "not assuming CPT" fit.

2 ABOUZAID 11 fit has  $\Delta m$ ,  $\tau_s$ ,  $\phi_\epsilon$ ,  $\text{Re}(\epsilon'/\epsilon)$ , and  $\text{Im}(\epsilon'/\epsilon)$  as free parameters. See  $\text{Im}(\epsilon'/\epsilon)$  in the " $K_L^0$  CP violation" section for correlation information.

3 ABOUZAID 11 fit has  $\Delta m$  and  $\tau_s$  free but constrains  $\phi_\epsilon$  to the Superweak value, i.e. assumes CPT. This  $\tau_s$  value is correlated with their  $\Delta m = m_{K_L^0} - m_{K_S^0}$  measurement in the  $K_L^0$  listings. The correlation coefficient  $\rho(\tau_s, \Delta m) = -0.670$ .

4 Fit to the proper time distribution.

5 This ALAVI-HARATI 03 fit has  $\Delta m$  and  $\tau_s$  free but constrains  $\phi_{+-}$  to the Superweak value, i.e. assumes CPT. This  $\tau_s$  value is correlated with their  $\Delta m = m_{K_L^0} - m_{K_S^0}$  measurement in the  $K_L^0$  listings. The correlation coefficient  $\rho(\tau_s, \Delta m) = -0.396$ .

Superseded by ABOUZAID 11.

6 This ALAVI-HARATI 03 fit has  $\Delta m$ ,  $\phi_{+-}$ , and  $\tau_{K_S^0}$  free. See  $\phi_{+-}$  in the " $K_L$  CP violation" section for correlation information. Superseded by ABOUZAID 11.

7 ARONSON 82 find that  $K_S^0$  mean life may depend on the kaon energy.

8 CARITHERS 75 measures the  $\Delta m$  dependence of the total decay rate (inverse mean life) to be  $\Gamma(K_S^0) = [(1.122 \pm 0.004) + 0.16(\Delta m - 0.5348)/\Delta m] 10^{10}/\text{s}$ , or, in terms of mean life, CARITHERS 75 measures  $\tau_s = (0.8913 \pm 0.0032) - 0.238 [\Delta m - 0.5348] (10^{-10} \text{ s})$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ s}^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

9 HILL 68 has been changed by the authors from the published value ( $0.865 \pm 0.009$ ) because of a correction in the shift due to  $\eta_{+-}$ . SKJEGGESTAD 72 and HILL 68 give detailed discussions of systematics encountered in this type of experiment.

10 Pre-1971 experiments are excluded from the average because of disagreement with later more precise experiments.

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NODE=S012T

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TYPE=noCPT

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TYPE=CPT

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NODE=S012T;LINKAGE=AU

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NODE=S012T;LINKAGE=TG

NODE=S012T;LINKAGE=S3

NODE=S012T;LINKAGE=A2

NODE=S012T;LINKAGE=C2

NODE=S012T;LINKAGE=H1

NODE=S012T;LINKAGE=N

## $K_S^0$ DECAY MODES

Mode		Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	
<b>Hadronic modes</b>				
$\Gamma_1$	$\pi^0 \pi^0$	( $30.69 \pm 0.05$ ) %		NODE=S012;CLUMP=A
$\Gamma_2$	$\pi^+ \pi^-$	( $69.20 \pm 0.05$ ) %		DESIG=2
$\Gamma_3$	$\pi^+ \pi^- \pi^0$	( $3.5^{+1.1}_{-0.9}$ ) $\times 10^{-7}$		DESIG=1
<b>Modes with photons or <math>\ell\bar{\ell}</math> pairs</b>				
$\Gamma_4$	$\pi^+ \pi^- \gamma$	[a,b] ( $1.79 \pm 0.05$ ) $\times 10^{-3}$		NODE=S012;CLUMP=B
$\Gamma_5$	$\pi^+ \pi^- e^+ e^-$	( $4.79 \pm 0.15$ ) $\times 10^{-5}$		DESIG=5
$\Gamma_6$	$\pi^0 \gamma \gamma$	[a] ( $4.9 \pm 1.8$ ) $\times 10^{-8}$		DESIG=13
$\Gamma_7$	$\gamma \gamma$	( $2.63 \pm 0.17$ ) $\times 10^{-6}$	S=3.1	DESIG=14
$\Gamma_8$	$\mu^+ \mu^- \mu^+ \mu^-$	< 5.1 $\times 10^{-12}$	CL=90%	DESIG=6
<b>Semileptonic modes</b>				
$\Gamma_9$	$\pi^\pm e^\mp \nu_e$	[c] ( $7.14 \pm 0.06$ ) $\times 10^{-4}$		NODE=S012;CLUMP=C
$\Gamma_{10}$	$\pi^\pm \mu^\mp \nu_\mu$	[c,d] ( $4.56 \pm 0.20$ ) $\times 10^{-4}$		DESIG=11
<b>CP violating (CP) and <math>\Delta S = 1</math> weak neutral current (S1) modes</b>				
$\Gamma_{11}$	$3\pi^0$	CP < 2.6 $\times 10^{-8}$	CL=90%	NODE=S012;CLUMP=F
$\Gamma_{12}$	$\mu^+ \mu^-$	S1 < 2.1 $\times 10^{-10}$	CL=90%	DESIG=7
$\Gamma_{13}$	$e^+ e^-$	S1 < 9 $\times 10^{-9}$	CL=90%	DESIG=3
$\Gamma_{14}$	$\pi^0 e^+ e^-$	S1 [a] ( $3.0^{+1.5}_{-1.2}$ ) $\times 10^{-9}$		DESIG=4
$\Gamma_{15}$	$\pi^0 \mu^+ \mu^-$	S1 ( $2.9^{+1.5}_{-1.2}$ ) $\times 10^{-9}$		DESIG=10
[a] See the Particle Listings below for the energy limits used in this measurement.				
[b] Most of this radiative mode, the low-momentum $\gamma$ part, is also included in the parent mode listed without $\gamma$ 's.				
[c] The value is for the sum of the charge states or particle/antiparticle states indicated.				
[d] Not a measurement. Calculated as $0.666 \cdot B(\pi^\pm e^\mp \nu_e)$ .				
LINKAGE=KDS				
LINKAGE=KX				
LINKAGE=SG				
LINKAGE=NM				

### CONSTRAINED FIT INFORMATION

An overall fit to 4 branching ratios uses 5 measurements and one constraint to determine 4 parameters. The overall fit has a  $\chi^2 = 0.6$  for 2 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta x_i \delta x_j \rangle / (\delta x_i \cdot \delta x_j)$ , in percent, from the fit to the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

$x_2$	-100			
$x_9$	-9	8		
$x_{10}$	-1	-3	0	
	$x_1$	$x_2$	$x_9$	

## $K_S^0$ DECAY RATES

$\Gamma(\pi^\pm e^\mp \nu_e)$		$\Gamma_9$
VALUE ( $10^6 \text{ s}^{-1}$ )	EVTS	DOCUMENT ID
• • • We do not use the following data for averages, fits, limits, etc. • • •		TECN COMMENT
8.1 $\pm 1.6$	75	<sup>1</sup> AKHMETSHIN 99 CMD2 Tagged $K_S^0$ using $\phi \rightarrow K_L^0 K_S^0$
7.50 $\pm 0.08$		<sup>2</sup> PDG 98
seen	BURGUN	72 HBC $K^+ p \rightarrow K^0 p \pi^+$
9.3 $\pm 2.5$	AUBERT	65 HLBC $\Delta S = \Delta Q$ , CP cons. not assumed

NODE=S012212

NODE=S012W1

NODE=S012W1

<sup>1</sup> AKHMETSHIN 99 is from a measured branching ratio  $B(K_S^0 \rightarrow \pi e \nu_e) = (7.2 \pm 1.4) \times 10^{-4}$  and  $\tau_{K_S^0} = (0.8934 \pm 0.0008) \times 10^{-10}$  s. Not independent of measured branching ratio.

<sup>2</sup> PDG 98 from  $K_L^0$  measurements, assuming that  $\Delta S = \Delta Q$  in  $K^0$  decay so that  $\Gamma(K_S^0 \rightarrow \pi^\pm e^\mp \nu_e) = \Gamma(K_L^0 \rightarrow \pi^\pm e^\mp \nu_e)$ .

### $\Gamma(\pi^\pm \mu^\mp \nu_\mu)$

VALUE ( $10^6 \text{ s}^{-1}$ )

DOCUMENT ID

$\Gamma_{10}$

• • • We do not use the following data for averages, fits, limits, etc. • • •

5.25  $\pm$  0.07      <sup>1</sup> PDG      98

<sup>1</sup> PDG 98 from  $K_L^0$  measurements, assuming that  $\Delta S = \Delta Q$  in  $K^0$  decay so that  $\Gamma(K_S^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu) = \Gamma(K_L^0 \rightarrow \pi^\pm \mu^\mp \nu_\mu)$ .

NODE=S012W1;LINKAGE=AW

NODE=S012W1;LINKAGE=P8

NODE=S012W2

NODE=S012W2

NODE=S012W2;LINKAGE=P8

NODE=S012215

NODE=S012405

NODE=S012R2

NODE=S012R2

### $K_S^0$ BRANCHING RATIOS

#### Hadronic modes

##### $\Gamma(\pi^0 \pi^0)/\Gamma_{\text{total}}$

VALUE

EVTS

DOCUMENT ID

TECN

$\Gamma_1/\Gamma$

0.3069  $\pm$  0.0005 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.335 $\pm$ 0.014	1066	BROWN	63	HLBC
0.288 $\pm$ 0.021	198	CHRETIEN	63	HLBC
0.30 $\pm$ 0.035		BROWN	61	HLBC

##### $\Gamma(\pi^+ \pi^-)/\Gamma_{\text{total}}$

VALUE

EVTS

DOCUMENT ID

TECN

COMMENT

$\Gamma_2/\Gamma$

0.6920  $\pm$  0.0005 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.670 $\pm$ 0.010	3447	DOYLE	69	HBC $\pi^- p \rightarrow \Lambda K^0$
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NODE=S012R1

NODE=S012R1

##### $\Gamma(\pi^+ \pi^-)/(\pi^0 \pi^0)$

VALUE

EVTS

DOCUMENT ID

TECN

COMMENT

$\Gamma_2/\Gamma_1$

2.255  $\pm$  0.005 OUR FIT

2.2549  $\pm$  0.0054

<sup>1</sup> AMBROSINO 06C KLOE

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.2555 $\pm$ 0.0012 $\pm$ 0.0054		<sup>2</sup> AMBROSINO	06C	KLOE
2.236 $\pm$ 0.003 $\pm$ 0.015	766k	<sup>2</sup> ALOISIO	02B	KLOE
2.11 $\pm$ 0.09	1315	EVERHART	76	WIRE $\pi^- p \rightarrow \Lambda K^0$
2.169 $\pm$ 0.094	16k	COWELL	74	OSPK $\pi^- p \rightarrow \Lambda K^0$
2.16 $\pm$ 0.08	4799	HILL	73	DBC $K^+ d \rightarrow K^0 pp$
2.22 $\pm$ 0.10	3068	<sup>3</sup> ALITTI	72	HBC $K^+ p \rightarrow \pi^+ p K^0$
2.22 $\pm$ 0.08	6380	MORSE	72B	DBC $K^+ n \rightarrow K^0 p$
2.10 $\pm$ 0.11	701	<sup>4</sup> NAGY	72	HLBC $K^+ n \rightarrow K^0 p$
2.22 $\pm$ 0.095	6150	<sup>5</sup> BALTAY	71	HBC $K p \rightarrow K^0_{\text{neutrals}}$
2.282 $\pm$ 0.043	7944	<sup>6</sup> MOFFETT	70	OSPK $K^+ n \rightarrow K^0 p$
2.12 $\pm$ 0.17	267	<sup>4</sup> BOZOKI	69	HLBC
2.285 $\pm$ 0.055	3016	<sup>6</sup> GOBBI	69	OSPK $K^+ n \rightarrow K^0 p$
2.10 $\pm$ 0.06	3700	MORFIN	69	HLBC $K^+ n \rightarrow K^0 p$

NODE=S012R3

NODE=S012R3

OCCUR=2

<sup>1</sup> This result combines AMBROSINO 06C KLOE 2001-02 data with ALOISIO 02B KLOE 2000 data.  $K_S^0 \rightarrow \pi^+ \pi^-$  fully inclusive.

NODE=S012R3;LINKAGE=AM

<sup>2</sup> Includes radiative decays  $\pi^+ \pi^- \gamma$ .

NODE=S012R3;LINKAGE=AL

<sup>3</sup> The directly measured quantity is  $K_S^0 \rightarrow \pi^+ \pi^- / \text{all } K^0 = 0.345 \pm 0.005$ .

NODE=S012R3;LINKAGE=A

<sup>4</sup> NAGY 72 is a final result which includes BOZOKI 69.

NODE=S012R3;LINKAGE=N

<sup>5</sup> The directly measured quantity is  $K_S^0 \rightarrow \pi^+ \pi^- / \text{all } \bar{K}^0 = 0.345 \pm 0.005$ .

NODE=S012R3;LINKAGE=B

<sup>6</sup> MOFFETT 70 is a final result which includes GOBBI 69.

NODE=S012R3;LINKAGE=G

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma_{\text{total}}$				$\Gamma_3/\Gamma$
VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.5<sup>+1.1</sup><sub>-0.9</sub> OUR AVERAGE</b>				
4.7 <sup>+2.2</sup> <sub>-1.7</sub> <sup>+1.7</sup> <sub>-1.5</sub>		1 BATLEY	05	NA48
2.5 <sup>+1.3</sup> <sub>-1.0</sub> <sup>+0.5</sup> <sub>-0.6</sub>	500k	2 ADLER	97B	CPLR
4.8 <sup>+2.2</sup> <sub>-1.6</sub> <sup>+1.1</sup>		3 ZOU	96	E621

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.1 <sup>+2.5</sup> <sub>-1.9</sub> <sup>+0.5</sup> <sub>-0.6</sub>		4 ADLER	96E	CPLR Sup. by ADLER 97B
3.9 <sup>+5.4</sup> <sub>-1.8</sub> <sup>+0.9</sup> <sub>-0.7</sub>		5 THOMSON	94	E621 Sup. by ZOU 96

1 BATLEY 05 is obtained by measuring the interference parameters in  $K_S$ ,  $K_L \rightarrow \pi^+\pi^-\pi^0$ :  $\text{Re}(\lambda) = 0.038 \pm 0.008 \pm 0.006$  and  $\text{Im}(\lambda) = -0.013 \pm 0.005 \pm 0.004$ ; the correlation coeff. between  $\text{Re}(\lambda)$  and  $\text{Im}(\lambda)$  is 0.66 (statistical only).

2 ADLER 97B find the CP-conserving parameters  $\text{Re}(\lambda) = (28 \pm 7 \pm 3) \times 10^{-3}$ ,  $\text{Im}(\lambda) = (-10 \pm 8 \pm 2) \times 10^{-3}$ . They estimate  $B(K_S^0 \rightarrow \pi^+\pi^-\pi^0)$  from  $\text{Re}(\lambda)$  and the  $K_L^0$  decay parameters. See also ANGELOPOULOS 98c.

3 ZOU 96 is from the measured quantities  $|\rho_{+-0}| = 0.039^{+0.009}_{-0.006} \pm 0.005$  and  $\phi_\rho = (-9 \pm 18)^\circ$ .

4 ADLER 96E is from the measured quantities  $\text{Re}(\lambda) = 0.036 \pm 0.010^{+0.002}_{-0.003}$  and  $\text{Im}(\lambda)$  consistent with zero. Note that the quantity  $\lambda$  is the same as  $\rho_{+-0}$  used in other footnotes.

5 THOMSON 94 calculates this branching ratio from their measurements  $|\rho_{+-0}| = 0.035^{+0.019}_{-0.011} \pm 0.004$  and  $\phi_\rho = (-59 \pm 48)^\circ$  where  $|\rho_{+-0}| e^{i\phi_\rho} = A(K_S^0 \rightarrow \pi^+\pi^-\pi^0, I=2) / A(K_L^0 \rightarrow \pi^+\pi^-\pi^0)$ .

### Modes with photons or $\ell\bar{\ell}$ pairs

$\Gamma(\pi^+\pi^-\gamma)/\Gamma(\pi^+\pi^-)$				$\Gamma_4/\Gamma_2$
VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.59<sup>±0.08</sup> OUR AVERAGE</b>				
2.56 $\pm 0.09$	1286	RAMBERG	93	E731 $p_\gamma > 50 \text{ MeV}/c$
2.68 $\pm 0.15$		1 TAUREG	76	SPEC $p_\gamma > 50 \text{ MeV}/c$

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.10 $\pm 0.22$	3723	RAMBERG	93	E731 $p_\gamma > 20 \text{ MeV}/c$
3.0 $\pm 0.6$	29	2 BOBISUT	74	HLBC $p_\gamma > 40 \text{ MeV}/c$
2.8 $\pm 0.6$		3 BURGUN	73	HBC $p_\gamma > 50 \text{ MeV}/c$

1 TAUREG 76 find direct emission contribution  $< 0.06$ , CL = 90%.

2 BOBISUT 74 not included in average because  $p_\gamma$  cut differs. Estimates direct emission contribution to be 0.5 or less, CL = 95%.

3 BURGUN 73 estimates that direct emission contribution is  $0.3 \pm 0.6$ .

$\Gamma(\pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}$				$\Gamma_5/\Gamma$
VALUE (units $10^{-5}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>4.79<sup>±0.15</sup> OUR AVERAGE</b>				

4.83 $\pm 0.11 \pm 0.14$	23k	1 BATLEY	11	NA48 2002 data
4.69 $\pm 0.30$	676	2 LAI	03C	NA48 1998+1999 data

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.71 $\pm 0.23 \pm 0.22$	620	2,3 LAI	03C	NA48 1999 data
4.5 $\pm 0.7 \pm 0.4$	56	LAI	00B	NA48 1998 data

1 BATLEY 11 reports  $[\Gamma(K_S^0 \rightarrow \pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}] / [B(K_L^0 \rightarrow \pi^+\pi^-\pi^0)] / [B(\pi^0 \rightarrow e^+e^-\gamma)] = (3.28 \pm 0.06 \pm 0.04) \times 10^{-2}$  which we multiply by our best values  $B(K_L^0 \rightarrow \pi^+\pi^-\pi^0) = (12.54 \pm 0.05) \times 10^{-2}$ ,  $B(\pi^0 \rightarrow e^+e^-\gamma) = (1.174 \pm 0.035) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best values. Also a limit on the absolute value of the interference between bremsstrahlung and E1 transition is given :  $< 4 \times 10^{-7}$  at 90% C.L.

2 Uses normalization  $BR(K_L \rightarrow \pi^+\pi^-\pi^0) * BR(\pi^0 \rightarrow e^+e^-) = (1.505 \pm 0.047) \times 10^{-3}$  from our 2000 Edition.

3 Second error is  $0.16(\text{syst}) \pm 0.15(\text{norm})$  combined in quadrature.

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NODE=S012R8;LINKAGE=B

NODE=S012410

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OCCUR=2

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NODE=S012R5;LINKAGE=B

NODE=S012R14  
NODE=S012R14

OCCUR=2

NODE=S012R14;LINKAGE=BA

NODE=S012R14;LINKAGE=LA

NODE=S012R14;LINKAGE=LB

$\Gamma(\pi^0 \gamma\gamma)/\Gamma_{\text{total}}$	$\Gamma_6/\Gamma$				
VALUE (units $10^{-8}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>4.9±1.6±0.9</b>		17	1 LAI	04 NA48	$m_{\gamma\gamma}^2/m_K^2 > 0.2$
<33	90	LAI	03B NA48		$m_{\gamma\gamma}^2/m_K^2 > 0.2$

• • • We do not use the following data for averages, fits, limits, etc. • • •

<33 90 LAI 03B NA48  $m_{\gamma\gamma}^2/m_K^2 > 0.2$

1 Spectrum also measured and found consistent with the one generated by a constant matrix element.

$\Gamma(\gamma\gamma)/\Gamma_{\text{total}}$	$\Gamma_7/\Gamma$				
VALUE (units $10^{-6}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT

**2.63 ±0.17 OUR AVERAGE** Error includes scale factor of 3.1.

2.26  $\pm 0.12 \pm 0.06$  711 1 AMBROSINO 08C KLOE  $\phi \rightarrow K_S^0 K_L^0$

2.713 $\pm 0.063 \pm 0.005$  7.5k 2 LAI 03 NA48

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.58 $\pm 0.36 \pm 0.22$	149	LAI	00 NA48
2.2 $\pm 1.1$	16	3 BARR	95B NA31
2.4 $\pm 0.9$	35	4 BARR	95B NA31
< 13	90	BALATS	89 SPEC
2.4 $\pm 1.2$	19	BURKHARDT	87 NA31
<133	90	BARMIN	86B XEBC

1 AMBROSINO 08C reports  $(2.26 \pm 0.12 \pm 0.06) \times 10^{-6}$  from a measurement of  $[\Gamma(K_S^0 \rightarrow \gamma\gamma)/\Gamma_{\text{total}}] \times [B(K_S^0 \rightarrow \pi^0 \pi^0)]$  assuming  $B(K_S^0 \rightarrow \pi^0 \pi^0) = (30.69 \pm 0.05) \times 10^{-2}$ .

2 LAI 03 reports  $[\Gamma(K_S^0 \rightarrow \gamma\gamma)/\Gamma_{\text{total}}] / [B(K_S^0 \rightarrow \pi^0 \pi^0)] = (8.84 \pm 0.18 \pm 0.10) \times 10^{-6}$  which we multiply by our best value  $B(K_S^0 \rightarrow \pi^0 \pi^0) = (30.69 \pm 0.05) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

3 BARR 95B result is calculated using  $B(K_L \rightarrow \gamma\gamma) = (5.86 \pm 0.17) \times 10^{-4}$ .

4 BARR 95B quotes this as the combined BARR 95B + BURKHARDT 87 result after rescaling BURKHARDT 87 to use same branching ratios and lifetimes as BARR 95B.

$\Gamma(\mu^+ \mu^- \mu^+ \mu^-)/\Gamma_{\text{total}}$	$\Gamma_8/\Gamma$			
VALUE	CL%	DOCUMENT ID	TECN	COMMENT
<b>&lt;5.1 × 10<sup>-12</sup></b>	90	1 AAIJ	23AE LHCb	

1 AAIJ 23AE uses  $5.1 \text{ fb}^{-1}$  of LHCb data recorded from 2016 to 2018.

### Semileptonic modes

$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma_{\text{total}}$	$\Gamma_9/\Gamma$			
VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT

**7.14 ±0.06 OUR FIT**

**7.04 ±0.08 OUR AVERAGE**

7.046 $\pm 0.18 \pm 0.16$	1 BATLEY	07D NA48	$K^0 (\bar{K}^0)(t) \rightarrow \pi e \nu$
6.91 $\pm 0.34 \pm 0.15$	624 2 ALOISIO	02 KLOE	Tagged $K_S^0$ using $\phi \rightarrow K_L^0 K_S^0$

• • • We use the following data for averages but not for fits. • • •

7.05  $\pm 0.09$  13k 3 AMBROSINO 06E KLOE Not fitted

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.2  $\pm 1.4$  75 AKHMETSHIN 99 CMD2 Tagged  $K_S^0$  using  $\phi \rightarrow K_L^0 K_S^0$

1 Reconstructed from  $K^0 (\bar{K}^0)(t) \rightarrow \pi e \nu$  distributions using PDG values of  $B(K_L^0 \rightarrow \pi e \nu) = 0.4053 \pm 0.0015$ ,  $\tau_L = (5.114 \pm 0.021) \times 10^{-8} \text{ s}$  and  $\tau_S = (0.8958 \pm 0.0005) \times 10^{-10} \text{ s}$ .

2 Uses the PDG 00 value for  $B(K_S^0 \rightarrow \pi^+ \pi^-)$ .

3 Obtained by imposing  $\sum_i B(K_S^0 \rightarrow i) = 1$ , where  $i$  runs over all the four branching ratios  $\pi^+ \pi^-$ ,  $\pi^0 \pi^0$ ,  $\pi e \nu$ , and  $\pi \mu \nu$ . Input value of  $B(K_S^0 \rightarrow \pi^+ \pi^-) / B(K_S^0 \rightarrow \pi^0 \pi^0)$  from AMBROSINO 06C is used. To derive  $\Gamma(K_S^0 \rightarrow \pi^+ \mu \nu) / \Gamma(K_S^0 \rightarrow \pi^+ e \nu)$ , lepton universality is assumed, radiative corrections from ANDRE 07 are used, and phase space integrals are taken from KTeV, ALEXOPOULOS 04A. This branching fraction enters our fit via their  $\Gamma(\pi^\pm e^\mp \nu_e) / \Gamma(\pi^+ \pi^-)$  branching ratio measurement.

$\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma_{\text{total}}$	$\Gamma_{10}/\Gamma$			
VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT

**4.56±0.20 OUR FIT**

**4.56±0.11±0.17** 7223 1 BABUSCI 20 KLOE direct measurement

1 Value obtained by normalizing to the KLOE measurement  $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.196 \pm 0.051)\%$ . Also comparison with the PDG 18 based derived value leads to a lepton flavor universality test  $|V_{us} f_+(0)|^2_{K_S^0 \rightarrow \pi \mu \nu} / |V_{us} f_+(0)|^2_{K_S^0 \rightarrow \pi e \nu} = 0.975 \pm 0.044$ .

NODE=S012R15  
NODE=S012R15

NODE=S012R15;LINKAGE=LA  
NODE=S012R7  
NODE=S012R7

OCCUR=2

NODE=S012R7;LINKAGE=AM

NODE=S012R7;LINKAGE=LB

NODE=S012R7;LINKAGE=A  
NODE=S012R7;LINKAGE=B

NODE=S012R00  
NODE=S012R00

NODE=S012R00;LINKAGE=A

NODE=S012415

NODE=S012R13  
NODE=S012R13

NOTFITTED

NODE=S012R13;LINKAGE=BA

NODE=S012R13;LINKAGE=A  
NODE=S012R13;LINKAGE=AM

NODE=S012R18  
NODE=S012R18

NODE=S012R18;LINKAGE=A

$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma(\pi^+ \pi^-)$ 

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN
<b>1.032 ± 0.008 OUR FIT</b>			

**1.0338±0.0054±0.0064**      <sup>1</sup> BABUSCI      23    KLOE

• • • We do not use the following data for averages, fits, limits, etc. • • •

$1.019 \pm 0.011 \pm 0.007$     13k      <sup>2</sup> AMBROSINO 06E KLOE

<sup>1</sup> BABUSCI 23 measured  $\Gamma(K_S^0 \rightarrow \pi e \nu)/\Gamma(K_S^0 \rightarrow \pi^+ \pi^-) = (1.0421 \pm 0.0066 \pm 0.0075) \times 10^{-3}$  based on data collected from 2004 to 2005. About 50k signal events were reconstructed from the dataset corresponding to an integrated luminosity of  $1.63 \text{ fb}^{-1}$ . The quoted value is their combination of this result with the previous measurement of AMBROSINO 06E. The correlation coefficient between the two measurements is 12%. <sup>2</sup> AMBROSINO 06E result is included in BABUSCI 23.

 $\Gamma_9/\Gamma_2$ 

NODE=S012R17  
NODE=S012R17

**CP violating (CP) and  $\Delta S = 1$  weak neutral current (S1) modes** $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ 

Violates CP conservation.

VALUE (units $10^{-7}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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< **0.26**    90    590M      <sup>1</sup> BABUSCI      13C    KLOE     $\phi \rightarrow K_L^0 K_S^0$

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 1.2    90    37.8M      AMBROSINO 05B KLOE  
< 7.4    90    4.9M      <sup>2</sup> LAI      05A NA48  
<140    90    7M      ACHASOV      99D SND  
<190    90    17300      <sup>3</sup> ANGELOPO... 98B CPLR  
<370    90    BARMIN      83    HLBC

<sup>1</sup> BABUSCI 13C uses  $1.7 \text{ fb}^{-1}$  of data of  $\phi \rightarrow K_L^0 K_S^0$  decays with  $K_L^0$  interaction in the calorimeter, collected from 2004 to 2005. No candidate events were found in the data with an expected background of  $0.04^{+0.15}_{-0.03}$  events. Upper limit is obtained by normalizing to  $K_S^0 \rightarrow 2\pi^0$  decays.

<sup>2</sup> LAI 05A value is obtained from their bound on  $|\eta_{000}|$  (not assuming CPT) and  $B(K_L^0 \rightarrow 3\pi^0) = 0.211 \pm 0.003$ , and PDG 04 values for  $K_L^0$  and  $K_S^0$  lifetimes. If CPT is assumed then  $B(K_S^0 \rightarrow 3\pi^0)_{CPT} < 2.3 \times 10^{-7}$  at 90% CL

<sup>3</sup> ANGELOPOULOS 98B is from  $\text{Im}(\eta_{000}) = -0.05 \pm 0.12 \pm 0.05$ , assuming  $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$  and using the value  $B(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0) = 0.2112 \pm 0.0027$ .

 $\Gamma_{11}/\Gamma$ 

NODE=S012R17;LINKAGE=A

NODE=S012R17;LINKAGE=B

NODE=S012420

NODE=S012R9  
NODE=S012R9  
NODE=S012R9

 $\Gamma(\mu^+ \mu^-)/\Gamma_{\text{total}}$ 

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE	CL%	DOCUMENT ID	TECN
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<**2.1 × 10<sup>-10</sup>**    90    <sup>1</sup> AAIJ      20AE LHCb

• • • We do not use the following data for averages, fits, limits, etc. • • •

<8 × 10<sup>-10</sup>    90    <sup>2</sup> AAIJ      17BQ LHCb  
<9 × 10<sup>-9</sup>    90    <sup>3</sup> AAIJ      13G LHCb  
<3.2 × 10<sup>-7</sup>    90    GJESDAL      73 ASPK  
<7 × 10<sup>-6</sup>    90    HYAMS      69B OSPK

<sup>1</sup> AAIJ 20AE uses  $8.6 \text{ fb}^{-1}$  of LHCb data from 2011 to 2012 and 2016 to 2018. The result utilizes the normalization mode branching fraction  $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$  from PDG 18. Supersedes AAIJ 17BQ.

<sup>2</sup> AAIJ 17BQ uses  $3.0 \text{ fb}^{-1}$  of  $p p$  collisions at  $\sqrt{s} = 7$  and  $8 \text{ TeV}$ . The result utilizes the normalization mode branching fraction  $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$  from PDG 16. Supersedes AAIJ 13G.

<sup>3</sup> AAIJ 13G uses  $1.0 \text{ fb}^{-1}$  of  $p p$  collisions at  $\sqrt{s} = 7 \text{ TeV}$ . They obtained  $B(K_S^0 \rightarrow \mu^+ \mu^-) < 11 \times 10^{-9}$  at 95% C.L.

 $\Gamma_{12}/\Gamma$ 

NODE=S012R9;LINKAGE=B

NODE=S012R9;LINKAGE=LA

NODE=S012R9;LINKAGE=A

NODE=S012R11

NODE=S012R11

NODE=S012R11

NODE=S012R11;LINKAGE=B

NODE=S012R11;LINKAGE=A

NODE=S012R11;LINKAGE=AA

NODE=S012R12

NODE=S012R12

NODE=S012R12

 $\Gamma(e^+ e^-)/\Gamma_{\text{total}}$ 

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE (units $10^{-7}$ )	CL%	DOCUMENT ID	TECN	COMMENT
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< **0.09**    90    <sup>1</sup> AMBROSINO 09A KLOE     $e^+ e^- \rightarrow \phi \rightarrow K_S^0 K_L^0$

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 1.4    90    ANGELOPO... 97 CPLR  
< 28    90    BLICK      94 CNTR Hyperon facility  
<100    90    BARMIN      86 XEBC

<sup>1</sup> AMBROSINO 09A reports  $< 0.09 \times 10^{-7}$  from a measurement of  $[\Gamma(K_S^0 \rightarrow e^+ e^-)/\Gamma_{\text{total}}]/[B(K_S^0 \rightarrow \pi^+ \pi^-)]$  assuming  $B(K_S^0 \rightarrow \pi^+ \pi^-) = (69.20 \pm 0.05) \times 10^{-2}$ .

NODE=S012R12

NODE=S012R12

NODE=S012R12

NODE=S012R12;LINKAGE=AM

$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$ 

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>3.0^{+1.5}_{-1.2} \pm 0.2</math></b>		7	1 BATLEY	03	NA48 $m_{ee} > 0.165$ GeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 140	90	LAI	01	NA48
< 1100	90	0	BARR	93B NA31
< 45000	90		GIBBONS	88 E731

<sup>1</sup> BATLEY 03 extrapolate also to the full kinematical region using a constant form factor and a vector matrix element. The resulting branching ratio is  $(5.8^{+2.9}_{-2.4}) \times 10^{-9}$ .

 $\Gamma(\pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$ 

Test for  $\Delta S = 1$  weak neutral current. Allowed by first-order weak interaction combined with electromagnetic interaction.

VALUE (units $10^{-9}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>2.9^{+1.5}_{-1.2} \pm 0.2</math></b>	6	1 BATLEY	04A	NA48/1 $K_S^0$ beam

<sup>1</sup> Background estimate is  $0.22^{+0.18}_{-0.11}$  events. Branching ratio assumes a vector matrix element and unit form factor.

 $\Gamma_{14}/\Gamma$ 

NODE=S012R10

NODE=S012R10

NODE=S012R10

NODE=S012R10;LINKAGE=BA

NODE=S012R16

NODE=S012R16

NODE=S012R16

NODE=S012R16;LINKAGE=BA

NODE=S012240

NODE=S012240

NODE=S012L+E

NODE=S012L+E

NODE=S012219

 $K_S^0$  FORM FACTORS

For discussion, see note on  $K_{\ell 3}$  form factors in the  $K^\pm$  section of the Particle Listings above. Because the semileptonic branching fraction is smaller in  $K_S^0$  than  $K_L^0$  by the ratio of the mean lives, the  $K_S^0$  semileptonic form factor has so far been measured only in the  $K_{e3}$  mode using the linear expansion  $f_+(t) = f_+(0) (1 + \lambda_+ t / m_{\pi^+}^2)$ , which gives the vector form factor  $f_+(t)$  relative to its value at  $t = 0$ .

 $\lambda_+$  (LINEAR ENERGY DEPENDENCE OF  $f_+$  IN  $K_{e3}^0$  DECAY)

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN
<b><math>3.39 \pm 0.41</math></b>	15k	AMBROSINO	06E KLOE

 $CP$  VIOLATION IN  $K_S \rightarrow 3\pi$ 

Written 1996 by T. Nakada (Paul Scherrer Institute) and L. Wolfenstein (Carnegie-Mellon University).

The possible final states for the decay  $K^0 \rightarrow \pi^+ \pi^- \pi^0$  have isospin  $I = 0, 1, 2$ , and  $3$ . The  $I = 0$  and  $I = 2$  states have  $CP = +1$  and  $K_S$  can decay into them without violating  $CP$  symmetry, but they are expected to be strongly suppressed by centrifugal barrier effects. The  $I = 1$  and  $I = 3$  states, which have no centrifugal barrier, have  $CP = -1$  so that the  $K_S$  decay to these requires  $CP$  violation.

In order to see  $CP$  violation in  $K_S \rightarrow \pi^+ \pi^- \pi^0$ , it is necessary to observe the interference between  $K_S$  and  $K_L$  decay, which determines the amplitude ratio

$$\eta_{+-0} = \frac{A(K_S \rightarrow \pi^+ \pi^- \pi^0)}{A(K_L \rightarrow \pi^+ \pi^- \pi^0)}. \quad (1)$$

If  $\eta_{+-0}$  is obtained from an integration over the whole Dalitz plot, there is no contribution from the  $I = 0$  and  $I = 2$  final

states and a nonzero value of  $\eta_{+-0}$  is entirely due to  $CP$  violation.

Only  $I = 1$  and  $I = 3$  states, which are  $CP = -1$ , are allowed for  $K^0 \rightarrow \pi^0 \pi^0 \pi^0$  decays and the decay of  $K_S$  into  $3\pi^0$  is an unambiguous sign of  $CP$  violation. Similarly to  $\eta_{+-0}$ ,  $\eta_{000}$  is defined as

$$\eta_{000} = \frac{A(K_S \rightarrow \pi^0 \pi^0 \pi^0)}{A(K_L \rightarrow \pi^0 \pi^0 \pi^0)}. \quad (2)$$

If one assumes that  $CPT$  invariance holds and that there are no transitions to  $I = 3$  (or to nonsymmetric  $I = 1$  states), it can be shown that

$$\begin{aligned} \eta_{+-0} &= \eta_{000} \\ &= \epsilon + i \frac{\text{Im } a_1}{\text{Re } a_1}. \end{aligned} \quad (3)$$

With the Wu-Yang phase convention,  $a_1$  is the weak decay amplitude for  $K^0$  into  $I = 1$  final states;  $\epsilon$  is determined from  $CP$  violation in  $K_L \rightarrow 2\pi$  decays. The real parts of  $\eta_{+-0}$  and  $\eta_{000}$  are equal to  $\text{Re}(\epsilon)$ . Since currently-known upper limits on  $|\eta_{+-0}|$  and  $|\eta_{000}|$  are much larger than  $|\epsilon|$ , they can be interpreted as upper limits on  $\text{Im}(\eta_{+-0})$  and  $\text{Im}(\eta_{000})$  and so as limits on the  $CP$ -violating phase of the decay amplitude  $a_1$ .

### CP-VIOLATION PARAMETERS IN $K_S^0$ DECAY

$$A_S = [\Gamma(K_S^0 \rightarrow \pi^- e^+ \nu_e) - \Gamma(K_S^0 \rightarrow \pi^+ e^- \bar{\nu}_e)] / \text{SUM}$$

Such asymmetry violates  $CP$ . If  $CPT$  is assumed then  $A_S = 2 \text{ Re}(\epsilon)$ .

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN
<b><math>-3.8 \pm 5.0 \pm 2.6</math></b>	83k	<sup>1</sup> ANASTASI	18A KLOE

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.5  $\pm$  9.6  $\pm$  2.9      13k      AMBROSINO 06E KLOE

<sup>1</sup> ANASTASI 18A result is a combination of the new measurement and AMBROSINO 06E.

The new ANASTASI 18A measurement using data collected from 2004–2005, which corresponds to an integrated luminosity of  $1.63 \text{ fb}^{-1}$  is  $A_S = (-4.9 \pm 5.7 \pm 2.6) \times 10^{-3}$ .

NODE=S012250

NODE=S012AS

NODE=S012AS

NODE=S012AS

NODE=S012AS;LINKAGE=B

NODE=S012220

NODE=S012ET+

NODE=S012ET+

NODE=S012ET+

$$\text{Im}(\eta_{+-0})^2 = \Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, \text{CP-violating}) / \Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$$

$CPT$  assumed valid (i.e.  $\text{Re}(\eta_{+-0}) \simeq 0$ ).

VALUE	CL%	EVTS	DOCUMENT ID	TECN
<0.23	90	601	<sup>1</sup> BARMIN	85 HLBC
<0.12	90	384	METCALF	72 ASPK

<sup>1</sup> BARMIN 85 find  $\text{Re}(\eta_{+-0}) = (0.05 \pm 0.17)$  and  $\text{Im}(\eta_{+-0}) = (0.15 \pm 0.33)$ . Includes events of BALDO-CEOLIN 75.

NODE=S012ET+;LINKAGE=B

$$\text{Im}(\eta_{+-0}) = \text{Im}(A(K_S^0 \rightarrow \pi^+ \pi^- \pi^0, \text{CP-violating}) / A(K_L^0 \rightarrow \pi^+ \pi^- \pi^0))$$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
$-0.002 \pm 0.009^{+0.002}_{-0.001}$	500k	1 ADLER	97B CPLR	

• • • We do not use the following data for averages, fits, limits, etc. • • •

$-0.002 \pm 0.018 \pm 0.003$	137k	2 ADLER	96D CPLR	Sup. by ADLER 97B
$-0.015 \pm 0.017 \pm 0.025$	272k	3 ZOU	94 SPEC	

1 ADLER 97B also find  $\text{Re}(\eta_{+-0}) = -0.002 \pm 0.007^{+0.004}_{-0.001}$ . See also ANGELOPOULOS 98C.

2 The ADLER 96D fit also yields  $\text{Re}(\eta_{+-0}) = 0.006 \pm 0.013 \pm 0.001$  with a correlation +0.66 between real and imaginary parts. Their results correspond to  $|\eta_{+-0}| < 0.037$  with 90% CL.

3 ZOU 94 use theoretical constraint  $\text{Re}(\eta_{+-0}) = \text{Re}(\epsilon) = 0.0016$ . Without this constraint they find  $\text{Im}(\eta_{+-0}) = 0.019 \pm 0.061$  and  $\text{Re}(\eta_{+-0}) = 0.019 \pm 0.027$ .

$$\text{Im}(\eta_{000})^2 = \Gamma(K_S^0 \rightarrow 3\pi^0) / \Gamma(K_L^0 \rightarrow 3\pi^0)$$

CPT assumed valid (i.e.  $\text{Re}(\eta_{000}) \simeq 0$ ). This limit determines branching ratio  $\Gamma(3\pi^0)/\Gamma_{\text{total}}$  above.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<0.1	90	632	1 BARMIN	83 HLBC	

<0.28	90	2 GJESDAL	74B SPEC	Indirect meas.
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1 BARMIN 83 find  $\text{Re}(\eta_{000}) = (-0.08 \pm 0.18)$  and  $\text{Im}(\eta_{000}) = (-0.05 \pm 0.27)$ . Assuming CPT invariance they obtain the limit quoted above.

2 GJESDAL 74B uses  $K2\pi$ ,  $K_{\mu 3}$ , and  $K_{e3}$  decay results, unitarity, and CPT. Calculates  $|\eta_{000}| = 0.26 \pm 0.20$ . We convert to upper limit.

$$\text{Im}(\eta_{000}) = \text{Im}(A(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0) / A(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0))$$

$K_S^0 \rightarrow \pi^0 \pi^0 \pi^0$  violates CP conservation, in contrast to  $K_S^0 \rightarrow \pi^+ \pi^- \pi^0$  which has a CP-conserving part.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>-0.001 \pm 0.016</math> OUR AVERAGE</b>				
0.000 $\pm 0.009 \pm 0.013$	4.9M	1 LAI	05A NA48	Assumes CPT

-0.05 $\pm 0.12 \pm 0.05$	17300	2 ANGELOPO... 98B	CPLR	Assumes CPT
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1 LAI 05A assumes  $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.66 \times 10^{-3}$ . The equivalent limit is  $|\eta_{000}|_{\text{CPT}} < 0.025$  at 90% CL. Without assuming CPT invariance, they obtain  $\text{Re}(\eta_{000}) = -0.002 \pm 0.011 \pm 0.015$  and  $\text{Im}(\eta_{000}) = -0.003 \pm 0.013 \pm 0.017$  with a statistical correlation coefficient of 0.77 and an overall correlation coefficient of 0.57 between imaginary and real part. The equivalent limit is  $|\eta_{000}| < 0.045$  at 90% CL

2 ANGELOPOULOS 98B assumes  $\text{Re}(\eta_{000}) = \text{Re}(\epsilon) = 1.635 \times 10^{-3}$ . Without assuming CPT invariance, they obtain  $\text{Re}(\eta_{000}) = 0.18 \pm 0.14 \pm 0.06$  and  $\text{Im}(\eta_{000}) = 0.15 \pm 0.20 \pm 0.03$ .

$$|\eta_{000}| = |A(K_S^0 \rightarrow 3\pi^0) / A(K_L^0 \rightarrow 3\pi^0)|$$

A non-zero value violates CP invariance.

VALUE	CL%	EVTS	DOCUMENT ID	TECN
<b>&lt;0.0088</b>	90	590M	BABUSCI	13C KLOE

• • • We do not use the following data for averages, fits, limits, etc. • • •

<0.018	90	37.8M	AMBROSINO	05B KLOE
<0.045	90	4.9M	LAI	05A NA48

### DECAY-PLANE ASYMMETRY IN $\pi^+ \pi^- e^+ e^-$ DECAYS

This is the CP-violating asymmetry

$$A = \frac{N_{\sin\phi \cos\phi > 0.0} - N_{\sin\phi \cos\phi < 0.0}}{N_{\sin\phi \cos\phi > 0.0} + N_{\sin\phi \cos\phi < 0.0}}$$

where  $\phi$  is the angle between the  $e^+ e^-$  and  $\pi^+ \pi^-$  planes in the  $K_S^0$  rest frame.

$$\text{CP asymmetry } A \text{ in } K_S^0 \rightarrow \pi^+ \pi^- e^+ e^-$$

VALUE (%)	DOCUMENT ID	TECN	COMMENT
<b><math>-0.4 \pm 0.8</math> OUR AVERAGE</b>			
-0.4 $\pm 0.8$	1 BATLEY	11 NA48	2002 data
-1.1 $\pm 4.1$	LAI	03C NA48	1998+1999 data

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.5 $\pm 4.0 \pm 1.6$	LAI	03C NA48	1999 data
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1 The result is used to set the limit  $A < 1.5\%$  at 90% C.L.

NODE=S012E+

NODE=S012E+

NODE=S012E+;LINKAGE=C

NODE=S012E+;LINKAGE=B

NODE=S012E+;LINKAGE=A

NODE=S012ET0

NODE=S012ET0

NODE=S012ET0

NODE=S012ET0;LINKAGE=B

NODE=S012ET0;LINKAGE=G

NODE=S012E0

NODE=S012E0

NODE=S012E0

NODE=S012E0;LINKAGE=LA

NODE=S012E0;LINKAGE=A

NODE=S012AE0

NODE=S012AE0

NODE=S012AE0

NODE=S012230

NODE=S012230

NODE=S012DPA

NODE=S012DPA

OCCUR=2

NODE=S012DPA;LINKAGE=BA

## K<sub>S</sub><sup>0</sup> REFERENCES

NODE=S012

AAIJ	23AE	PR D108 L031102	R. Aaij <i>et al.</i>	(LHCb Collab.)	REFID=62337
BABUSCI	23	JHEP 2302 098	D. Babusci <i>et al.</i>	(KLOE-2 Collab.)	REFID=62108
AAIJ	20AE	PRL 125 231801	R. Aaij <i>et al.</i>	(LHCb Collab.)	REFID=60699
BABUSCI	20	PL B804 135378	D. Babusci <i>et al.</i>	(KLOE-2 Collab.)	REFID=60393
ANASTASI	18A	JHEP 1809 021	A. Anastasi <i>et al.</i>	(KLOE-2 Collab.)	REFID=59251
PDG	18	PR D98 030001	M. Tanabashi <i>et al.</i>	(PDG Collab.)	REFID=59304
AAIJ	17BQ	EPJ C77 678	R. Aaij <i>et al.</i>	(LHCb Collab.)	REFID=58357
PDG	16	CP 40 100001	C. Patrignani <i>et al.</i>	(PDG Collab.)	REFID=57140
AAIJ	13G	JHEP 1301 090	R. Aaij <i>et al.</i>	(LHCb Collab.)	REFID=54858
BABUSCI	13C	PL B723 54	D. Babusci <i>et al.</i>	(KLOE-2 Collab.)	REFID=55083
ABOUZAID	11	PR D83 092001	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)	REFID=53712
AMBROSINO	11	EPJ C71 1604	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=16403
BATLEY	11	PL B694 301	J.R. Batley <i>et al.</i>	(CERN NA48/1 Collab.)	REFID=53568
AMBROSINO	09A	PL B672 203	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=52835
AMBROSINO	08C	JHEP 0805 051	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=52321
ANDRE	07	ANP 322 2518	T. Andre	(EFI)	REFID=50524
BATLEY	07D	PL B653 145	J.R. Batley <i>et al.</i>	(CERN NA48 Collab.)	REFID=51876
AMBROSINO	06C	EPJ C48 767	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=51068
AMBROSINO	06E	PL B636 173	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=51073
AMBROSINO	05B	PL B619 61	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=50682
BATLEY	05	PL B630 31	J.R. Batley <i>et al.</i>	(NA48 Collab.)	REFID=50953
LAI	05A	PL B610 165	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=50509
ALEXOPOU...	04A	PR D70 092007	T. Alexopoulos <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50243
BATLEY	04A	PL B599 197	J.R. Batley <i>et al.</i>	(NA48 Collab.)	REFID=50127
LAI	04	PL B578 276	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49654
PDG	04	PL B592 1	S. Eidelman <i>et al.</i>	(PDG Collab.)	REFID=49653
ALAVI-HARATI	03	PR D67 012005	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=49244
Also		PR D70 079904 (errat.)	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50236
BATLEY	03	PL B576 43	J.R. Batley <i>et al.</i>	(CERN NA48 Collab.)	REFID=49534
LAI	03	PL B551 7	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49148
LAI	03B	PL B556 105	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49257
LAI	03C	EPJ C30 33	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49502
ALOISIO	02	PL B535 37	A. Aloisio <i>et al.</i>	(KLOE Collab.)	REFID=48727
ALOISIO	02B	PL B538 21	A. Aloisio <i>et al.</i>	(KLOE Collab.)	REFID=48770
LAI	02C	PL B537 28	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=48765
LAI	01	PL B514 253	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=48191
LAI	00	PL B493 29	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=47830
LAI	00B	PL B496 137	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=47921
PDG	00	EPJ C15 1	D.E. Groom <i>et al.</i>	(PDG Collab.)	REFID=47469
ACHASOV	99D	PL B459 674	M.N. Achasov <i>et al.</i>	(Novosibirsk CMD-2 Collab.)	REFID=47048
AKHMETSHIN	99	PL B456 90	R.R. Akhmetshin <i>et al.</i>	(CPLEAR Collab.)	REFID=47032
ANGELOPO...	98B	PL B425 391	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46084
ANGELOPO...	98C	EPJ C5 389	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46264
PDG	98	EPJ C3 1	C. Caso <i>et al.</i>	(PDG Collab.)	REFID=45838
ADLER	97B	PL B407 193	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=45617
ANGELOPO...	97	PL B413 232	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=45750
BERTANZA	97	ZPHY C73 629	L. Bertanza <i>(PISA, CERN, EDIN, MAINZ, ORSAY+)</i>	(PISA, CERN, EDIN, MAINZ, ORSAY+)	REFID=45296
ADLER	96D	PL B370 167	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44839
ADLER	96E	PL B374 313	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44892
ZOU	96	PL B369 362	Y. Zou <i>et al.</i>	(RUTG, MINN, MICH)	REFID=44835
BARR	95B	PL B351 579	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=44282
SCHWINGEN...	95	PRL 74 4376	B. Schwingerheuer <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=44259
BLICK	94	PL B334 234	A.M. Blick <i>et al.</i>	(SERP, JINR)	REFID=43957
THOMSON	94	PL B337 411	G.B. Thomson <i>et al.</i>	(RUTG, MINN, MICH)	REFID=44020
ZOU	94	PL B329 519	Y. Zou <i>et al.</i>	(RUTG, MINN, MICH)	REFID=43893
BARR	93B	PL B304 381	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=43338
GIBBONS	93	PRL 70 1199	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=43209
Also		PR D55 6625	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=45465
RAMBERG	93	PRL 70 2525	E. Ramberg <i>et al.</i>	(FNAL E731 Collab.)	REFID=43263
BALATS	89	SJNP 49 828	M.Y. Balats <i>et al.</i>	(ITEP)	REFID=40977
GIBBONS	88	Translated from YAF 49 1332	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=40624
BURKHARDT	87	PL B199 139	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MAINZ+)	REFID=40237
GROSSMAN	87	PRL 59 18	N. Grossman <i>et al.</i>	(MINN, MICH, RUTG)	REFID=40230
BARMIN	86	SJNP 44 622	V.V. Barmin <i>et al.</i>	(ITEP)	REFID=40228
BARMIN	86B	NC 96A 159	V.V. Barmin <i>et al.</i>	(ITEP, PADO)	REFID=40231
PDG	86B	PL 170B 130	M. Aguilar-Benitez <i>et al.</i>	(CERN, CIT+)	REFID=41168
BARMIN	85	NC 85A 67	V.V. Barmin <i>et al.</i>	(ITEP, PADO)	REFID=11119
Also		SJNP 41 759	V.V. Barmin <i>et al.</i>	(ITEP)	REFID=11120
BARMIN	83	Translated from YAF 41 1187	V.V. Barmin <i>et al.</i>	(ITEP, PADO)	REFID=11117
Also		PL 128B 129	V.V. Barmin <i>et al.</i>	(ITEP, PADO)	REFID=11118
BARMIN	83	SJNP 39 269	V.V. Barmin <i>et al.</i>	(ITEP, PADO)	REFID=11117
TRANSLATED FROM YAF 39 428					REFID=11118
ARONSON	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)	REFID=11411
ARONSON	82B	PRL 48 1306	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11401
Also		PL 116B 73	E. Fischbach <i>et al.</i>	(PURD, BNL, CHIC)	REFID=11402
Also		PR D28 476	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11403
Also		PR D28 495	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11404
ARONSON	76	NC 32A 236	S.H. Aronson <i>et al.</i>	(WISC, EFI, UCSD+)	REFID=11110
EVERHART	76	PR D14 661	G.C. Everhart <i>et al.</i>	(PENN)	REFID=11111
TAUREG	76	PL 65B 92	H. Taureg <i>et al.</i>	(HEIDH, CERN, DORT)	REFID=11112
BALDO...	75	NC 25A 688	M. Baldo-Ceolin <i>et al.</i>	(PADO, WISC)	REFID=11108
CARITHERS	75	PRL 34 1244	W.C.J. Carithers <i>et al.</i>	(COLU, NYU)	REFID=11109
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COWELL	74	PR D10 2083	P.L. Cowell <i>et al.</i>	(STON, COLU)	REFID=11105
GEWENIGER	74B	PL 48B 487	C. Geweniger <i>et al.</i>	(CERN, HEIDH)	REFID=11357
GJESDAL	74B	PL 52B 119	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)	REFID=11358
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GESDAL	73	PL 44B 217	S. Gjesdal <i>et al.</i>	(SACL, CERN)	REFID=11101
HILL	73	PR D8 1290	D.G. Hill <i>et al.</i>	(BNL, CMU)	REFID=11102
ALITTI	72	PL 39B 568	J. Alitti, E. Lesquoy, A. Muller	(SACL)	REFID=11088
BURGUN	72	NP B50 194	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)	REFID=11306
METCALF	72	PL 40B 703	M. Metcalf <i>et al.</i>	(CERN, IPN, WIEN)	REFID=11092
MORSE	72B	PRL 28 388	R. Morse <i>et al.</i>	(COLO, PRIN, UMD)	REFID=11093
NAGY	72	NP B47 94	E. Nagy, F. Telszisz, G. Vesztorgombi	(BUDA)	REFID=11094
Also		PL 30B 498	G. Bozoki <i>et al.</i>	(BUDA)	REFID=11095
SKJEGGEST...	72	NP B48 343	O. Skjeggestad <i>et al.</i>	(OSLO, CERN, SACL)	REFID=11096
BALTYAY	71	PRL 27 1678	C. Baltay <i>et al.</i>	(COLU)	REFID=11082
Also		Thesis Nevis 187	W.A. Cooper	(COLU)	REFID=11083
MOFFETT	70	BAPS 15 512	R. Moffett <i>et al.</i>	(ROCH)	REFID=11079
BOZOKI	69	PL 30B 498	G. Bozoki <i>et al.</i>	(BUDA)	REFID=11095
DOYLE	69	Thesis UCRL 18139	J.C. Doyle	(LRL)	REFID=11074
GOBBI	69	PRL 22 682	B. Gobbi <i>et al.</i>	(ROCH)	REFID=11075
HYAMS	69B	PL 29B 521	B.D. Hyams <i>et al.</i>	(CERN, MPIM)	REFID=11076
MORFIN	69	PRL 23 660	J.G. Morfin, D. Sinclair	(MICH)	REFID=11077
DONALD	68B	PL 27B 58	R.A. Donald <i>et al.</i>	(LIVP, CERN, IPNP+)	REFID=11069
HILL	68	PR 171 1418	D.G. Hill <i>et al.</i>	(BNL, CMU)	REFID=11070
AUBERT	65	PL 177 59	B. Aubert <i>et al.</i>	(EPOLE, ORSAY)	REFID=11151
BROWN	63	PR 130 769	J.L. Brown <i>et al.</i>	(LRL, MICH)	REFID=11057
CHRETIEN	63	PR 131 2208	M. Chretien <i>et al.</i>	(BRAN, BROW, HARV+)	REFID=11056
BROWN	61	NC 19 1155	J.L. Brown <i>et al.</i>	(MICH)	REFID=11053
BOLDT	58B	PRL 1 150	E. Boldt, D.O. Caldwell, Y. Pal	(MIT)	REFID=11048

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