



$$I(J^P) = \frac{1}{2}(0^-)$$

$$m_{K_L^0} - m_{K_S^0}$$

For earlier measurements, beginning with GOOD 61 and FITCH 61, see our 1986 edition, Physics Letters **170B** 132 (1986).

OUR FIT is described in the note on "CP violation in  $K_L$  decays" in the  $K_L^0$  Particle Listings. The result labeled "OUR FIT Assuming CPT" ["OUR FIT Not assuming CPT"] includes all measurements except those with the comment "Not assuming CPT" ["Assuming CPT"]. Measurements with neither comment do not assume CPT and enter both fits.

VALUE ( $10^{10} \text{ s}^{-1}$ )	DOCUMENT ID	TECN	COMMENT
<b>0.5293 ± 0.0009 OUR FIT</b>			Error includes scale factor of 1.3. Assuming CPT
<b>0.5289 ± 0.0010 OUR FIT</b>			Not assuming CPT
0.52797 ± 0.00195	1,2 ABOUZAID	11 KTEV	Not assuming CPT
0.52699 ± 0.00123	1,3 ABOUZAID	11 KTEV	Assuming CPT
0.5240 ± 0.0044 ± 0.0033	APOSTOLA...	99C CPLR	$K^0 - \bar{K}^0$ to $\pi^+ - \pi^-$
0.5297 ± 0.0030 ± 0.0022	4 SCHWINGEN...	95 E773	20–160 GeV $K$ beams
0.5286 ± 0.0028	5 GIBBONS	93 E731	Assuming CPT
0.5257 ± 0.0049 ± 0.0021	4 GIBBONS	93C E731	Not assuming CPT
0.5340 ± 0.00255 ± 0.0015	6 GEWENIGER	74C SPEC	Gap method
0.5334 ± 0.0040 ± 0.0015	6,7 GJESDAL	74 SPEC	Assuming CPT
• • • We do not use the following data for averages, fits, limits, etc. • • •			
0.5261 ± 0.0015	8 ALAVI-HARATI03	KTEV	Assuming CPT
0.5288 ± 0.0043	9 ALAVI-HARATI03	KTEV	Not assuming CPT
0.5343 ± 0.0063 ± 0.0025	10 ANGELOPO...	01 CPLR	
0.5295 ± 0.0020 ± 0.0003	11 ANGELOPO...	98D CPLR	Assuming CPT
0.5307 ± 0.0013	12 ADLER	96C RVUE	
0.5274 ± 0.0029 ± 0.0005	11 ADLER	95 CPLR	Sup. by ANGELOPOU-LOS 98D
0.482 ± 0.014	13 ARONSON	82B SPEC	$E=30-110$ GeV
0.534 ± 0.007	14 CARNEGIE	71 ASPK	Gap method
0.542 ± 0.006	14 ARONSON	70 ASPK	Gap method
0.542 ± 0.006	CULLEN	70 CNTR	

<sup>1</sup> The two ABOUZAID 11 values use the same data. The first enters the "assuming CPT" fit and the second enters the "not assuming CPT" fit.

<sup>2</sup> ABOUZAID 11 fit has  $\Delta m$ ,  $\tau_s$ ,  $\phi_\epsilon$ ,  $\text{Re}(\epsilon'/\epsilon)$ , and  $\text{Im}(\epsilon'/\epsilon)$  as free parameters. See  $\text{Im}(\epsilon'/\epsilon)$  in the " $K_L^0$  CP violation" section for correlation information.

<sup>3</sup> ABOUZAID 11 fit has  $\Delta m$  and  $\tau_s$  free but constrains  $\phi_\epsilon$  to the Superweak value, i.e. assumes CPT. See " $K_S^0$  Mean Life" section for correlation information.

<sup>4</sup> Fits  $\Delta m$  and  $\phi_{+-}$  simultaneously. GIBBONS 93C systematic error is from B. Weinstein via private communication. 20–160 GeV  $K$  beams.

<sup>5</sup> GIBBONS 93 value assume  $\phi_{+-} = \phi_{00} = \phi_{SW} = (43.7 \pm 0.2)^\circ$ , i.e. assumes CPT. 20–160 GeV  $K$  beams.

<sup>6</sup> These two experiments have a common systematic error due to the uncertainty in the momentum scale, as pointed out in WAHL 89.

<sup>7</sup> GJESDAL 74 uses charge asymmetry in  $K_{l3}^0$  decays.

<sup>8</sup> ALAVI-HARATI 03 fit  $\Delta m$  and  $\tau_{K_S^0}$  simultaneously.  $\phi_{+-}$  is constrained to the Superweak value, i.e. CPT is assumed. See " $K_S^0$  Mean Life" section for correlation information. Superseded by ABOUZAID 11.

<sup>9</sup> ALAVI-HARATI 03 fit  $\Delta m$ ,  $\phi_{+-}$ , and  $\tau_{K_S^0}$  simultaneously. See  $\phi_{+-}$  in the " $K_L$  CP violation" section for correlation information. Superseded by ABOUZAID 11.

<sup>10</sup> ANGELOPOULOS 01 uses strong interactions strangeness tagging at two different times.

<sup>11</sup> Uses  $\bar{K}_{e3}^0$  and  $K_{e3}^0$  strangeness tagging at production and decay. Assumes CPT conservation on  $\Delta S = -\Delta Q$  transitions.

<sup>12</sup> ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value above.

<sup>13</sup> ARONSON 82 find that  $\Delta m$  may depend on the kaon energy.

<sup>14</sup> ARONSON 70 and CARNEGIE 71 use  $K_S^0$  mean life =  $(0.862 \pm 0.006) \times 10^{-10}$  s. We have not attempted to adjust these values for the subsequent change in the  $K_S^0$  mean life or in  $\eta_{+-}$ .

NODE=S013

NODE=S013D

NODE=S013D

NODE=S013D

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OCCUR=2;TYPE=CPTTYPE=CPT  
TYPE=noCPT  
SYCLP=A  
SYCLP=A;TYPE=CPTTYPE=CPT  
OCCUR=2;TYPE=noCPT

TYPE=CPT

NODE=S013D;LINKAGE=AB

NODE=S013D;LINKAGE=AO

NODE=S013D;LINKAGE=AU

NODE=S013D;LINKAGE=CG

NODE=S013D;LINKAGE=GB

NODE=S013D;LINKAGE=G

NODE=S013D;LINKAGE=GJ

NODE=S013D;LINKAGE=VI

NODE=S013D;LINKAGE=S3

NODE=S013D;LINKAGE=AG

NODE=S013D;LINKAGE=X1

NODE=S013D;LINKAGE=Y1

NODE=S013D;LINKAGE=Z

NODE=S013D;LINKAGE=R

## $K_L^0$ MEAN LIFE

VALUE ( $10^{-8}$ s)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>5.116±0.021 OUR FIT</b>		Error includes scale factor of 1.1.		

**5.099±0.021 OUR AVERAGE**

5.072±0.011±0.035	13M	<sup>1</sup> AMBROSINO	06	KLOE	$\sum_i B_i = 1$
5.092±0.017±0.025	15M	AMBROSINO	05C	KLOE	
5.154±0.044	0.4M	VOSBURGH	72	CNTR	

• • • We do not use the following data for averages, fits, limits, etc. • • •

5.15 ±0.14	DEVLIN	67	CNTR
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<sup>1</sup> AMBROSINO 06 uses  $\phi \rightarrow K_L K_S$  with  $K_L$  tagged by  $K_S \rightarrow \pi^+ \pi^-$ . The four major  $K_L$  BR's are measured, the small remainder ( $\pi^+ \pi^-, \pi^0 \pi^0, \gamma\gamma$ ) is taken from PDG 04. This KLOE  $K_L$  lifetime is obtained by imposing  $\sum_i B_i = 1$ . The correlation matrix among the four measured  $K_L$  BR's and this  $K_L$  lifetime is

$$\begin{matrix} & K_{e3} & K_{\mu 3} & 3\pi^0 & \pi^+ \pi^- \pi^0 & \tau_{K_L} \\ K_{e3} & 1 & -0.25 & -0.56 & -0.07 & 0.25 \\ K_{\mu 3} & & 1 & -0.43 & -0.20 & 0.33 \\ 3\pi^0 & & & 1 & -0.39 & -0.21 \\ \pi^+ \pi^- \pi^0 & & & & 1 & -0.39 \\ \tau_{K_L} & & & & & 1 \end{matrix}$$

These correlations are taken into account in our fit. The average of this KLOE mean life measurement and the independent KLOE measurement in AMBROSINO 05C is  $(5.084 \pm 0.023) \times 10^{-8}$  s.

NODE=S013T

NODE=S013T

NODE=S013T;LINKAGE=AM

## $K_L^0$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level
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**Semileptonic modes**

$\Gamma_1$ $\pi^\pm e^\mp \nu_e$ Called $K_{e3}^0$ .	[a] $(40.55 \pm 0.11) \%$	S=1.7
$\Gamma_2$ $\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[a] $(27.04 \pm 0.07) \%$	S=1.1
$\Gamma_3$ $(\pi \mu \text{atom}) \nu$	$(1.05 \pm 0.11) \times 10^{-7}$	DESIG=19
$\Gamma_4$ $\pi^0 \pi^\pm e^\mp \nu$	[a] $(5.20 \pm 0.11) \times 10^{-5}$	DESIG=18
$\Gamma_5$ $\pi^\pm e^\mp \nu e^+ e^-$	[a] $(1.26 \pm 0.04) \times 10^{-5}$	DESIG=51

**Hadronic modes, including Charge conjugation x Parity Violating (CPV) modes**

$\Gamma_6$ $3\pi^0$	$(19.52 \pm 0.12) \%$	S=1.6
$\Gamma_7$ $\pi^+ \pi^- \pi^0$	$(12.54 \pm 0.05) \%$	DESIG=2
$\Gamma_8$ $\pi^+ \pi^-$	CPV [b] $(1.967 \pm 0.010) \times 10^{-3}$	DESIG=5
$\Gamma_9$ $\pi^0 \pi^0$	CPV $(8.64 \pm 0.06) \times 10^{-4}$	DESIG=11

**Semileptonic modes with photons**

$\Gamma_{10}$ $\pi^\pm e^\mp \nu_e \gamma$	[a,c,d] $(3.79 \pm 0.06) \times 10^{-3}$
$\Gamma_{11}$ $\pi^\pm \mu^\mp \nu_\mu \gamma$	$(5.65 \pm 0.23) \times 10^{-4}$

**Hadronic modes with photons or  $\ell\bar{\ell}$  pairs**

$\Gamma_{12}$ $\pi^0 \pi^0 \gamma$	$< 2.43 \times 10^{-7}$	CL=90%
$\Gamma_{13}$ $\pi^+ \pi^- \gamma$	[c,d] $(4.15 \pm 0.15) \times 10^{-5}$	S=2.8
$\Gamma_{14}$ $\pi^+ \pi^- \gamma$ (DE)	$(2.84 \pm 0.11) \times 10^{-5}$	S=2.0
$\Gamma_{15}$ $\pi^0 2\gamma$	[c] $(1.273 \pm 0.033) \times 10^{-6}$	DESIG=13
$\Gamma_{16}$ $\pi^0 \gamma e^+ e^-$	$(1.62 \pm 0.17) \times 10^{-8}$	DESIG=46

**Other modes with photons or  $\ell\bar{\ell}$  pairs**

$\Gamma_{17}$ $2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$	S=1.1
$\Gamma_{18}$ $3\gamma$	$< 7.4 \times 10^{-8}$	CL=90%
$\Gamma_{19}$ $e^+ e^- \gamma$	$(9.4 \pm 0.4) \times 10^{-6}$	S=2.0
$\Gamma_{20}$ $\mu^+ \mu^- \gamma$	$(3.59 \pm 0.11) \times 10^{-7}$	S=1.3
$\Gamma_{21}$ $\mu^+ \mu^- \mu^+ \mu^-$	$< 2.3 \times 10^{-9}$	CL=90%
$\Gamma_{22}$ $e^+ e^- \gamma\gamma$	[c] $(5.95 \pm 0.33) \times 10^{-7}$	DESIG=23
$\Gamma_{23}$ $\mu^+ \mu^- \gamma\gamma$	[c] $(1.0 \pm 0.8) \times 10^{-8}$	DESIG=47

NODE=S013215;NODE=S013

NODE=S013;CLUMP=A  
DESIG=4

DESIG=3

DESIG=19

DESIG=18

DESIG=51

NODE=S013;CLUMP=B  
DESIG=1

DESIG=2

DESIG=5

DESIG=11

NODE=S013;CLUMP=C  
DESIG=12

DESIG=34

NODE=S013;CLUMP=D  
DESIG=33

DESIG=10

DESIG=50

DESIG=13

DESIG=46

NODE=S013;CLUMP=E  
DESIG=9

DESIG=45

DESIG=14

DESIG=15

DESIG=56

DESIG=23

DESIG=47

**Charge conjugation  $\times$  Parity ( $CP$ ) or Lepton Family number ( $LF$ ) violating modes, or  $\Delta S = 1$  weak neutral current ( $S1$ ) modes**

$\Gamma_{24}$	$\mu^+ \mu^-$	$S1$	$( 6.84 \pm 0.11 ) \times 10^{-9}$	NODE=S013;CLUMP=F
$\Gamma_{25}$	$e^+ e^-$	$S1$	$( 9 \pm 4 ) \times 10^{-12}$	DESIG=6
$\Gamma_{26}$	$\pi^+ \pi^- e^+ e^-$	$S1$	$[c] ( 3.11 \pm 0.19 ) \times 10^{-7}$	DESIG=7
$\Gamma_{27}$	$\pi^0 \pi^0 e^+ e^-$	$S1$	$< 6.6 \times 10^{-9}$ CL=90%	DESIG=17
$\Gamma_{28}$	$\pi^0 \pi^0 \mu^+ \mu^-$	$S1$	$< 9.2 \times 10^{-11}$ CL=90%	DESIG=48
$\Gamma_{29}$	$\mu^+ \mu^- e^+ e^-$	$S1$	$( 2.69 \pm 0.27 ) \times 10^{-9}$	DESIG=54
$\Gamma_{30}$	$e^+ e^- e^+ e^-$	$S1$	$( 3.56 \pm 0.21 ) \times 10^{-8}$	DESIG=21
$\Gamma_{31}$	$\pi^0 \mu^+ \mu^-$	$CP, S1$	$[e] < 3.8 \times 10^{-10}$ CL=90%	DESIG=22
$\Gamma_{32}$	$\pi^0 e^+ e^-$	$CP, S1$	$[e] < 2.8 \times 10^{-10}$ CL=90%	DESIG=16
$\Gamma_{33}$	$\pi^0 \nu \bar{\nu}$	$CP, S1$	$[f] < 3.0 \times 10^{-9}$ CL=90%	DESIG=20
$\Gamma_{34}$	$\pi^0 \pi^0 \nu \bar{\nu}$	$S1$	$< 8.1 \times 10^{-7}$ CL=90%	DESIG=43
$\Gamma_{35}$	$e^\pm \mu^\mp$	$LF$	$[a] < 4.7 \times 10^{-12}$ CL=90%	DESIG=52
$\Gamma_{36}$	$e^\pm e^\pm \mu^\mp \mu^\mp$	$LF$	$[a] < 4.12 \times 10^{-11}$ CL=90%	DESIG=8
$\Gamma_{37}$	$\pi^0 \mu^\pm e^\mp$	$LF$	$[a] < 7.6 \times 10^{-11}$ CL=90%	DESIG=24
$\Gamma_{38}$	$\pi^0 \pi^0 \mu^\pm e^\mp$	$LF$	$< 1.7 \times 10^{-10}$ CL=90%	DESIG=36
				DESIG=53

**Lorentz invariance violating modes**

$\Gamma_{39}$	$\pi^0 \gamma$	$< 1.7 \times 10^{-7}$	CL=90%	NODE=S013;CLUMP=H
				DESIG=55

- [a] The value is for the sum of the charge states or particle/antiparticle states indicated.
- [b] This mode includes gammas from inner bremsstrahlung but not the direct emission mode  $K_L^0 \rightarrow \pi^+ \pi^- \gamma$  (DE).
- [c] See the Particle Listings below for the energy limits used in this measurement.
- [d] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ 's.
- [e] Allowed by higher-order electroweak interactions.
- [f] Violates  $CP$  in leading order. Test of direct  $CP$  violation since the indirect  $CP$ -violating and  $CP$ -conserving contributions are expected to be suppressed.

### CONSTRAINED FIT INFORMATION

An overall fit to the mean life and 15 branching ratios uses 27 measurements and one constraint to determine 11 parameters. The overall fit has a  $\chi^2 = 37.4$  for 17 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta p_i \delta p_j \rangle / (\delta p_i \delta p_j)$ , in percent, from the fit to parameters  $p_i$ , including the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

	$x_2$	$x_6$	$x_7$	$x_8$	$x_9$	$x_{13}$	$x_{14}$	$x_{17}$	$x_{19}$	$\Gamma$	$x_1$	$x_2$	$x_6$	$x_7$	$x_8$	$x_9$	$x_{13}$	$x_{14}$	$x_{17}$	$x_{19}$
	-21																			
	-77	-29																		
	-15	-20	-18																	
	53	-11	-47	4																
	30	-23	-11	-12	64															
	6	-1	-6	0	12	8														
	6	-1	-6	0	11	7	93													
	-46	-22	64	-14	-21	8	-3	-3												
	-5	-2	7	-1	-3	-1	0	0	4											
	-27	-9	24	15	-13	-6	-2	-2	15	2										

Mode	Rate ( $10^8 \text{ s}^{-1}$ )	Scale factor	
$\Gamma_1$ $\pi^\pm e^\mp \nu_\ell$ Called $K_{e3}^0$ .	[a] $0.07927 \pm 0.00034$	1.1	DESIG=4
$\Gamma_2$ $\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[a] $0.05286 \pm 0.00025$	1.1	DESIG=3

$\Gamma_6$	$3\pi^0$	$0.03815 \pm 0.00030$	1.5	DESIG=1
$\Gamma_7$	$\pi^+ \pi^- \pi^0$	$0.02451 \pm 0.00015$		DESIG=2
$\Gamma_8$	$\pi^+ \pi^-$	$[b] (3.844 \pm 0.023) \times 10^{-4}$	1.2	DESIG=5
$\Gamma_9$	$\pi^0 \pi^0$	$(1.690 \pm 0.013) \times 10^{-4}$	1.4	DESIG=11
$\Gamma_{13}$	$\pi^+ \pi^- \gamma$	$[c,d] (8.11 \pm 0.29) \times 10^{-6}$	2.7	DESIG=10
$\Gamma_{14}$	$\pi^+ \pi^- \gamma(\text{DE})$	$(5.55 \pm 0.21) \times 10^{-6}$	2.0	DESIG=50
$\Gamma_{17}$	$2\gamma$	$(1.069 \pm 0.010) \times 10^{-4}$	1.2	DESIG=9
$\Gamma_{19}$	$e^+ e^- \gamma$	$(1.84 \pm 0.08) \times 10^{-6}$	1.9	DESIG=14

 **$K_L^0$  DECAY RATES** **$\Gamma(\pi^+ \pi^- \pi^0)$** 

VALUE ( $10^6 \text{ s}^{-1}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>2.451 \pm 0.015</math> OUR FIT</b>				$\Gamma_7$

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.32 $^{+0.13}_{-0.15}$	192	BALDO-...	75	HLBC	Assumes CP
2.35 $\pm 0.20$	180	<sup>1</sup> JAMES	72	HBC	Assumes CP
2.71 $\pm 0.28$	99	CHO	71	DBC	Assumes CP
2.5 $\pm 0.3$	98	<sup>1</sup> JAMES	71	HBC	Assumes CP
2.12 $\pm 0.33$	50	MEISNER	71	HBC	Assumes CP
2.20 $\pm 0.35$	53	WEBBER	70	HBC	Assumes CP
2.62 $^{+0.28}_{-0.27}$	136	BEHR	66	HLBC	Assumes CP
3.26 $\pm 0.77$	18	ANDERSON	65	HBC	
1.4 $\pm 0.4$	14	FRANZINI	65	HBC	

<sup>1</sup>JAMES 72 is a final measurement and includes JAMES 71.

 **$\Gamma(\pi^\pm e^\mp \nu_e)$** 

VALUE ( $10^6 \text{ s}^{-1}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>7.927 \pm 0.034</math> OUR FIT</b>				$\Gamma_1$

Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

7.81 $\pm 0.56$	620	CHAN	71	HBC
7.52 $^{+0.85}_{-0.72}$		AUBERT	65	HLBC $\Delta S = \Delta Q, CP$ assumed

 **$\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)$**  **$(\Gamma_1 + \Gamma_2)$** 

VALUE ( $10^6 \text{ s}^{-1}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>13.21 \pm 0.05</math> OUR FIT</b>				

• • • We do not use the following data for averages, fits, limits, etc. • • •

12.4 $\pm 0.7$	410	<sup>1</sup> BURGUN	72	HBC	$K^+ p \rightarrow K^0 p \pi^+$
8.47 $\pm 1.69$	126	<sup>1</sup> MANN	72	HBC	$K^- p \rightarrow n \bar{K}^0$
13.1 $\pm 1.3$	252	<sup>1</sup> WEBBER	71	HBC	$K^- p \rightarrow n \bar{K}^0$
11.6 $\pm 0.9$	393	<sup>1,2</sup> CHO	70	DBC	$K^+ n \rightarrow K^0 p$
10.3 $\pm 0.8$	335	<sup>2</sup> HILL	67	DBC	$K^+ n \rightarrow K^0 p$
9.85 $^{+1.15}_{-1.05}$	109	<sup>1</sup> FRANZINI	65	HBC	

<sup>1</sup> Assumes  $\Delta S = \Delta Q$  rule.

<sup>2</sup> CHO 70 includes events of HILL 67.

NODE=S013W2;LINKAGE=J

NODE=S013W3  
NODE=S013W3

NODE=S013W5  
NODE=S013W5

NODE=S013W5;LINKAGE=D  
NODE=S013W5;LINKAGE=C

 **$K_L^0$  BRANCHING RATIOS****Semileptonic modes** **$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma_{\text{total}}$**  **$\Gamma_1/\Gamma$** 

VALUE	EVTS	DOCUMENT ID	TECN	
<b><math>0.4055 \pm 0.0011</math> OUR FIT</b>				Error includes scale factor of 1.7.
<b><math>0.4047 \pm 0.0028</math> OUR AVERAGE</b>				Error includes scale factor of 3.1.

0.4007  $\pm 0.0005 \pm 0.0015$  13M <sup>1</sup>AMBROSINO 06 KLOE  
0.4067  $\pm 0.0011$  2ALEXOPOU... 04 KTEV

NODE=S013230

NODE=S013405

NODE=S013R57  
NODE=S013R57

<sup>1</sup> There are correlations between these five KLOE measurements:  $B(K_L \rightarrow \pi e \nu)$ ,  $B(K_L \rightarrow \pi \mu \nu)$ ,  $B(K_L \rightarrow 3\pi^0)$ ,  $B(K_L \rightarrow \pi^+ \pi^- \pi^0)$ , and  $\tau_{K_L}$  measured in AMBROSINO 06. See the footnote for the  $\tau_{K_L}$  measurement for the correlation matrix.

<sup>2</sup> ALEXOPOULOS 04 constrains  $\sum_i B_i = 0.9993$  for the six major  $K_L$  branching fractions. The correlations among these branching fractions are taken into account in our fit. The correlation matrix is

	$K_{e3}$	$K_{\mu 3}$	$3\pi^0$	$\pi^+ \pi^- \pi^0$	$\pi^+ \pi^-$	$\pi^0 \pi^0$
$K_{e3}$	1					
$K_{\mu 3}$	0.15	1				
$3\pi^0$	-0.77	-0.62	1			
$\pi^+ \pi^- \pi^0$	0.18	0.08	-0.54	1		
$\pi^+ \pi^-$	0.28	0.22	-0.48	0.49	1	
$\pi^0 \pi^0$	-0.72	-0.54	0.89	-0.46	-0.39	1

### $\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma_{\text{total}}$

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.2704 ± 0.0007 OUR FIT</b>	Error includes scale factor of 1.1.		

#### 0.2700 ± 0.0008 OUR AVERAGE

$0.2698 \pm 0.0005 \pm 0.0015$	13M	1 AMBROSINO 06	KLOE
$0.2701 \pm 0.0009$		2 ALEXOPOU... 04	KTEV

<sup>1</sup> There are correlations between these five KLOE measurements:  $B(K_L \rightarrow \pi e \nu)$ ,  $B(K_L \rightarrow \pi \mu \nu)$ ,  $B(K_L \rightarrow 3\pi^0)$ ,  $B(K_L \rightarrow \pi^+ \pi^- \pi^0)$ , and  $\tau_{K_L}$  measured in AMBROSINO 06. See the footnote for the  $\tau_{K_L}$  measurement for the correlation matrix.

<sup>2</sup> For correlations with other ALEXOPOULOS 04 measurements, see the footnote with their  $B(K_L \rightarrow \pi e \nu)$  measurement.

### $[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)]/\Gamma_{\text{total}}$

VALUE	DOCUMENT ID
<b>0.6760 ± 0.0012 OUR FIT</b>	Error includes scale factor of 1.6.

### $\Gamma_2/\Gamma$

NODE=S013R58  
NODE=S013R58

### $\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma(\pi^\pm e^\mp \nu_e)$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.6669 ± 0.0027 OUR FIT</b>	Error includes scale factor of 1.2.			

#### 0.666 ± 0.004 OUR AVERAGE

• • • We use the following data for averages but not for fits. • • •

$0.6740 \pm 0.0059$	13M	1 AMBROSINO 06	KLOE	Not in fit
$0.6640 \pm 0.0014 \pm 0.0022$	394k	2 ALEXOPOU... 04	KTEV	Not in fit

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.702 ± 0.011	33k	CHO	80	HBC
0.662 ± 0.037	10k	WILLIAMS	74	ASPK
0.741 ± 0.044	6700	BRANDENB...	73	HBC
0.662 ± 0.030	1309	EVANS	73	HLBC
0.68 ± 0.08	3548	BASILE	70	OSPK
0.71 ± 0.05	770	BUDAGOV	68	HLBC

<sup>1</sup> AMBROSINO 06 enters the fit via their separate measurements of these two modes.

<sup>2</sup> ALEXOPOULOS 04 enters the fit via their separate measurements of these two modes.

### $\Gamma_2/\Gamma_1$

NODE=S013R7  
NODE=S013R7

### $\Gamma((\pi \mu \text{atom}) \nu)/\Gamma(\pi^\pm \mu^\mp \nu_\mu)$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN
<b>3.90 ± 0.39</b>	155	1 ARONSON 86	SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

seen	18	COOMBES	76	WIRE
------	----	---------	----	------

<sup>1</sup> ARONSON 86 quote theoretical value of  $(4.31 \pm 0.08) \times 10^{-7}$ .

### $\Gamma_3/\Gamma_2$

NODE=S013R10;LINKAGE=AM  
NODE=S013R10;LINKAGE=AL

### $\Gamma(\pi^0 \pi^\pm e^\mp \nu)/\Gamma_{\text{total}}$

VALUE (units $10^{-5}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>5.20 ± 0.11 OUR AVERAGE</b>				

• • • We do not use the following data for averages, fits, limits, etc. • • •

5.21 ± 0.07 ± 0.09	5402	BATLEY	04	NA48
5.16 ± 0.20 ± 0.22	729	MAKOFF	93	E731

• • • We do not use the following data for averages, fits, limits, etc. • • •

6.2 ± 2.0	16	CARROLL	80C	SPEC
< 220	90	<sup>1</sup> DONALDSON	74	SPEC

<sup>1</sup> DONALDSON 74 uses  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$  decays = 0.126.

### $\Gamma_4/\Gamma$

NODE=S013R33  
NODE=S013R33

NODE=S013R33;LINKAGE=A

NODE=S013R32  
NODE=S013R32

NODE=S013R32;LINKAGE=D

$\Gamma(\pi^\pm e^\mp \nu e^+ e^-)/\Gamma(\pi^+ \pi^- \pi^0)$	$\Gamma_5/\Gamma_7$
<u>VALUE (units <math>10^{-5}</math>)</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
<b>10.02±0.17±0.29</b>	19k    1 ABOUZAID    07C KTEV $M_{ee} > 5$ MeV, $E_{ee}^* > 30$ MeV 1 $E_{ee}^*$ is the energy of the $e^+ e^-$ pair in the kaon rest frame. ABOUZAID 07C reports $[\Gamma(K_L^0 \rightarrow \pi^\pm e^\mp \nu e^+ e^-)/\Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)] / [B(\pi^0 \rightarrow e^+ e^- \gamma)] = (8.54 \pm 0.07 \pm 0.13) \times 10^{-3}$ which we multiply by our best value $B(\pi^0 \rightarrow e^+ e^- \gamma) = (1.174 \pm 0.035) \times 10^{-2}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

**Hadronic modes,**  
**including Charge conjugation×Parity Violating (CPV) modes**

$\Gamma(3\pi^0)/\Gamma_{\text{total}}$	$\Gamma_6/\Gamma$
<u>VALUE</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
<b>0.1952±0.0012 OUR FIT</b>	Error includes scale factor of 1.6.
<b>0.1969±0.0026 OUR AVERAGE</b>	Error includes scale factor of 2.0.
• • • We use the following data for averages but not for fits. • • •	
0.1997±0.0003±0.0019	13M    1 AMBROSINO    06 KLOE Not fitted
0.1945±0.0018	1 ALEXOPOU...    04 KTEV Not fitted
1 We exclude these $B(K_L \rightarrow 3\pi^0)$ measurements from our fit because the authors have constrained $K_L$ branching fractions to sum to one. It enters our fit via the other measurements from the experiment and their correlations, along with our constraint that the fitted branching fractions sum to one.	

$\Gamma(3\pi^0)/\Gamma(\pi^\pm e^\mp \nu_e)$	$\Gamma_6/\Gamma_1$
<u>VALUE</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
<b>0.481 ±0.004 OUR FIT</b>	Error includes scale factor of 1.8.
• • • We use the following data for averages but not for fits. • • •	
<b>0.4782±0.0014±0.0053</b>	209k    1 ALEXOPOU...    04 KTEV Not in fit
• • • We do not use the following data for averages, fits, limits, etc. • • •	
0.545 ± 0.004 ± 0.009	38k    KREUTZ    95 NA31

1 This measurement enters the fit via their separate measurements of these two modes.

$\Gamma(3\pi^0)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+ \pi^- \pi^0)]$	$\Gamma_6/(\Gamma_1+\Gamma_2+\Gamma_7)$
<u>VALUE</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
<b>0.2436±0.0018 OUR FIT</b>	Error includes scale factor of 1.6.
• • • We do not use the following data for averages, fits, limits, etc. • • •	
0.251 ± 0.014	549    BUDAGOV    68 HLBC ORSAY measur.
0.277 ± 0.021	444    BUDAGOV    68 HLBC Ecole polytec.meas
0.31 + 0.07 - 0.06	29    KULYUKINA    68 CC
0.24 ± 0.08	24    ANIKINA    64 CC

$\Gamma(3\pi^0)/\Gamma(\pi^+ \pi^- \pi^0)$	$\Gamma_6/\Gamma_7$
<u>VALUE</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
<b>1.557±0.012 OUR FIT</b>	Error includes scale factor of 1.3.
• • • We use the following data for averages but not for fits. • • •	
<b>1.582±0.027</b>	13M    1 AMBROSINO    06 KLOE Not in fit
• • • We do not use the following data for averages, fits, limits, etc. • • •	
1.611±0.014±0.034	28k    KREUTZ    95 NA31
1.65 ± 0.07	883    BARMIN    72B HLBC Error statistical only
1.80 ± 0.13	1010    BUDAGOV    68 HLBC
2.0 ± 0.6	188    ALEKSANYAN 64B FBC

1 AMBROSINO 06 enters the fit via their separate measurements of these two modes.

$\Gamma(\pi^+ \pi^- \pi^0)/\Gamma_{\text{total}}$	$\Gamma_7/\Gamma$
<u>VALUE</u>	<u>EVTS</u> <u>DOCUMENT ID</u> <u>TECN</u>
<b>0.1254±0.0005 OUR FIT</b>	
<b>0.1255±0.0006 OUR AVERAGE</b>	
0.1263±0.0004±0.0011	13M    1 AMBROSINO    06 KLOE
0.1252±0.0007	2 ALEXOPOU...    04 KTEV

1 There are correlations between these five KLOE measurements:  $B(K_L \rightarrow \pi e \nu)$ ,  $B(K_L \rightarrow \pi \mu \nu)$ ,  $B(K_L \rightarrow 3\pi^0)$ ,  $B(K_L \rightarrow \pi^+ \pi^- \pi^0)$ , and  $\tau K_L$  measured in AMBROSINO 06. See the footnote for the  $\tau K_L$  measurement for the correlation matrix.

2 For correlations with other ALEXOPOULOS 04 measurements, see the footnote with their  $B(K_L \rightarrow \pi e \nu)$  measurement.

NODE=S013R62  
NODE=S013R62

NODE=S013R62;LINKAGE=AB

NODE=S013410

NODE=S013R45  
NODE=S013R45

NOTFITTED  
NOTFITTED

NODE=S013R45;LINKAGE=AB

NODE=S013R46  
NODE=S013R46

NOTFITTED

NODE=S013R46;LINKAGE=AB

NODE=S013R1  
NODE=S013R1

OCCUR=2

NODE=S013R18  
NODE=S013R18

NOTFITTED

NODE=S013R18;LINKAGE=AM

NODE=S013R6  
NODE=S013R6

NODE=S013R6;LINKAGE=AM

NODE=S013R6;LINKAGE=AL

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma(\pi^\pm e^\mp \nu_e)$	$\Gamma_7/\Gamma_1$			
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.3092±0.0016 OUR FIT</b>				Error includes scale factor of 1.1.

• • • We use the following data for averages but not for fits. • • •
<b>0.3078±0.0005±0.0017</b> 799k <sup>1</sup> ALEXOPOU... 04 KTEV Not in fit
• • • We do not use the following data for averages, fits, limits, etc. • • •
0.336 ± 0.003 ± 0.007 28k KREUTZ 95 NA31

<sup>1</sup>This measurement enters the fit via their separate measurements for the two modes.

$\Gamma(\pi^+\pi^-\pi^0)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+\pi^-\pi^0)]$	$\Gamma_7/(\Gamma_1+\Gamma_2+\Gamma_7)$			
VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.1565±0.0006 OUR FIT</b>				Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •
0.163 ± 0.003 6499 CHO 77 HBC
0.1605 ± 0.0038 1590 ALEXANDER 73B HBC
0.146 ± 0.004 3200 BRANDENB... 73 HBC
0.159 ± 0.010 558 EVANS 73 HLBC
0.167 ± 0.016 1402 KULYUKINA 68 CC
0.161 ± 0.005 126 HOPKINS 67 HBC
0.162 ± 0.015 326 ASTBURY 65B CC
0.159 ± 0.015 566 GUIDONI 65 HBC
0.178 ± 0.017 1729 HOPKINS 65 HBC
0.144 ± 0.004 1729 HOPKINS 65 HBC

See HOPKINS 67

$\Gamma(\pi^+\pi^-)/\Gamma_{\text{total}}$	$\Gamma_8/\Gamma$
Violates CP conservation.	
<b>1.967±0.010 OUR FIT</b>	Error includes scale factor of 1.5.

<b>1.975±0.012</b>	<sup>1</sup> ALEXOPOU... 04 KTEV
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<sup>1</sup>For correlations with other ALEXOPOULOS 04 measurements, see the footnote with their  $B(K_L \rightarrow \pi e \nu)$  measurement.

NODE=S013R38  
NODE=S013R38  
NODE=S013R38

$\Gamma(\pi^+\pi^-)/\Gamma(\pi^\pm e^\mp \nu_e)$	$\Gamma_8/\Gamma_1$			
VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>4.849±0.020 OUR FIT</b>				Error includes scale factor of 1.1.

<b>4.840±0.020 OUR AVERAGE</b>	
4.826 ± 0.022 ± 0.016 47k <sup>1</sup> LAI 07 NA48	

• • • We use the following data for averages but not for fits. • • •

4.856 ± 0.017 ± 0.023 84k <sup>2</sup> ALEXOPOU... 04 KTEV
--

<sup>1</sup>The LAI 07 central value of  $4.835 \times 10^{-3}$  has been reduced by 0.19% to  $4.826 \times 10^{-3}$  to subtract the contribution from the direct emission mode  $K_L^0 \rightarrow \pi^+ \pi^- \gamma$ (DE).

<sup>2</sup>This measurement enters the fit via their separate measurements for the two modes.

NODE=S013R38;LINKAGE=AL

$[\Gamma(\pi^+\pi^-) + \Gamma(\pi^+\pi^-\gamma(\text{DE}))]/\Gamma(\pi^\pm \mu^\mp \nu_\mu)$	$(\Gamma_8+\Gamma_{14})/\Gamma_2$			
VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>7.38 ± 0.04 OUR FIT</b>				Error includes scale factor of 1.4.

<b>7.275±0.042±0.054</b>	45k <sup>1</sup> AMBROSINO 06F KLOE
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<sup>1</sup>Fully inclusive. Taking  $B(K_L^0 \rightarrow \pi \mu \nu)$  from KLOE, AMBROSINO 06,  $B(K_L^0 \rightarrow \pi^+ \pi^- + \pi^+ \pi^- \gamma)$ (DE) =  $(1.963 \pm 0.012 \pm 0.017) \times 10^{-3}$  is obtained.

NODE=S013R59;LINKAGE=AM

$\Gamma(\pi^+\pi^-)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)]$	$\Gamma_8/(\Gamma_1+\Gamma_2)$
Violates CP conservation.	
<b>2.909±0.013 OUR FIT</b>	Error includes scale factor of 1.3.

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.13 ± 0.14 1687 COUPAL 85 SPEC	$\eta_{+-}=2.28 \pm 0.06$
3.04 ± 0.14 2703 DEVOE 77 SPEC	$\eta_{+-}=2.25 \pm 0.05$
2.51 ± 0.23 309 <sup>1</sup> DEBOUARD 67 OSPK	$\eta_{+-}=2.00 \pm 0.09$
2.35 ± 0.19 525 <sup>1</sup> FITCH 67 OSPK	$\eta_{+-}=1.94 \pm 0.08$

NODE=S013R20  
NODE=S013R20  
NODE=S013R20

<sup>1</sup>Old experiments excluded from fit. See subsection on  $\eta_{+-}$  in section on "PARAMETERS FOR  $K_L^0 \rightarrow 2\pi$  DECAY" below for average  $\eta_{+-}$  of these experiments and for note on discrepancy.

NODE=S013R20;LINKAGE=O

$\Gamma(\pi^\pm e^\mp \nu_e)/\Gamma(2 \text{ tracks})$ 

$\Gamma(2 \text{ tracks}) = \Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + 0.03508 \Gamma(3\pi^0) + \Gamma(\pi^+ \pi^- \pi^0)$   
 $+ \Gamma(\pi^+ \pi^-)$  where 0.03508 is the fraction of  $3\pi^0$  events with one Dalitz decay ( $\pi^0 \rightarrow \gamma e^+ e^-$ ).

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.5006±0.0009 OUR FIT</b>		Error includes scale factor of 1.3.	
<b>0.4978±0.0035</b>	6.8M	LAI	04B NA48

NODE=S013R56

NODE=S013R56

NODE=S013R56

 $\Gamma(\pi^+ \pi^-)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+ \pi^- \pi^0)] \quad \Gamma_8/(\Gamma_1+\Gamma_2+\Gamma_7)$ 

Violates CP conservation.

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.454±0.011 OUR FIT</b>		Error includes scale factor of 1.3.		

NODE=S013R9

NODE=S013R9

NODE=S013R9

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.60 ± 0.07 4200 <sup>1</sup> MESSNER 73 ASPK  $\eta_{+-} = 2.23 \pm 0.05$ 1 From same data as  $\Gamma(\pi^+ \pi^-)/\Gamma(\pi^+ \pi^- \pi^0)$  MESSNER 73, but with different normalization.

NODE=S013R9;LINKAGE=M

 $\Gamma(\pi^+ \pi^-)/\Gamma(\pi^+ \pi^- \pi^0)$  $\Gamma_8/\Gamma_7$ 

Violates CP conservation.

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.568±0.010 OUR FIT</b>		Error includes scale factor of 1.3.		

NODE=S013R27

NODE=S013R27

NODE=S013R27

• • • We do not use the following data for averages, fits, limits, etc. • • •  
1.64 ± 0.04 4200 MESSNER 73 ASPK  $\eta_{+-} = 2.23$  $\Gamma(\pi^0 \pi^0)/\Gamma_{\text{total}}$  $\Gamma_9/\Gamma$ 

Violates CP conservation.

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN
<b>0.864±0.006 OUR FIT</b>		Error includes scale factor of 1.8.	
<b>0.865±0.012</b>	1 ALEXOPOU... 04 KTEV		

NODE=S013R17

NODE=S013R17

NODE=S013R17

1 For correlations with other ALEXOPOULOS 04 measurements, see the footnote with their  $B(K_L \rightarrow \pi e \nu)$  measurement.

NODE=S013R17;LINKAGE=AL

 $\Gamma(\pi^0 \pi^0)/\Gamma(\pi^+ \pi^-)$  $\Gamma_9/\Gamma_8$ 

Violates CP conservation.

VALUE	EVTS	DOCUMENT ID
<b>0.4395±0.0023 OUR FIT</b>		Error includes scale factor of 2.0.
<b>0.4390±0.0012</b>	ETAFIT 16	

NODE=S013R39

NODE=S013R39

NODE=S013R39

 $\Gamma(\pi^0 \pi^0)/\Gamma(3\pi^0)$  $\Gamma_9/\Gamma_6$ 

Violates CP conservation.

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.443 ± 0.004 OUR FIT</b>		Error includes scale factor of 2.1.		

NODE=S013R19

NODE=S013R19

NODE=S013R19

• • • We use the following data for averages but not for fits. • • •

NOTFITTED

0.4446±0.0016±0.0019 100k <sup>1</sup> ALEXOPOU... 04 KTEV Not in fit

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.37 ± 0.08 29 BARMIN 70 HLBC  $\eta_{00}=2.02 \pm 0.23$   
0.32 ± 0.15 30 BUDAGOV 70 HLBC  $\eta_{00}=1.9 \pm 0.5$   
0.46 ± 0.11 57 BANNER 69 OSPK  $\eta_{00}=2.2 \pm 0.3$ 

NODE=S013R19;LINKAGE=AL

1 This measurement enters the fit via their separate measurements for the two modes.

## —— Semileptonic modes with photons ——

 $\Gamma(\pi^\pm e^\mp \nu_e \gamma)/\Gamma(\pi^\pm e^\mp \nu_e)$  $\Gamma_{10}/\Gamma_1$ 

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.935±0.015 OUR AVERAGE</b>				Error includes scale factor of 1.9. See the ideogram below.
0.924±0.023±0.016	9k	<sup>1</sup> AMBROSINO 08F KLOE	$E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ$	
0.916±0.017	4309	<sup>2</sup> ALEXOPOU... 05 KTEV	$E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ$	
$0.964 \pm 0.008^{+0.011}_{-0.009}$	19k	LAI 05 NA48	$E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ$	
$0.908 \pm 0.008^{+0.013}_{-0.012}$	15k	ALAVI-HARATI01J KTEV	$E_\gamma^* \geq 30 \text{ MeV}, \theta_{e\gamma}^* \geq 20^\circ$	
$0.934 \pm 0.036^{+0.055}_{-0.039}$	1384	LEBER 96 NA31	$E_\gamma^* \geq 30 \text{ MeV}, \theta_{e\gamma}^* \geq 20^\circ$	

NODE=S013R25

NODE=S013R25

NODE=S013R25

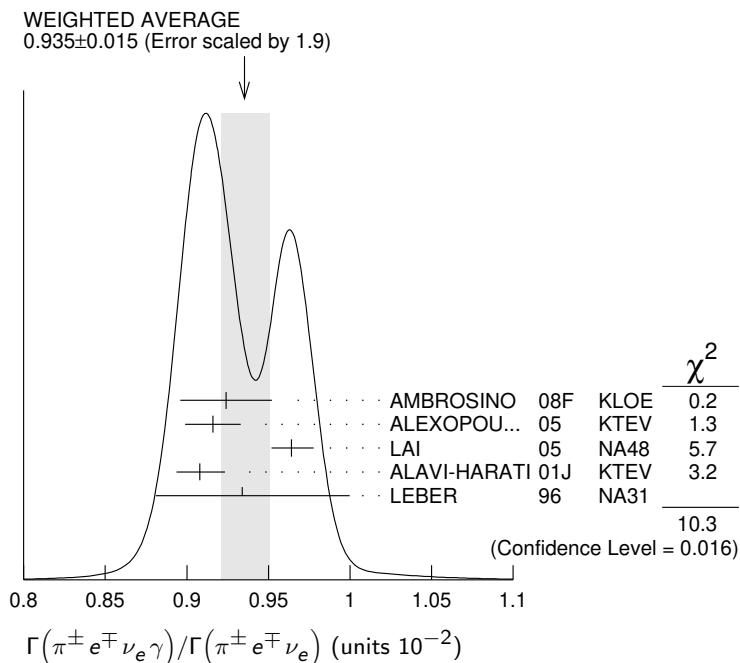
NODE=S013415

<sup>1</sup> Direct emission contribution measured  $\langle X \rangle = -2.3 \pm 1.3 \pm 1.4$ .

<sup>2</sup> Also measured cut  $E_\gamma^* > 10$  MeV,  $\theta_{e\gamma}^* > 0^\circ$  14221 evts:  $\Gamma(\pi^\pm e^\mp \nu_e \gamma) / \Gamma(\pi^\pm e^\mp \nu_e)$  =  $(4.942 \pm 0.062)\%$ .

NODE=S013R25;LINKAGE=AM

NODE=S013R25;LINKAGE=AL



### $\Gamma(\pi^\pm \mu^\mp \nu_\mu \gamma) / \Gamma(\pi^\pm \mu^\mp \nu_\mu)$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>2.09 \pm 0.08</math> OUR AVERAGE</b>				
$2.09 \pm 0.09$		<sup>1</sup> ALEXOPOU... 05	KTEV	$E_\gamma^* > 30$ MeV
$2.08 \pm 0.17^{+0.16}_{-0.21}$	252	BENDER	98	NA48 $E_\gamma^* \geq 30$ MeV

<sup>1</sup> Also measured cut  $E_\gamma^* > 10$  MeV, 1385 evts:  $\Gamma(\pi^\pm \mu^\mp \nu_\mu \gamma) / \Gamma(\pi^\pm \mu^\mp \nu_\mu) = (0.530 \pm 0.014 \pm 0.012)\%$ .

### $\Gamma_{11}/\Gamma_2$

NODE=S013R49  
NODE=S013R49

### $\Gamma(\pi^0 \pi^0 \gamma) / \Gamma_{\text{total}}$

VALUE (units $10^{-6}$ )	CL %	DOCUMENT ID	TECN	COMMENT
< <b>0.243</b>	90	ABOUZAID 08B	KTEV	$K_L^0 \rightarrow \pi^0 \pi_D^0 \gamma, \pi_D^0 \rightarrow ee\gamma$
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>				
< 5.6	90	BARR 94	NA31	
< 230	90	ROBERTS 94	E799	

### $\Gamma(\pi^+ \pi^- \gamma) / \Gamma(\pi^+ \pi^- \pi^0)$

### $\Gamma_{12}/\Gamma$

NODE=S013R12  
NODE=S013R12  
NODE=S013R12

For earlier limits see our 1992 edition Physical Review D45 S1 (1992).

VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>				
$1.23 \pm 0.13$	516	<sup>1,2</sup> CARROLL 80B	SPEC	$E_\gamma^* > 20$ MeV
$2.33 \pm 0.23$	546	<sup>1,3</sup> CARROLL 80B	SPEC	
$3.56 \pm 0.26$	1062	<sup>1,4</sup> CARROLL 80B	SPEC	$E_\gamma^* > 20$ MeV

<sup>1</sup> CARROLL 80B quotes  $B(\pi^+ \pi^- \gamma)$  using normalization  $B(\pi^+ \pi^- \pi^0) = 0.1239$ . We divide by this value to obtain their measured  $\Gamma(\pi^+ \pi^- \gamma) / \Gamma(\pi^+ \pi^- \pi^0)$ .

<sup>2</sup> Internal Bremsstrahlung component only.

<sup>3</sup> Direct  $\gamma$  emission component only.

<sup>4</sup> Both IB and DE components.

OCCUR=2  
OCCUR=3

NODE=S013R12;LINKAGE=CA

NODE=S013R12;LINKAGE=H  
NODE=S013R12;LINKAGE=J  
NODE=S013R12;LINKAGE=K

$\Gamma(\pi^+\pi^-\gamma)/\Gamma(\pi^+\pi^-)$   $\Gamma_{13}/\Gamma_8$ 

<u>VALUE (units <math>10^{-2}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>2.11±0.08 OUR FIT</b>	Error includes scale factor of 2.9.			
<b>2.11±0.08 OUR AVERAGE</b>	Error includes scale factor of 2.9.			

2.08±0.02±0.02 8669 1 ALAVI-HARATI01B KTEV  $E_\gamma^*$  > 20 MeV  
 2.30±0.07 3136 RAMBERG 93 E731  $E_\gamma^*$  > 20 MeV

<sup>1</sup> ALAVI-HARATI 01B includes both Direct Emission (DE) and Inner Bremsstrahlung (IB) processes.

 $\Gamma(\pi^+\pi^-\gamma(\text{DE}))/\Gamma(\pi^+\pi^-\gamma)$   $\Gamma_{14}/\Gamma_{13}$ 

These values assume that  $\Gamma(K_L^0 \rightarrow \pi^+\pi^-\gamma) = \Gamma(K_L^0 \rightarrow \pi^+\pi^-\gamma(\text{DE})) + \Gamma(K_L^0 \rightarrow \pi^+\pi^-\gamma(\text{IB}))$ , the sum of widths for the direct emission (DE) and inner bremsstrahlung (IE) processes, with no IB-DE interference. DE assumes a form factor as described in RAMBERG 93.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.684±0.009 OUR FIT</b>				
<b>0.684±0.009 OUR AVERAGE</b>				
0.689±0.021 111k ABOUZAID 06A KTEV $E_\gamma^*$ > 20 MeV				
0.683±0.011 8669 ALAVI-HARATI01B KTEV $E_\gamma^*$ > 20 MeV				
0.685±0.041 3136 RAMBERG 93 E731 $E_\gamma^*$ > 20 MeV				

 $\Gamma(\pi^0 2\gamma)/\Gamma_{\text{total}}$   $\Gamma_{15}/\Gamma$ 

<u>VALUE (units <math>10^{-6}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1.273±0.033 OUR AVERAGE</b>					

1.28 ± 0.06 ± 0.01 1.4k <sup>1</sup> ABOUZAID 08 KTEV  
 1.27 ± 0.04 ± 0.01 2.5k <sup>2</sup> LAI 02B NA48

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.68 ± 0.07 ± 0.08 884 <sup>3</sup> ALAVI-HARATI99B KTEV  
 1.7 ± 0.2 ± 0.2 63 <sup>4</sup> BARR 92 NA31  
 1.86 ± 0.60 ± 0.60 60 PAPADIMITR...91 E731  $m_{\gamma\gamma} > 280$  MeV  
 <5.1 90 PAPADIMITR...91 E731  $m_{\gamma\gamma} < 264$  MeV  
 2.1 ± 0.6 14 <sup>5</sup> BARR 90C NA31  $m_{\gamma\gamma} > 280$  MeV

<sup>1</sup> ABOUZAID 08 reports  $(1.29 \pm 0.03 \pm 0.05) \times 10^{-6}$  from a measurement of  $[\Gamma(K_L^0 \rightarrow \pi^0 2\gamma)/\Gamma_{\text{total}}] / [\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0)]$  assuming  $\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.69 \pm 0.04) \times 10^{-4}$ , which we rescale to our best value  $\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.64 \pm 0.06) \times 10^{-4}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

<sup>2</sup> LAI 02B reports  $[\Gamma(K_L^0 \rightarrow \pi^0 2\gamma)/\Gamma_{\text{total}}] / [\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0)] = (1.467 \pm 0.032 \pm 0.032) \times 10^{-3}$  which we multiply by our best value  $\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.64 \pm 0.06) \times 10^{-4}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value. They also find that  $\mathcal{B}(\pi^0 2\gamma, m_{\gamma\gamma} < 110$  MeV) <  $0.6 \times 10^{-8}$  (90% CL).

<sup>3</sup> ALAVI-HARATI 99B finds that  $\Gamma(\pi^0 2\gamma, m_{\gamma\gamma} < 240$  MeV) /  $\Gamma(\pi^0 2\gamma) = (17.3 \pm 1.3 \pm 1.5)\%$ . Superseded by ABOUZAID 08.

<sup>4</sup> BARR 92 find that  $\Gamma(\pi^0 2\gamma, m_{\gamma\gamma} < 240$  MeV) /  $\Gamma(\pi^0 2\gamma) < 0.09$  (90% CL).

<sup>5</sup> BARR 90C superseded by BARR 92.

 $\Gamma(\pi^0 \gamma e^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_{16}/\Gamma$ 

<u>VALUE (units <math>10^{-8}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>1.62±0.14±0.09</b>		125	<sup>1</sup> ABOUZAID 07D KTEV	

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.34±0.35±0.13 44 ALAVI-HARATI01E KTEV  
 <71 90 0 MURAKAMI 99 SPEC

<sup>1</sup> ABOUZAID 07D includes 1997 (ALAVI-HARATI 01E) and 1999 data. It measures the ratio of  $\mathcal{B}(K_L^0 \rightarrow \pi^0 \gamma e^+ e^-) / \mathcal{B}(K_L^0 \rightarrow \pi^0 \pi_D^0)$ , where  $\pi_D^0$  is the Dalitz decaying  $\pi^0$ , and uses PDG 06 values  $\mathcal{B}(K_L^0 \rightarrow \pi^0 \pi^0) = (8.69 \pm 0.04) \times 10^{-4}$ , and  $\mathcal{B}(\pi_D^0 \rightarrow e^+ e^- \gamma) = (1.198 \pm 0.032) \times 10^{-2}$ . Supersedes ALAVI-HARATI 01E result.

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NODE=S013R60

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NODE=S013R26;LINKAGE=LB

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 NODE=S013R26;LINKAGE=A

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NODE=S013R51;LINKAGE=AD

**Other modes with photons or  $\ell\bar{\ell}$  pairs**

$\Gamma(2\gamma)/\Gamma_{\text{total}}$					$\Gamma_{17}/\Gamma$
<u>VALUE (units <math>10^{-4}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>5.47±0.04 OUR FIT</b>	Error includes scale factor of 1.1.				
• • • We do not use the following data for averages, fits, limits, etc. • • •					
4.54 ± 0.84		<sup>1</sup> BANNER	72B	OSPK	
4.5 ± 1.0	23	ENSTROM	71	OSPK	$K_L^0$ 1.5–9 GeV/c
5.0 ± 1.0		<sup>2</sup> REPELLIN	71	OSPK	
5.5 ± 1.1	90	KUNZ	68	OSPK	Norm.to 3 $\pi(C+N)$

<sup>1</sup> This value uses  $(\eta_{00}/\eta_{+-})^2 = 1.05 \pm 0.14$ . In general,  $\Gamma(2\gamma)/\Gamma_{\text{total}} = [(4.32 \pm 0.55) \times 10^{-4}] [(\eta_{00}/\eta_{+-})^2]$ .

<sup>2</sup> Assumes regeneration amplitude in copper at 2 GeV is 22 mb. To evaluate for a given regeneration amplitude and error, multiply by  $(\text{regeneration amplitude}/22\text{mb})^2$ .

$\Gamma(2\gamma)/\Gamma(3\pi^0)$					$\Gamma_{17}/\Gamma_6$
<u>VALUE (units <math>10^{-3}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
<b>2.802±0.017 OUR FIT</b>					
<b>2.802±0.018 OUR AVERAGE</b>					
2.79 ± 0.02 ± 0.02	27k	ADINOLFI	03	KLOE	
2.81 ± 0.01 ± 0.02		LAI	03	NA48	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
2.13 ± 0.43	28	BARMIN	71	HLBC	
2.24 ± 0.28	115	BANNER	69	OSPK	
2.5 ± 0.7	16	ARNOLD	68B	HLBC	Vacuum decay

$\Gamma(2\gamma)/\Gamma(\pi^0\pi^0)$					$\Gamma_{17}/\Gamma_9$
<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>		
<b>0.633±0.006 OUR FIT</b>	Error includes scale factor of 1.4.				
<b>0.632±0.004±0.008</b>	110k	BURKHARDT	87	NA31	

$\Gamma(3\gamma)/\Gamma_{\text{total}}$					$\Gamma_{18}/\Gamma$
<u>VALUE</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>		
<b>&lt;7.4 × 10<sup>-8</sup></b>	90	<sup>1</sup> TUNG	11	K391	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<2.4 × 10 <sup>-7</sup>	90	<sup>2</sup> BARR	95C	NA31	

<sup>1</sup> TUNG 11 reports the result assuming parity violating interaction and using 2005 data (Run-II and III). Assuming parity conserving or phase space interaction, the 90% upper limits obtained are  $7.5 \times 10^{-8}$  and  $8.6 \times 10^{-8}$ , respectively.

<sup>2</sup> Assumes a phase-space decay distribution.

$\Gamma(e^+e^-\gamma)/\Gamma_{\text{total}}$					$\Gamma_{19}/\Gamma$
<u>VALUE (units <math>10^{-6}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>		
<b>9.4±0.4 OUR FIT</b>	Error includes scale factor of 2.0.				
<b>10.0±0.5 OUR AVERAGE</b>	Error includes scale factor of 1.5. See the ideogram below.				
10.6 ± 0.2 ± 0.4	6864	<sup>1</sup> FANTI	99B	NA48	
9.2 ± 0.5 ± 0.5	1053	BARR	90B	NA31	
9.1 ± 0.4 <sup>+0.6</sup> <sub>-0.5</sub>	919	OHL	90B	B845	

<sup>1</sup> For FANTI 99B, the ±0.4 systematic error includes for uncertainties in the calculation, primarily uncertainties in the  $\pi^0 \rightarrow e^+e^-\gamma$  and  $K_L^0 \rightarrow \pi^0\pi^0$  branching ratios, evaluated using our 1999 Web edition values.

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NODE=S013R8

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NODE=S013R8;LINKAGE=R

NODE=S013R21

NODE=S013R21

NODE=S013R37

NODE=S013R37

NODE=S013R44

NODE=S013R44

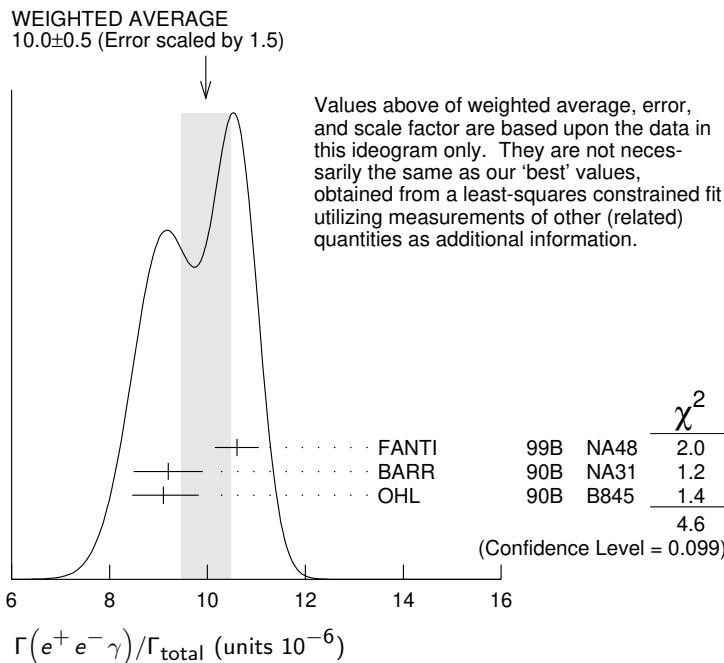
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NODE=S013R44;LINKAGE=A

NODE=S013R28

NODE=S013R28

NODE=S013R28;LINKAGE=FR



### $\Gamma(e^+ e^- \gamma)/\Gamma(3\pi^0)$

VALUE (units $10^{-5}$ )	EVTS	DOCUMENT ID	TECN
<b>4.82±0.21 OUR FIT</b>		Error includes scale factor of 2.0.	
<b>4.63±0.04±0.13</b>	83k	<sup>1</sup> ABOUZAID	07B KTEV

<sup>1</sup>ABOUZAID 07B reports  $[\Gamma(K_L^0 \rightarrow e^+ e^- \gamma)/\Gamma(K_L^0 \rightarrow 3\pi^0)] / [3\Gamma(\pi^0 \rightarrow 2\gamma)/\Gamma_{\text{total}} \times \Gamma(\pi^0 \rightarrow e^+ e^- \gamma)/\Gamma_{\text{total}}] = (1.3302 \pm 0.0046 \pm 0.0103) \times 10^{-3}$  which we multiply by our best value  $3\Gamma(\pi^0 \rightarrow 2\gamma)/\Gamma_{\text{total}} \times \Gamma(\pi^0 \rightarrow e^+ e^- \gamma)/\Gamma_{\text{total}} = 0.0348 \pm 0.0010$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.

### $\Gamma_{19}/\Gamma_6$

NODE=S013R61  
NODE=S013R61

### $\Gamma(\mu^+ \mu^- \gamma)/\Gamma_{\text{total}}$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN
<b>3.59±0.11 OUR AVERAGE</b>		Error includes scale factor of 1.3.	
3.62±0.04±0.08	9100	ALAVI-HARATI01G	KTEV
3.4 ± 0.6 ± 0.4	45	FANTI	97 NA48
3.23±0.23±0.19	197	SPENCER	95 E799

### $\Gamma_{20}/\Gamma$

NODE=S013R29  
NODE=S013R29

### $\Gamma(\mu^+ \mu^- \mu^+ \mu^-)/\Gamma_{\text{total}}$

VALUE	CL%	DOCUMENT ID	TECN
<b>&lt;2.3 × 10<sup>-9</sup></b>	90	<sup>1</sup> AAIJ	23AE LHCb

<sup>1</sup>AAIJ 23AE uses 5.1 fb<sup>-1</sup> of LHCb data recorded from 2016 to 2018.

### $\Gamma_{21}/\Gamma$

NODE=S013R01  
NODE=S013R01  
OCCUR=2  
NODE=S013R01;LINKAGE=A

### $\Gamma(e^+ e^- \gamma\gamma)/\Gamma_{\text{total}}$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>5.95±0.33 OUR AVERAGE</b>				
5.84±0.15±0.32	1543	ALAVI-HARATI01F	KTEV	$E_\gamma^* > 5 \text{ MeV}$
8.0 ± 1.5 ± 1.4	40	SETZU	98 NA31	$E_\gamma^* > 5 \text{ MeV}$
6.5 ± 1.2 ± 0.6	58	NAKAYA	94 E799	$E_\gamma^* > 5 \text{ MeV}$
6.6 ± 3.2		MORSE	92 B845	$E_\gamma^* > 5 \text{ MeV}$

### $\Gamma_{22}/\Gamma$

NODE=S013R41  
NODE=S013R41

### $\Gamma(\mu^+ \mu^- \gamma\gamma)/\Gamma_{\text{total}}$

VALUE (units $10^{-9}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>10.4<sup>+7.5</sup><sub>-5.9</sub>±0.7</b>	4	ALAVI-HARATI00E	KTEV	$m_{\gamma\gamma} \geq 1 \text{ MeV}/c^2$

### $\Gamma_{23}/\Gamma$

NODE=S013R52  
NODE=S013R52

— Charge conjugation × Parity (CP) or Lepton Family number (LF) —  
— violating modes, or  $\Delta S = 1$  weak neutral current (S1) modes —

NODE=S013430

$\Gamma(\mu^+\mu^-)/\Gamma(\pi^+\pi^-)$  $\Gamma_{24}/\Gamma_8$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-6}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.48 ± 0.05 OUR AVERAGE</b>				

3.474 ± 0.057	6210	AMBROSE	00	B871
3.87 ± 0.30	179	<sup>1</sup> AKAGI	95	SPEC
3.38 ± 0.17	707	HEINSON	95	B791

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.9 ± 0.3 ± 0.1	178	<sup>2</sup> AKAGI	91B	SPEC In AKAGI 95
3.45 ± 0.18 ± 0.13	368	<sup>3</sup> HEINSON	91	SPEC In HEINSON 95
4.1 ± 0.5	54	INAGAKI	89	SPEC In AKAGI 91B
2.8 ± 0.3 ± 0.2	87	MATHIAZHA...	89B	SPEC In HEINSON 91

<sup>1</sup> AKAGI 95 gives this number multiplied by the PDG 1992 average for  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma(\text{total})$ .<sup>2</sup> AKAGI 91B give this number multiplied by the 1990 PDG average for  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma(\text{total})$ .<sup>3</sup> HEINSON 91 give  $\Gamma(K_L^0 \rightarrow \mu\mu)/\Gamma_{\text{total}}$ . We divide out the  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}$  PDG average which they used. $\Gamma(e^+e^-)/\Gamma_{\text{total}}$  $\Gamma_{25}/\Gamma$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-10}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>0.087 ± 0.057</b>		4	AMBROSE	98 B871

• • • We do not use the following data for averages, fits, limits, etc. • • •

<1.6	90	1	AKAGI	95 SPEC
<0.41	90	0	<sup>1</sup> ARISAKA	93B B791

<sup>1</sup> ARISAKA 93B includes all events with <6 MeV radiated energy. $\Gamma(\pi^+\pi^-e^+e^-)/\Gamma_{\text{total}}$  $\Gamma_{26}/\Gamma$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-7}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.11 ± 0.19 OUR AVERAGE</b>					

3.08 ± 0.09 ± 0.18	1125	<sup>1</sup> LAI	03C	NA48
3.2 ± 0.6 ± 0.4	37	ADAMS	98	KTEV
4.4 ± 1.3 ± 0.5	13	TAKEUCHI	98	SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

<4.6	90	NOMURA	97	SPEC $m_{ee} > 4$ MeV
------	----	--------	----	-----------------------

<sup>1</sup> LAI 03C second error is  $0.15(\text{syst}) \pm 0.10(\text{norm})$  combined in quadrature. The normalization uses  $\text{BR}(K_L^0 \rightarrow \pi^+\pi^-\pi^0) * \text{BR}(\pi^0 \rightarrow e^+e^-) = (1.505 \pm 0.047) \times 10^{-3}$  from our 2000 Edition. $\Gamma(\pi^0\pi^0e^+e^-)/\Gamma_{\text{total}}$  $\Gamma_{27}/\Gamma$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>&lt;6.6</b>	90	1	ALAVI-HARATI02C	E799

 $\Gamma(\pi^0\pi^0\mu^+\mu^-)/\Gamma_{\text{total}}$  $\Gamma_{28}/\Gamma$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE	CL%	DOCUMENT ID	TECN
<b>&lt;9.2 × 10<sup>-11</sup></b>	90	<sup>1</sup> ABOUZAID	11A E799

<sup>1</sup> ABOUZAID 11A also reports  $\text{B}(K_L^0 \rightarrow \pi^0\pi^0X^0 \rightarrow \pi^0\pi^0\mu^+\mu^-) < 1.0 \times 10^{-10}$  at 90% C.L., where the  $X^0$  is a possible new neutral boson that was reported by PARK 05 with a mass of  $214.3 \pm 0.5$  MeV/c<sup>2</sup>. $\Gamma(\mu^+\mu^-e^+e^-)/\Gamma_{\text{total}}$  $\Gamma_{29}/\Gamma$ Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.69 ± 0.27 OUR AVERAGE</b>					

2.69 ± 0.24 ± 0.12	131	<sup>1</sup> ALAVI-HARATI03B	KTEV	
2.9 ± 6.7 -2.4	1	GU	96	E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.62 ± 0.40 ± 0.17	43	ALAVI-HARATI01H	KTEV	Sup. by ALAVI-HARATI 03B
<4900	90	BALATS	83	SPEC

<sup>1</sup> ALAVI-HARATI 03B also measures the linear slope  $\alpha = -1.59 \pm 0.37$ .

NODE=S013R22

NODE=S013R22

NODE=S013R22

NODE=S013R22;LINKAGE=G

NODE=S013R22;LINKAGE=D

NODE=S013R22;LINKAGE=B

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NODE=S013R31

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NODE=S013R31;LINKAGE=A

NODE=S013R54

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NODE=S013R54

NODE=S013R65

NODE=S013R65

NODE=S013R65

NODE=S013R65;LINKAGE=AB

NODE=S013R35

NODE=S013R35

NODE=S013R35

NODE=S013R35;LINKAGE=AL

$\Gamma(e^+e^-e^+e^-)/\Gamma_{\text{total}}$  $\Gamma_{30}/\Gamma$ 

Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-8}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.56±0.21 OUR AVERAGE</b>				
3.30±0.24±0.25	200	1 LAI	05B	NA48
3.72±0.18±0.23	441	ALAVI-HARATI01D	KTEV	
3.96±0.78±0.32	27	GU	94	E799
3.07±1.25±0.26	6	VAGINS	93	B845
• • • We do not use the following data for averages, fits, limits, etc. • • •				
6 ±2 ±1	18	2 AKAGI	95	SPEC $m_{ee} > 470$ MeV
7 ±3 ±2	6	2 AKAGI	95	SPEC $m_{ee} > 470$ MeV
10.4 ±3.7 ±1.1	8	3 BARR	95	NA31
6 ±2 ±1	18	AKAGI	93	CNTR Sup. by AKAGI 95
4 ±3	2	BARR	91	NA31 Sup. by BARR 95

1 LAI 05B uses 1998 and 1999 data. Data are normalized to the observed events of  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  ( $\pi^0$  into Dalitz pair) and PDG 04 values are used for  $B(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)$  and  $B(\pi^0 \rightarrow e^+ e^- \gamma)$ . The systematic error includes a normalization error of ±0.10.

2 Values are for the total branching fraction, acceptance-corrected for the  $m_{ee}$  cuts shown.

3 Distribution of angles between two  $e^+ e^-$  pair planes favors  $CP=-1$  for  $K_L^0$ .

 $\Gamma(\pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$  $\Gamma_{31}/\Gamma$ 

Violates  $CP$  in leading order. Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN
<0.38	90		ALAVI-HARATI00D	KTEV
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<5.1	90	0	HARRIS	93 E799

 $\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$  $\Gamma_{32}/\Gamma$ 

Violates  $CP$  in leading order. Direct and indirect  $CP$ -violating contributions are expected to be comparable and to dominate the  $CP$ -conserving part. LAI 02B result suggests that  $CP$ -violation effects dominate. Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-10}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
< 2.8	90		1 ALAVI-HARATI04A	KTEV	combined result
• • • We do not use the following data for averages, fits, limits, etc. • • •					
< 3.5	90		ALAVI-HARATI04A	KTEV	
< 0.0047 <sup>+0.0022</sup> <sub>-0.0018</sub>		2 LAI	02B	NA48	$CP$ -conserving part
< 5.1	90	2	ALAVI-HARATI01	KTEV	
0.01 to 0.02			ALAVI-HARATI99B	KTEV	$CP$ -conserving part
< 43	90	0	HARRIS	93B	E799
< 75	90	0	BARKER	90	E731
< 55	90	0	OHL	90	B845
< 400	90		BARR	88	NA31
<3200	90		JASTRZEM...	88	SPEC

1 Combined result of ALAVI-HARATI 04A 1999-2000 data set and ALAVI-HARATI 01 1997 data set.

2 LAI 02B uses the absence of a signal in  $K_L^0 \rightarrow \pi^0 \gamma \gamma$  with  $m(\gamma \gamma) < m(\pi^0)$  and their  $a_V$  value to predict this value.

 $\Gamma(\pi^0 \nu \bar{\nu})/\Gamma_{\text{total}}$  $\Gamma_{33}/\Gamma$ 

Violates  $CP$  in leading order. Test of direct  $CP$  violation since the indirect  $CP$ -violating and  $CP$ -conserving contributions are expected to be suppressed. Test of  $\Delta S = 1$  weak neutral current.

VALUE (units $10^{-8}$ )	CL%	DOCUMENT ID	TECN
< 0.49	90	1 AHN	21 KOTO
< 0.30	90	2 AHN	19 KOTO
• • • We do not use the following data for averages, fits, limits, etc. • • •			
< 5.1	90	3 AHN	17 KOTO
< 2.6	90	4 AHN	10 K391
< 6.7	90	5 AHN	08 K391
<21	90	6 AHN	06 K391
<59	90	ALAVI-HARATI00	KTEV

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NODE=S013R34

OCCUR=2

NODE=S013R34;LINKAGE=AL

NODE=S013R34;LINKAGE=LB

NODE=S013R40

NODE=S013R40

NODE=S013R40

OCCUR=2

<sup>1</sup> AHN 21 result is based on data collected in 2016, 2017 and 2018, which corresponds to  $3.05 \times 10^{19}$  protons on target. A single event sensitivity of  $(7.20 \pm 0.05 \pm 0.66) \times 10^{-10}$  was achieved with 3 candidate events observed and total  $1.22 \pm 0.26$  background events.

<sup>2</sup> AHN 19 result is based on data collected in 2015, which corresponds to  $2.2 \times 10^{19}$  protons on target. A single event sensitivity of  $(1.30 \pm 0.01 \pm 0.14) \times 10^{-9}$  was achieved with no candidate events observed. An upper limit of  $< 2.4 \times 10^{-9}$  at the 90% C.L. for the  $K_L \rightarrow \pi^0 X^0$  decay was also set, where  $X^0$  is an invisible particle with a mass of 135 MeV/c<sup>2</sup>.

<sup>3</sup> AHN 17 result is based on the first 100 hours of physics running in 2013. One candidate event was observed with an expected background of  $0.34 \pm 0.16$  events. An upper limit of  $< 3.7 \times 10^{-8}$  at the 90% C.L. for the  $K_L \rightarrow \pi^0 X^0$  decay was also set, where  $X^0$  is an invisible particle with a mass of 135 MeV/c<sup>2</sup>.

<sup>4</sup> Obtained combining Run-2 (AHN 08) and Run-3 data.

<sup>5</sup> Value obtained using data from February to April 2005.

<sup>6</sup> Value obtained analyzing 10% of data of RUN 1 (performed in 2004).

### $\Gamma(\pi^0 \pi^0 \nu \bar{\nu})/\Gamma_{\text{total}}$

VALUE	CL%	DOCUMENT ID	TECN
$< 8.1 \times 10^{-7}$	90	1 OGATA	11 K391
$< 4.7 \times 10^{-5}$	90	2 NIX	07 K391

<sup>1</sup> Using 2005 Run-I data. OGATA 11 also sets a limit on the  $K_L^0 \rightarrow \pi^0 \pi^0 X \rightarrow$  invisible particles process: the limit on the branching fraction varied from  $7.0 \times 10^{-7}$  to  $4.0 \times 10^{-5}$  for the mass of  $X$  ranging from 50 to 200 MeV/c<sup>2</sup>.

<sup>2</sup> Observed 1 event with expected background of  $0.43 \pm 0.35$  events. NIX 07 also measured  $B(K_L^0 \rightarrow \pi^0 \pi^0 P) < 1.2 \times 10^{-6}$  at 90% CL, where  $P$  is the pseudoscalar particle and  $m_P < 100$  MeV.

### $\Gamma(e^\pm \mu^\mp)/\Gamma_{\text{total}}$

Test of lepton family number conservation.					
VALUE (units $10^{-11}$ )	CL%	EVTS	DOCUMENT ID	TECN	
$< 0.47$	90	0	AMBROSE	98B	B871
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$					
$< 9.4$	90	0	AKAGI	95	SPEC
$< 3.9$	90	0	ARISAKA	93	B791
$< 3.3$	90	0	1 ARISAKA	93	B791

<sup>1</sup> This is the combined result of ARISAKA 93 and MATHIAZHAGAN 89.

### $\Gamma(e^\pm e^\pm \mu^\mp \mu^\mp)/\Gamma_{\text{total}}$

Test of lepton family number conservation.					
VALUE (units $10^{-11}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
$< 4.12$	90	0	ALAVI-HARATI03B	KTEV	
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$					
$< 12.3$	90	0	1 ALAVI-HARATI01H	KTEV	Sup. by ALAVI-HARATI 03B
$< 610$	90	0	1 GU	96	E799

<sup>1</sup> Assuming uniform phase space distribution.

### $\Gamma(\pi^0 \mu^\pm e^\mp)/\Gamma_{\text{total}}$

Test of lepton family number conservation.					
VALUE (units $10^{-10}$ )	CL%	DOCUMENT ID	TECN		
$< 0.76$	90	ABOUZAID	08C	KTEV	
$\bullet \bullet \bullet$ We do not use the following data for averages, fits, limits, etc. $\bullet \bullet \bullet$					
$< 62$	90	ARISAKA	98	E799	

### $\Gamma(\pi^0 \pi^0 \mu^\pm e^\mp)/\Gamma_{\text{total}}$

Test of lepton family number conservation.					
VALUE (units $10^{-10}$ )	CL%	DOCUMENT ID	TECN		
$< 1.7$	90	ABOUZAID	08C	KTEV	

### $\Gamma_{34}/\Gamma$

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NODE=S013R40;LINKAGE=D

NODE=S013R40;LINKAGE=B

NODE=S013R40;LINKAGE=NA  
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NODE=S013R63  
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NODE=S013R63;LINKAGE=OG

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OCCUR=2

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NODE=S013R48  
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NODE=S013R48;LINKAGE=A

NODE=S013R50  
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NODE=S013R64  
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NODE=S013R64

### $\Gamma_{35}/\Gamma$

NODE=S013R24

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NODE=S013R24

NODE=S013R50

NODE=S013R50

NODE=S013R50

### $\Gamma_{36}/\Gamma$

NODE=S013R48

NODE=S013R48

NODE=S013R48

NODE=S013R64

NODE=S013R64

NODE=S013R64

NODE=S013R64

NODE=S013R64

**Lorentz invariance violating modes**

$\Gamma(\pi^0\gamma)/\Gamma_{\text{total}}$	$CL\%$	DOCUMENT ID	TECN	$\Gamma_{39}/\Gamma$
$<1.7 \times 10^{-7}$	90	1 SHIMIZU	20 KOTO	

1 SHIMIZU 20 uses data collected from 2016 to 2018 at the J-PARC KOTO experiment. The single event sensitivity is  $(7.1 \pm 0.3 \pm 1.6) \times 10^{-8}$ . No candidate event was observed.

**See the related review(s):**

$V_{ud}$ ,  $V_{us}$  the Cabibbo Angle, and CKM Unitarity

**ENERGY DEPENDENCE OF  $K_L^0$  DALITZ PLOT**

For discussion, see note on Dalitz plot parameters in the  $K^\pm$  section of the Particle Listings above. For definitions of  $a_V$ ,  $a_t$ ,  $a_u$ , and  $a_Y$ , see the earlier version of the same note in the 1982 edition of this Review published in Physics Letters **111B** 70 (1982).

$$|\text{matrix element}|^2 = 1 + gu + hu^2 + jv + kv^2 + fuv \\ \text{where } u = (s_3 - s_0) / m_\pi^2 \text{ and } v = (s_2 - s_1) / m_\pi^2$$

**LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$** 

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.678 ± 0.008 OUR AVERAGE</b>				Error includes scale factor of 1.5. See the ideogram below.

0.6823 ± 0.0044 ± 0.0044	500k	ANGELOPO...	98C CPLR	
0.681 ± 0.024	6499	CHO	77 HBC	
0.620 ± 0.023	4709	PEACH	77 HBC	
0.677 ± 0.010	509k	MESSNER	74 ASPK	$a_y = -0.917 \pm 0.013$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.69 ± 0.07	192	1 BALDO-...	75 HLBC	
0.590 ± 0.022	56k	1 BUCHANAN	75 SPEC	$a_u = -0.277 \pm 0.010$
0.619 ± 0.027	20k	1,2 BISI	74 ASPK	$a_t = -0.282 \pm 0.011$
0.612 ± 0.032		1 ALEXANDER	73B HBC	
0.73 ± 0.04	3200	1 BRANDENB...	73 HBC	
0.608 ± 0.043	1486	1 KRENZ	72 HLBC	$a_t = -0.277 \pm 0.018$
0.650 ± 0.012	29k	1 ALBROW	70 ASPK	$a_y = -0.858 \pm 0.015$
0.593 ± 0.022	36k	1,3 BUCHANAN	70 SPEC	$a_u = -0.278 \pm 0.010$
0.664 ± 0.056	4400	1 SMITH	70 OSPK	$a_t = -0.306 \pm 0.024$
0.400 ± 0.045	2446	1 BASILE	68B OSPK	$a_t = -0.188 \pm 0.020$
0.649 ± 0.044	1350	1 HOPKINS	67 HBC	$a_t = -0.294 \pm 0.018$
0.428 ± 0.055	1198	1 NEFKENS	67 OSPK	$a_u = -0.204 \pm 0.025$

<sup>1</sup> Quadratic dependence required by some experiments. (See sections on “QUADRATIC COEFFICIENT  $h$ ” and “QUADRATIC COEFFICIENT  $k$ ” below.) Correlations prevent us from averaging results of fits not including  $g$ ,  $h$ , and  $k$  terms.

<sup>2</sup> BISI 74 value comes from quadratic fit with quad. term consistent with zero.  $g$  error is thus larger than if linear fit were used.

<sup>3</sup> BUCHANAN 70 result revised by BUCHANAN 75 to include radiative correlations and to use more reliable  $K_L^0$  momentum spectrum of second experiment (had same beam).

NODE=S013440

NODE=S013R00

NODE=S013R00

NODE=S013R00;LINKAGE=A

NODE=S013235

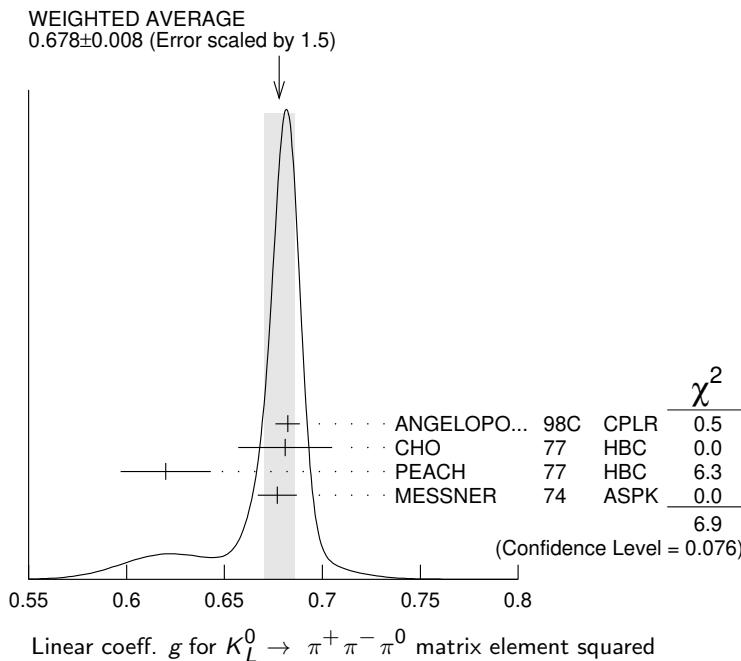
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NODE=S013GT0  
NODE=S013GT0

NODE=S013GT0;LINKAGE=Q

NODE=S013GT0;LINKAGE=C

NODE=S013GT0;LINKAGE=B



### QUADRATIC COEFFICIENT $h$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

See notes in section "LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  | MATRIX ELEMENT|<sup>2</sup>" above.

VALUE	EVTS	DOCUMENT ID	TECN	NODE
<b>0.076±0.006 OUR AVERAGE</b>				
0.061±0.004±0.015	500k	ANGELOPO...	98C CPLR	S013HT0
0.095±0.032	6499	CHO	77 HBC	S013HT0
0.048±0.036	4709	PEACH	77 HBC	S013HT0
0.079±0.007	509k	MESSNER	74 ASPK	S013HT0
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.011±0.018	29k	<sup>1</sup> ALBROW	70 ASPK	
0.043±0.052	4400	<sup>1</sup> SMITH	70 OSPK	

<sup>1</sup> Quadratic coefficients  $h$  and  $k$  required by some experiments. (See section on "QUADRATIC COEFFICIENT  $k$ " below.) Correlations prevent us from averaging results of fits not including  $g$ ,  $h$ , and  $k$  terms.

NODE=S013HT0;LINKAGE=Q

### QUADRATIC COEFFICIENT $k$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN	NODE
<b>0.0099±0.0015 OUR AVERAGE</b>				
0.0104±0.0017±0.0024	500k	ANGELOPO...	98C CPLR	S013KT0
0.024 ±0.010	6499	CHO	77 HBC	S013KT0
-0.008 ±0.012	4709	PEACH	77 HBC	S013KT0
0.0097±0.0018	509k	MESSNER	74 ASPK	S013KT0

### LINEAR COEFFICIENT $j$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ (CP-VIOLATING TERM)

Listed in CP-violation section below.

NODE=S013JTR  
NODE=S013JTR  
NODE=S013JTR

### QUADRATIC COEFFICIENT $f$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ (CP-VIOLATING TERM)

Listed in CP-violation section below.

NODE=S013FTR  
NODE=S013FTR  
NODE=S013FTR

### QUADRATIC COEFFICIENT $h$ FOR $K_L^0 \rightarrow \pi^0 \pi^0 \pi^0$

We do not average measurements that do not account for the effect of final state rescattering.

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	NODE
<b>+0.59±0.20±1.16</b>	68M	<sup>1</sup> ABOUZAID	08A KTEV	S013HTZ
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-6.1 ±0.9 ±0.5	14.7M	<sup>2</sup> LAI	01B NA48	S013HTZ
-3.3 ±1.1 ±0.7	5M	<sup>2,3</sup> SOMALWAR	92 E731	S013HTZ

- <sup>1</sup> Result obtained using CI3pl model of CABIBBO 05 to include  $\pi\pi$  rescattering effects. The systematic error includes an external error of  $1.06 \times 10^{-3}$  from the parametrization input of  $(a_0 - a_2) m_{\pi^+} = 0.268 \pm 0.017$  from BATLEY 06.
- <sup>2</sup> LAI 01B and SOMALWAR 92 results do not include  $\pi\pi$  final state rescattering effects.
- <sup>3</sup> SOMALWAR 92 chose  $m_{\pi^+}$  as normalization to make it compatible with the Particle Data Group  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  definitions.

## $K_L^0$ FORM FACTORS

For discussion, see note on form factors in the  $K^\pm$  section of the Particle Listings above.

In the form factor comments, the following symbols are used.

$f_+$  and  $f_-$  are form factors for the vector matrix element.

$f_S$  and  $f_T$  refer to the scalar and tensor term.

$$f_0(t) = f_+(t) + f_-(t) t / (m_{K^0}^2 - m_{\pi^+}^2).$$

$t$  = momentum transfer to the  $\pi$ .

$\lambda_+$  and  $\lambda_0$  are the linear expansion coefficients of  $f_+$  and  $f_0$ :

$$f_+(t) = f_+(0) (1 + \lambda_+ t / m_{\pi^+}^2)$$

For quadratic expansion

$$f_+(t) = f_+(0) (1 + \lambda'_+ t / m_{\pi^+}^2 + \frac{\lambda''_+}{2} t^2 / m_{\pi^+}^4)$$

as used by KTeV. If there is a non-vanishing quadratic term, then  $\lambda_+$

represents an average slope, which is then different from  $\lambda'_+$ .

NA48 ( $K_{e3}$ ) and ISTRA quadratic expansion coefficients are converted with

$$\lambda'_+{}^{PDG} = \lambda'_+{}^{NA48} \text{ and } \lambda''_+{}^{PDG} = 2 \lambda'_+{}^{NA48}$$

$$\lambda'_+{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda'_+{}^{ISTR A} \text{ and}$$

$$\lambda''_+{}^{PDG} = 2 (\frac{m_{\pi^+}}{m_{\pi^0}})^4 \lambda'_+{}^{ISTR A}$$

ISTR A linear expansion coefficients are converted with

$$\lambda'_+{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda'_+{}^{ISTR A} \text{ and } \lambda_0{}^{PDG} = (\frac{m_{\pi^+}}{m_{\pi^0}})^2 \lambda_0{}^{ISTR A}$$

The pole parametrization is

$$f_+(t) = f_+(0) \left( \frac{M_V^2}{M_V^2 - t} \right)$$

$$f_0(t) = f_0(0) \left( \frac{M_S^2}{M_S^2 - t} \right)$$

where  $M_V$  and  $M_S$  are the vector and scalar pole masses.

The dispersive parametrization is

$$f_+(t) = f_+(0) \exp \left[ \frac{t}{m_\pi^2} (\Lambda_+ + H(t)) \right];$$

$$f_0(t) = f_0(0) \exp \left[ \frac{t}{m_K^2 - m_\pi^2} (\ln[C] - G(t)) \right],$$

where  $\Lambda_+$  is the slope parameter and  $\ln[C] = \ln[f_0(m_K^2 - m_\pi^2)]$

is the logarithm of the scalar form factor at the Callan-Treiman point.

$H(t)$  and  $G(t)$  are dispersive integrals.

The following abbreviations are used:

DP = Dalitz plot analysis.

PI =  $\pi$  spectrum analysis.

MU =  $\mu$  spectrum analysis.

POL =  $\mu$  polarization analysis.

BR =  $K_{\mu 3}^0 / K_{e3}^0$  branching ratio analysis.

E = positron or electron spectrum analysis.

RC = radiative corrections.

## $\lambda_+$ (LINEAR ENERGY DEPENDENCE OF $f_+$ IN $K_{e3}^0$ DECAY)

For radiative correction of  $K_{e3}^0$  DP, see GINSBERG 67, BECHERRAWY 70, CIRIGLIANO 02, CIRIGLIANO 04, and ANDRE 07. Results labeled OUR FIT are discussed in the review "K $_{\ell 3}^\pm$  and K $_{\ell 3}^0$  Form Factors" in the K $^\pm$  Listings. For earlier,

NODE=S013HTZ;LINKAGE=AB

NODE=S013HTZ;LINKAGE=RE

NODE=S013HTZ;LINKAGE=A

NODE=S013240

NODE=S013240

lower statistics results, see the 2004 edition of this review, Physics Letters **B592** 1 (2004).

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.82 <math>\pm 0.04</math> OUR FIT</b>	Error includes scale factor of 1.1. Assuming $\mu$ -e universality			
<b>2.85 <math>\pm 0.04</math> OUR AVERAGE</b>				
2.86 $\pm 0.05$ $\pm 0.04$	2M	AMBROSINO 06D	KLOE	
2.832 $\pm 0.037$ $\pm 0.043$	1.9M	ALEXOPOU...	04A KTEV	PI, no $\mu = e$
2.88 $\pm 0.04$ $\pm 0.11$	5.6M	<sup>1</sup> LAI	04C NA48	DP
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>				
2.84 $\pm 0.07$ $\pm 0.13$	5.6M	<sup>2</sup> LAI	04C NA48	DP
2.45 $\pm 0.12$ $\pm 0.22$	366k	APOSTOLA...	00 CPLR	DP
3.06 $\pm 0.34$	74k	BIRULEV	81 SPEC	DP
3.12 $\pm 0.25$	500k	GJESDAL	76 SPEC	DP
2.70 $\pm 0.28$	25k	BLUMENTHAL75	SPEC	DP

<sup>1</sup> Results from linear fit and assuming only vector and axial couplings.

<sup>2</sup> Results from linear fit with  $|f_S/f_+|$  and  $|f_T/f_+|$  free.

### $\lambda_+$ (LINEAR ENERGY DEPENDENCE OF $f_+$ IN $K_{\ell 3}^0$ DECAY)

Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^\pm$  Listings. For earlier, lower statistics results, see the 2004 edition of this review, Physics Letters **B592** 1 (2004).

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.82 <math>\pm 0.04</math> OUR FIT</b>	Error includes scale factor of 1.1. Assuming $\mu$ -e universality			
<b>2.71 <math>\pm 0.10</math> OUR FIT</b>	Error includes scale factor of 1.4. Not assuming $\mu$ -e universality			
2.67 $\pm 0.06$ $\pm 0.08$	2.3M	<sup>1</sup> LAI	07A NA48	DP
2.745 $\pm 0.088$ $\pm 0.063$	1.5M	ALEXOPOU...	04A KTEV	DP, no $\mu = e$
2.813 $\pm 0.051$	3.4M	ALEXOPOU...	04A KTEV	PI, DP, $\mu = e$
3.0 $\pm 0.3$	1.6M	DONALDSON 74B	SPEC	DP
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>				
4.27 $\pm 0.44$	150k	BIRULEV	81 SPEC	DP

1 LAI 07A gives a correlation  $-0.40$  between their  $\lambda_0$  and  $\lambda_+$  measurements.

### $\lambda_0$ (LINEAR ENERGY DEPENDENCE OF $f_0$ IN $K_{\ell 3}^0$ DECAY)

Wherever possible, we have converted the above values of  $\xi(0)$  into values of  $\lambda_0$  using the associated  $\lambda_+^\mu$  and  $d\xi(0)/d\lambda_+$ . Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^\pm$  Listings. For earlier, lower statistics results, see the 2004 edition of this review, Physics Letters **B592** 1 (2004).

VALUE (units $10^{-2}$ )	$d\lambda_0/d\lambda_+$	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.38 <math>\pm 0.18</math> OUR FIT</b>	Error includes scale factor of 2.2. Assuming $\mu$ -e universality				
<b>1.42 <math>\pm 0.23</math> OUR FIT</b>	Error includes scale factor of 2.8. Not assuming $\mu$ -e universality				
1.17 $\pm 0.07$ $\pm 0.10$	2.3M	<sup>1</sup> LAI	07A NA48	DP	
1.657 $\pm 0.125$	-0.44	1.5M	<sup>2</sup> ALEXOPOU...	04A KTEV	DP, no $\mu = e$
1.635 $\pm 0.121$	-0.85	3.4M	<sup>3</sup> ALEXOPOU...	04A KTEV	PI, DP, $\mu = e$
+1.9 $\pm 0.4$	-0.47	1.6M	<sup>4</sup> DONALDSON 74B	SPEC	DP
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>					
3.41 $\pm 0.67$	unknown	150k	<sup>5</sup> BIRULEV	81 SPEC	DP

1 LAI 07A gives a correlation  $-0.40$  between their  $\lambda_0$  and  $\lambda_+$  measurements.

2 ALEXOPOULOS 04A gives a correlation  $-0.38$  between their  $\lambda_0$  and  $\lambda_+$  measurements.

3 ALEXOPOULOS 04A gives a correlation  $-0.36$  between their  $\lambda_0$  and  $\lambda_+$  measurements.

4 DONALDSON 74B  $d\lambda_0/d\lambda_+$  obtained from figure 18.

5 BIRULEV 81 gives  $d\lambda_0/d\lambda_+ = -1.5$ , giving an unreasonably narrow error ellipse which dominates all other results. We use  $d\lambda_0/d\lambda_+ = 0$ .

### $\lambda'_+$ (LINEAR $K_{e 3}^0$ FORM FACTOR FROM QUADRATIC FIT)

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.40 <math>\pm 0.12</math> OUR FIT</b>	Error includes scale factor of 1.2. Assuming $\mu$ -e universality			
<b>2.49 <math>\pm 0.13</math> OUR FIT</b>	Error includes scale factor of 1.1. Not assuming $\mu$ -e universality			
<b>2.48 <math>\pm 0.17</math> OUR AVERAGE</b>	Error includes scale factor of 1.5. See the ideogram below.			
2.55 $\pm 0.15$ $\pm 0.10$	2M	<sup>1</sup> AMBROSINO 06D	KLOE	
2.167 $\pm 0.137$ $\pm 0.143$	1.9M	<sup>2</sup> ALEXOPOU...	04A KTEV	PI, no $\mu = e$
2.80 $\pm 0.19$ $\pm 0.15$	5.6M	<sup>3</sup> LAI	04C NA48	DP

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OCCUR=2

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NODE=S013L+M

NODE=S013L+M

TYPE=noUNIV  
OCCUR=2;TYPE=UNIV

NODE=S013L+M;LINKAGE=LI

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NODE=S013L0

NODE=S013L0

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OCCUR=2;TYPE=UNIV

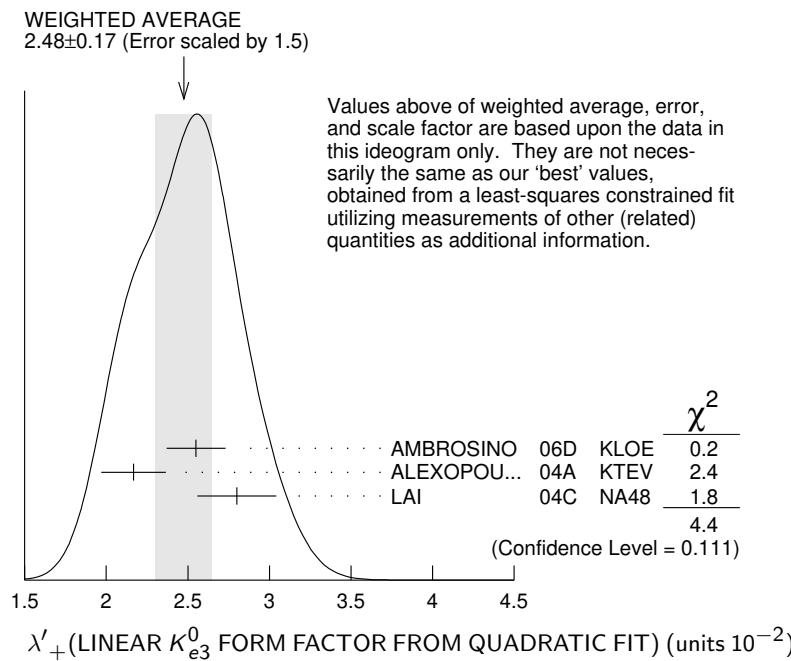
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NODE=S013L0;LINKAGE=AL  
NODE=S013L0;LINKAGE=AE  
NODE=S013L0;LINKAGE=E  
NODE=S013L0;LINKAGE=H

NODE=S013LPE  
NODE=S013LPE

TYPE=noUNIV  
TYPE=noUNIV

- <sup>1</sup>We use AMBROSINO 06D result in the fit not assuming  $\mu-e$  universality. This result enters the fit assuming  $\mu-e$  universality via AMBROSINO 07C measurement of  $\lambda'_+$  in  $K_{\mu 3}$  decays. AMBROSINO 06D gives a correlation  $-0.95$  between their  $\lambda'_+$  and  $\lambda''_+$ .  
<sup>2</sup>ALEXOPOULOS 04A gives a correlation  $-0.97$  between their  $\lambda'_+$  and  $\lambda''_+$ .  
<sup>3</sup>For LAI 04C we calculate a correlation  $-0.88$  between their  $\lambda'_+$  and  $\lambda''_+$ .

NODE=S013LPE;LINKAGE=AM

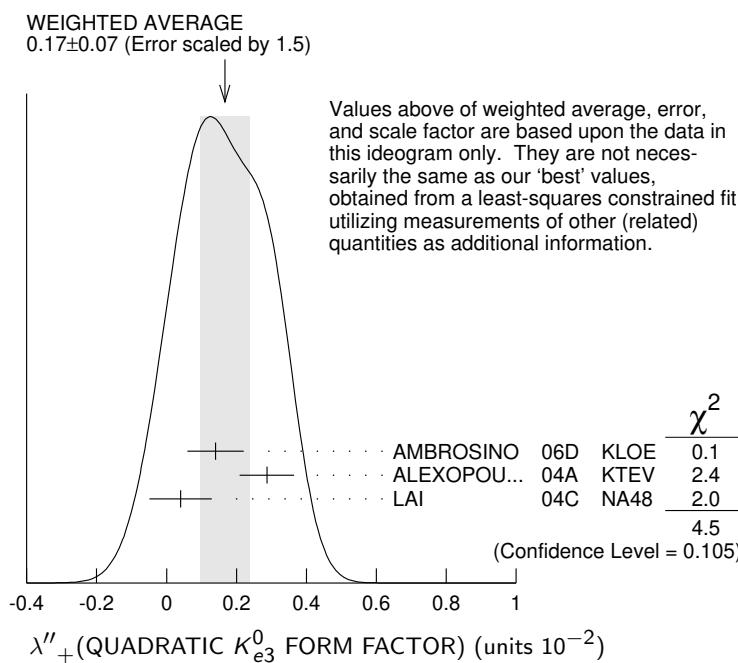
NODE=S013LPE;LINKAGE=AL  
NODE=S013LPE;LINKAGE=LA **$\lambda''_+ (\text{QUADRATIC } K^0_{e3} \text{ FORM FACTOR})$** 

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>0.20 \pm 0.05</math> OUR FIT</b>		Error includes scale factor of 1.2. Assuming $\mu-e$ universality		
<b><math>0.16 \pm 0.05</math> OUR FIT</b>		Error includes scale factor of 1.1. Not assuming $\mu-e$ universality		
<b><math>0.17 \pm 0.07</math> OUR AVERAGE</b>		Error includes scale factor of 1.5. See the ideogram below.		
0.14 $\pm 0.07 \pm 0.04$	2M	<sup>1</sup> AMBROSINO 06D	KLOE	
$0.287 \pm 0.057 \pm 0.053$	1.9M	<sup>2</sup> ALEXOPOU... 04A	KTEV	PI, no $\mu = e$
0.04 $\pm 0.08 \pm 0.04$	5.6M	LAI 04C	NA48	DP

- <sup>1</sup>We use AMBROSINO 06D result in the fit not assuming  $\mu-e$  universality. This result enters the fit assuming  $\mu-e$  universality via AMBROSINO 07C measurement of  $\lambda''_+$  in  $K_{\mu 3}$  decays. AMBROSINO 06D gives a correlation  $-0.95$  between their  $\lambda'_+$  and  $\lambda''_+$ .  
<sup>2</sup>ALEXOPOULOS 04A gives a correlation  $-0.97$  between their  $\lambda'_+$  and  $\lambda''_+$ .  
<sup>3</sup>Values doubled to agree with PDG conventions described above.  
<sup>4</sup>LAI 04C gives a correlation  $-0.88$  between their  $\lambda'_+$  and  $\lambda''_+$ .

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NODE=S013LQETYPE=noUNIV  
TYPE=noUNIV

NODE=S013LQE;LINKAGE=AM

NODE=S013LQE;LINKAGE=AL  
NODE=S013LQE;LINKAGE=DB  
NODE=S013LQE;LINKAGE=LA

### $\lambda'_+$ (LINEAR $K_{\mu 3}^0$ FORM FACTOR FROM QUADRATIC FIT)

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.40 <math>\pm 0.12</math> OUR FIT</b>		Error includes scale factor of 1.2. Assuming $\mu$ -e universality		
<b>1.89 <math>\pm 0.24</math> OUR FIT</b>		Not assuming $\mu$ -e universality		
2.23 $\pm 0.98$ $\pm 0.37$	1.8M	<sup>1</sup> AMBROSINO 07C KLOE	no $\mu = e$	
2.56 $\pm 0.15$ $\pm 0.09$	3.8M	<sup>1</sup> AMBROSINO 07C KLOE	$\mu = e$	
2.05 $\pm 0.22$ $\pm 0.24$	2.3M	<sup>1</sup> LAI 07A NA48	DP	
1.703 $\pm 0.319$ $\pm 0.177$	1.5M	<sup>1</sup> ALEXOPOU... 04A KTEV	DP, no $\mu = e$	
2.064 $\pm 0.175$	3.4M	<sup>1</sup> ALEXOPOU... 04A KTEV	PI, DP, $\mu = e$	

<sup>1</sup> See section  $\lambda_0$  below for correlations.

### $\lambda''_+$ (QUADRATIC $K_{\mu 3}^0$ FORM FACTOR)

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.20 <math>\pm 0.05</math> OUR FIT</b>		Error includes scale factor of 1.2. Assuming $\mu$ -e universality		
<b>0.37 <math>\pm 0.12</math> OUR FIT</b>		Error includes scale factor of 1.3. Not assuming $\mu$ -e universality		
0.48 $\pm 0.49$ $\pm 0.16$	1.8M	<sup>1</sup> AMBROSINO 07C KLOE	no $\mu = e$	
0.15 $\pm 0.07$ $\pm 0.04$	3.8M	<sup>1</sup> AMBROSINO 07C KLOE	$\mu = e$	
0.26 $\pm 0.09$ $\pm 0.10$	2.3M	<sup>1</sup> LAI 07A NA48	DP	
0.443 $\pm 0.131$ $\pm 0.072$	1.5M	<sup>1</sup> ALEXOPOU... 04A KTEV	DP, no $\mu = e$	
0.320 $\pm 0.069$	3.4M	<sup>1</sup> ALEXOPOU... 04A KTEV	PI, DP, $\mu = e$	

<sup>1</sup> See section  $\lambda_0$  below for correlations.

### $\lambda_0$ (LINEAR $f_0 K_{\mu 3}^0$ FORM FACTOR FROM QUADRATIC FIT)

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.16 <math>\pm 0.09</math> OUR FIT</b>		Error includes scale factor of 1.2. Assuming $\mu$ -e universality		
<b>1.07 <math>\pm 0.14</math> OUR FIT</b>		Error includes scale factor of 1.3. Not assuming $\mu$ -e universality		
0.91 $\pm 0.59$ $\pm 0.26$	1.8M	<sup>1</sup> AMBROSINO 07C KLOE	no $\mu = e$	
1.54 $\pm 0.18$ $\pm 0.13$	3.8M	<sup>2</sup> AMBROSINO 07C KLOE	$\mu = e$	
0.95 $\pm 0.11$ $\pm 0.08$	2.3M	<sup>3</sup> LAI 07A NA48	DP	
1.281 $\pm 0.136$ $\pm 0.122$	1.5M	<sup>4</sup> ALEXOPOU... 04A KTEV	DP, no $\mu = e$	
1.372 $\pm 0.131$	3.4M	<sup>5</sup> ALEXOPOU... 04A KTEV	PI, DP, $\mu = e$	

<sup>1</sup> AMBROSINO 07C, not assuming  $\mu$ -e universality, gives a correlation matrix

$$\begin{array}{ccc} \lambda'_+ & \lambda''_+ \\ \lambda''_+ & -0.97 & 1 \\ \lambda_0 & 0.81 & -0.91 \end{array}$$

<sup>2</sup> AMBROSINO 07C, assuming  $\mu$ -e universality, gives a correlation matrix

$$\begin{array}{ccc} \lambda'_+ & \lambda''_+ \\ \lambda''_+ & -0.95 & 1 \\ \lambda_0 & 0.29 & -0.38 \end{array}$$

<sup>3</sup> LAI 07A gives a correlation matrix

$$\begin{array}{ccc} \lambda'_+ & \lambda''_+ \\ \lambda''_+ & -0.96 & 1 \\ \lambda_0 & 0.63 & -0.73 \end{array}$$

<sup>4</sup> ALEXOPOULOS 04A, not assuming  $\mu$ -e universality, gives a correlation matrix

$$\begin{array}{ccc} \lambda'_+ & \lambda''_+ & \lambda_0 \\ \lambda'_+ & 1 & \\ \lambda''_+ & -0.96 & 1 \\ \lambda_0 & 0.65 & -0.75 & 1 \end{array}$$

<sup>5</sup> ALEXOPOULOS 04A, assuming  $\mu$ -e universality, gives a correlation matrix

$$\begin{array}{ccc} \lambda'_+ & \lambda''_+ & \lambda_0 \\ \lambda'_+ & 1 & \\ \lambda''_+ & -0.97 & 1 \\ \lambda_0 & 0.34 & -0.44 & 1 \end{array}$$

### $M_V^e$ (POLE MASS FOR $K_{e 3}^0$ DECAY)

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>878 <math>\pm 6</math> OUR FIT</b>		Error includes scale factor of 1.1. Assuming $\mu$ -e universality		
<b>875 <math>\pm 5</math> OUR AVERAGE</b>				
870 $\pm 6$ $\pm 7$	2M	AMBROSINO 06D KLOE		
881.03 $\pm 5.12 \pm 4.94$	1.9M	ALEXOPOU... 04A KTEV	PI, no $\mu = e$	
859 $\pm 18$	5.6M	LAI 04C NA48		

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NODE=S013LQM;LINKAGE=AL

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NODE=S013LZ;LINKAGE=LA

NODE=S013LZ;LINKAGE=AL

NODE=S013LZ;LINKAGE=AE

NODE=S013MVE  
NODE=S013MVE

TYPE=noUNIV

### $M_V^\mu$ (POLE MASS FOR $K_{\mu 3}^0$ DECAY)

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
878 $\pm$ 6 <b>OUR FIT</b>		Error includes scale factor of 1.1. Assuming $\mu$ -e universality		
900 $\pm$ 21 <b>OUR FIT</b>		Error includes scale factor of 1.7. Not assuming $\mu$ -e universality		
905 $\pm$ 9 $\pm$ 17	2.3M	<sup>1</sup> LAI 07A NA48 DP		
889.19 $\pm$ 12.81 $\pm$ 9.92	1.5M	<sup>1</sup> ALEXOPOU... 04A KTEV DP, no $\mu = e$		
882.32 $\pm$ 6.54	3.4M	<sup>1</sup> ALEXOPOU... 04A KTEV PI, DP, $\mu = e$		

<sup>1</sup> See section  $M_S^\mu$  below for correlations.

### $M_S^\mu$ (POLE MASS FOR $K_{\mu 3}^0$ DECAY)

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
1250 $\pm$ 90 <b>OUR FIT</b>		Error includes scale factor of 2.6. Assuming $\mu$ -e universality		
1220 $\pm$ 80 <b>OUR FIT</b>		Error includes scale factor of 2.3. Not assuming $\mu$ -e universality		
1400 $\pm$ 46 $\pm$ 53	2.3M	<sup>1</sup> LAI 07A NA48 DP		
1167.14 $\pm$ 28.30 $\pm$ 31.04	1.5M	<sup>2</sup> ALEXOPOU... 04A KTEV PI, no $\mu = e$		
1173.80 $\pm$ 39.47	3.4M	<sup>3</sup> ALEXOPOU... 04A KTEV PI, DP, $\mu = e$		

<sup>1</sup> LAI 07A gives a correlation  $-0.47$  between their  $M_S^\mu$  and  $M_V^\mu$  measurements, not assuming  $\mu$ -e universality.

<sup>2</sup> ALEXOPOULOS 04A gives a correlation  $-0.46$  between their  $M_S^\mu$  and  $M_V^\mu$  and measurements, not assuming  $\mu$ -e universality.

<sup>3</sup> ALEXOPOULOS 04A gives a correlation  $-0.40$  between their  $M_S^\mu$  and  $M_V^\mu$  and measurements, assuming  $\mu$ -e universality.

### $\Lambda_+$ (DISPERSIVE VECTOR FORM FACTOR FOR $K_{\mu 3}^0$ DECAY)

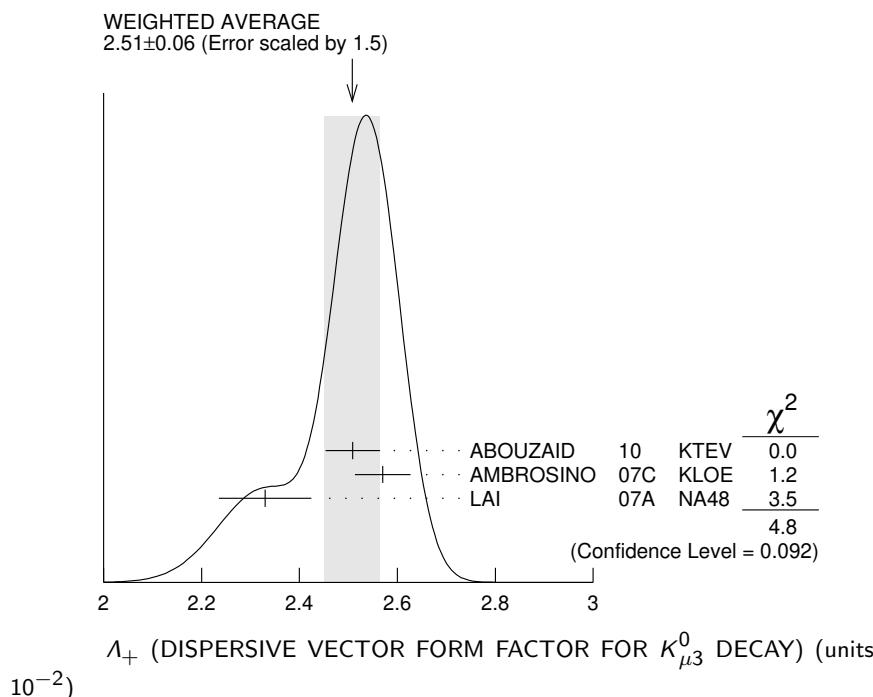
See the review on " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" for details of the dispersive parametrization.

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.51 <math>\pm</math> 0.06 OUR AVERAGE</b>		Error includes scale factor of 1.5. See the ideogram below.		
2.509 $\pm$ 0.035 $\pm$ 0.043	3.4M	<sup>1</sup> ABOUZAID 10 KTEV $\mu = e$		
2.57 $\pm$ 0.04 $\pm$ 0.04	3.8M	<sup>2</sup> AMBROSINO 07C KLOE $\mu = e$		
2.33 $\pm$ 0.05 $\pm$ 0.08	2.3M	<sup>3</sup> LAI 07A NA48 DP		

<sup>1</sup> Obtained from a sample of 1.9 M  $K_{e3}$  and 1.5 M  $K_{\mu 3}$ . The correlation between  $\Lambda_+$  and  $\ln(C)$  is  $-0.269$ .

<sup>2</sup> AMBROSINO 07C results include 2M  $K_{e3}$  events from AMBROSINO 06D. The correlation between  $\Lambda_+$  and  $\ln(C)$  is  $-0.26$ .

<sup>3</sup> LAI 07A gives a correlation  $-0.44$  between their  $\Lambda_+$  and  $\ln(C)$  measurements.



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NODE=S013MVM

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NODE=S013MVM;LINKAGE=AL

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NODE=S013MSM

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NODE=S013MSM;LINKAGE=LA

NODE=S013MSM;LINKAGE=AL

NODE=S013MSM;LINKAGE=AE

NODE=S013LAM

NODE=S013LAM

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TYPE=UNIV

TYPE=UNIV

NODE=S013LAM;LINKAGE=AB

NODE=S013LAM;LINKAGE=AM

NODE=S013LAM;LINKAGE=LA

## $\ln(C)$ (DISPERSIVE SCALAR FORM FACTOR FOR $K_{\mu 3}^0$ DECAY)

See the review on " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" for details of the dispersive parametrization.

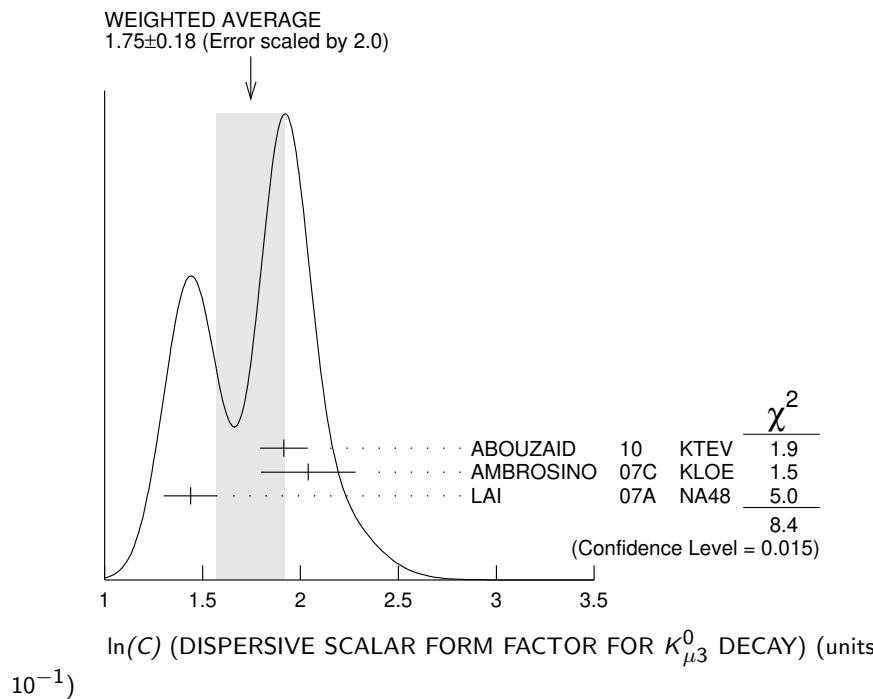
VALUE (units $10^{-1}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.75 ± 0.18 OUR AVERAGE</b>				Error includes scale factor of 2.0. See the ideogram below.
1.915 ± 0.078 ± 0.094	3.4M	<sup>1</sup> ABOUZAID	10 KTEV	$\mu = e$
2.04 ± 0.19 ± 0.15	3.8M	<sup>2</sup> AMBROSINO	07C KLOE	$\mu = e$

1.438 ± 0.080 ± 0.112 2.3M <sup>3</sup> LAI 07A NA48 DP

1 Obtained from a sample of 1.9 M  $K_{e3}$  and 1.5 M  $K_{\mu 3}$ . The correlation between  $\Lambda_+$  and  $\ln(C)$  is -0.269.

2 AMBROSINO 07C results include 2M  $K_{e3}$  events from AMBROSINO 06D. We convert  $(\Lambda_+, \Lambda_0)$  to  $(\Lambda_+, \ln(C))$  parametrization using  $\ln(C) = (\Lambda_0 \cdot 11.713 + 0.0398) \pm 0.0041$ , where the error is due to theory parametrization of the form factor. The correlation between  $\Lambda_+$  and  $\ln(C)$  is -0.26.

3 LAI 07A gives a correlation -0.44 between their  $\Lambda_+$  and  $\ln(C)$  measurements.



## $a_1(t_0, Q^2)$ FORM FACTOR PARAMETER

See HILL 06 for a definition of this parameter.

VALUE	EVTS	DOCUMENT ID	TECN
<b>1.023 ± 0.028 ± 0.029</b>	2M	<sup>1</sup> ABOUZAID	06C KTEV

<sup>1</sup>  $Q^2 = 2 \text{ GeV}^2$ ,  $t_0 = 0.49 (m_K - m_\pi)^2$ . Correlation between  $a_1$  and  $a_2$ :  $\rho_{12} = -0.064$ .

## $a_2(t_0, Q^2)$ FORM FACTOR PARAMETER

See HILL 06 for a definition of this parameter.

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.75 ± 1.58 ± 1.47</b>	2M	<sup>1</sup> ABOUZAID	06C KTEV

<sup>1</sup>  $Q^2 = 2 \text{ GeV}^2$ ,  $t_0 = 0.49 (m_K - m_\pi)^2$ . Correlation between  $a_1$  and  $a_2$ :  $\rho_{12} = -0.064$ .

## $|f_S/f_+|$ FOR $K_{e3}^0$ DECAY

Ratio of scalar to  $f_+$  couplings.

VALUE (units $10^{-2}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.5<sup>+0.7</sup><sub>-1.0</sub> ± 1.2</b>		5.6M	<sup>1</sup> LAI	04C NA48	

• • • We do not use the following data for averages, fits, limits, etc. • • •

<9.5	95	18k	HILL	78	STRC
<7.	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<4.	68	25k	BLUMENTHAL75		SPEC

<sup>1</sup> Results from linear fit with  $|f_S/f_+|$  and  $|f_T/f_+|$  free.

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NODE=S013HA2

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NODE=S013FS

NODE=S013FS

NODE=S013FS

NODE=S013FS;LINKAGE=LA

## $|f_T/f_+|$ FOR $K_{e3}^0$ DECAY

Ratio of tensor to  $f_+$  couplings.

VALUE (units $10^{-2}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
$5^{+3}_{-4} \pm 3$		5.6M	1 LAI	04C	NA48

• • • We do not use the following data for averages, fits, limits, etc. • • •

<40.	95	18k	HILL	78	STRC
<34.	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<23.	68	25k	BLUMENTHAL75		SPEC

<sup>1</sup> Results from linear fit with  $|f_S/f_+|$  and  $|f_T/f_+|$  free.

NODE=S013FT

NODE=S013FT

NODE=S013FT

## $|f_T/f_+|$ FOR $K_{\mu 3}^0$ DECAY

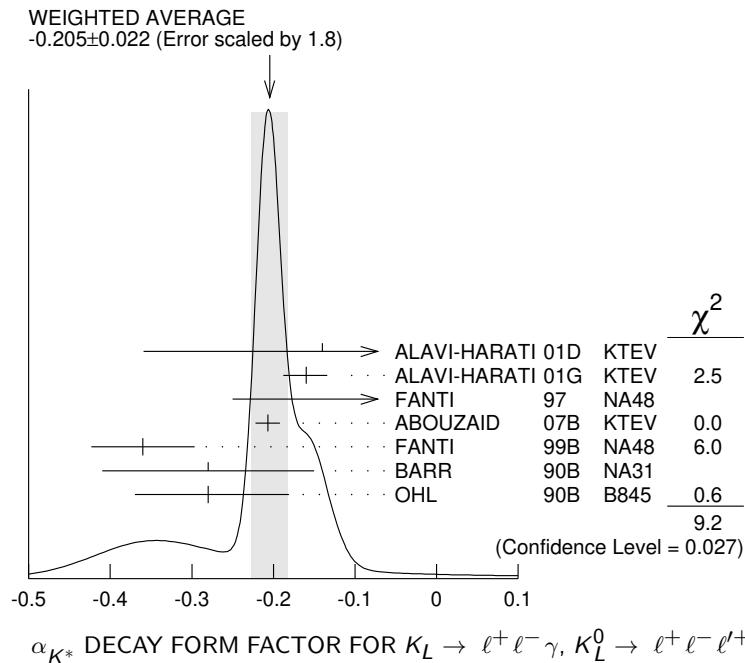
Ratio of tensor to  $f_+$  couplings.

VALUE (units $10^{-2}$ )	DOCUMENT ID	TECN
12. $\pm$ 12.	BIRULEV	81

## $\alpha_{K^*}$ DECAY FORM FACTOR FOR $K_L \rightarrow \ell^+ \ell^- \gamma$ , $K_L^0 \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-$

Average of all  $\alpha_{K^*}$  measurements (from each of three datablocks following this one) assuming lepton universality.

**-0.205  $\pm$  0.022 OUR AVERAGE** Includes data from the 3 datablocks that follow this one. Error includes scale factor of 1.8. See the ideogram below.



$\alpha_{K^*}$  DECAY FORM FACTOR FOR  $K_L \rightarrow \ell^+ \ell^- \gamma$ ,  $K_L^0 \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-$

## $\alpha_{K^*}$ DECAY FORM FACTOR FOR $K_L \rightarrow e^+ e^- \gamma$

$\alpha_{K^*}$  is the constant in the model of BERGSTROM 83 which measures the relative strength of the vector-vector transition  $K_L \rightarrow K^* \gamma$  with  $K^* \rightarrow \rho, \omega, \phi \rightarrow \gamma^*$  and the pseudoscalar-pseudoscalar transition  $K_L \rightarrow \pi, \eta, \eta' \rightarrow \gamma\gamma^*$ .

VALUE	EVTS	DOCUMENT ID	TECN
The data in this block is included in the average printed for a previous datablock.			

<b>-0.217 <math>\pm</math> 0.034 OUR AVERAGE</b>	Error includes scale factor of 2.4.
-0.207 $\pm$ 0.012 $\pm$ 0.009	83k
-0.36 $\pm$ 0.06 $\pm$ 0.02	6864
-0.28 $\pm$ 0.13	
-0.280 $^{+0.099}_{-0.090}$	OHL
	90B
	B845

<sup>1</sup> ABOUZAID 07B measures  $C \cdot \alpha_{K^*} = -0.517 \pm 0.030 \pm 0.022$ . We assume  $C = 2.5$ , as in all other measurements.

NODE=S013ALP

NODE=S013ALP

NODE=S013ALP

NODE=S013ALP;LINKAGE=AB

**$\alpha_{K^*}$  DECAY FORM FACTOR FOR  $K_L \rightarrow \mu^+ \mu^- \gamma$** 

$\alpha_{K^*}$  is the constant in the model of BERGSTROM 83 described in the previous section.

VALUE	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

 **$-0.158 \pm 0.027$  OUR AVERAGE**

$-0.160^{+0.026}_{-0.028}$	9100	ALAVI-HARATI01G	KTEV
$-0.04^{+0.24}_{-0.21}$	FANTI	97	NA48

 **$\alpha_{K^*}^{\text{eff}}$  DECAY FORM FACTOR FOR  $K_L \rightarrow e^+ e^- e^+ e^-$** 

$\alpha_{K^*}^{\text{eff}}$  is the parameter describing the relative strength of an intermediate pseudoscalar decay amplitude and a vector meson decay amplitude in the model of BERGSTROM 83. It takes into account both the radiative effects and the form factor. Since there are two  $e^+ e^-$  pairs here compared with one in  $e^+ e^- \gamma$  decays, a factorized expression is used for the  $e^+ e^- e^+ e^-$  decay form factor.

VALUE	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

**$-0.14 \pm 0.16 \pm 0.15$**  441 ALAVI-HARATI01D KTEV

 **$\alpha_{DIP}$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \ell^+ \ell^- \gamma, K_L^0 \rightarrow \ell^+ \ell^- \ell^+ \ell^-$** 

Average of all  $\alpha_{DIP}$  measurements (from each of three datablocks following this one) assuming lepton universality.

VALUE	EVTS	DOCUMENT ID	TECN
-------	------	-------------	------

**$-1.69 \pm 0.08$  OUR AVERAGE** Includes data from the 3 datablocks that follow this one. Error includes scale factor of 1.7.

 **$\alpha_{DIP}$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow e^+ e^- \gamma$** 

$\alpha_{DIP}$  parameter in  $K_L^0 \rightarrow \gamma^* \gamma^*$  form factor by DAMBROSIO 98, motivated by vector meson dominance and a proper short distance behavior.

VALUE	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

**$-1.729 \pm 0.043 \pm 0.028$**  83k ABOUZAID 07B KTEV

 **$\alpha_{DIP}$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \mu^+ \mu^- \gamma$** 

$\alpha_{DIP}$  is a constant in the model of DAMBROSIO 98 described in the previous section.

VALUE	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

**$-1.54 \pm 0.10$**  9100 ALAVI-HARATI01G KTEV

 **$\alpha_{DIP}$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow e^+ e^- \mu^+ \mu^-$** 

$\alpha_{DIP}$  is a constant in the model of DAMBROSIO 98 described in the previous section.

VALUE	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

**$-1.59 \pm 0.37$**  131 ALAVI-HARATI03B KTEV

 **$a_1/a_2$  FORM FACTOR FOR M1 DIRECT EMISSION AMPLITUDE**

Form factor =  $\tilde{g}_{M1} \left[ 1 + \frac{a_1/a_2}{(M_P^2 - M_K^2) + 2M_K E_\gamma^*} \right]$  as described in ALAVI-HARATI 00B.

VALUE (GeV <sup>2</sup> )	EVTS	DOCUMENT ID	TECN	COMMENT
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 **$-0.737 \pm 0.014$  OUR AVERAGE**

$-0.744 \pm 0.027 \pm 0.032$	5241	1 ABOUZAID	06	KTEV	$\pi^+ \pi^- e^+ e^-$
$-0.738 \pm 0.007 \pm 0.018$	111k	2 ABOUZAID	06A	KTEV	$\pi^+ \pi^+ \gamma$
$-0.81^{+0.07}_{-0.13}$ $\pm 0.02$		3 LAI	03C	NA48	$\pi^+ \pi^- e^+ e^-$
$-0.737 \pm 0.026 \pm 0.022$		4 ALAVI-HARATI01B			$\pi^+ \pi^- \gamma$
$-0.720 \pm 0.028 \pm 0.009$	1766	5 ALAVI-HARATI00B		KTEV	$\pi^+ \pi^- e^+ e^-$

1 ABOUZAID 06 also measured  $|\tilde{g}_{M1}| = 1.11 \pm 0.14$ .

2 ABOUZAID 06A also measured  $|\tilde{g}_{M1}| = 1.198 \pm 0.035 \pm 0.086$ .

3 LAI 03C also measured  $\tilde{g}_{M1} = 0.99^{+0.28}_{-0.27} \pm 0.07$ .

4 ALAVI-HARATI 01B fit gives  $\chi^2/\text{DOF} = 38.8/27$ . Linear and quadratic fits give  $\chi^2/\text{DOF} = 43.2/27$  and  $37.6/26$  respectively.

5 ALAVI-HARATI 00B also measured  $|\tilde{g}_{M1}| = 1.35^{+0.20}_{-0.17} \pm 0.04$ .

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NODE=S013ALM

NODE=S013ALE

NODE=S013ALE

NODE=S013ALE

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NODE=S013A12;LINKAGE=LA

NODE=S013A12;LINKAGE=AH

NODE=S013A12;LINKAGE=AL

**$\bar{f}_S$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$** 

VALUE	DOCUMENT ID	TECN
<b>0.049±0.011 OUR AVERAGE</b>		Error includes scale factor of 1.7.
0.052±0.006±0.002	BATLEY 04	NA48
0.010±0.016±0.017	MAKOFF 93	E731

NODE=S013FSB  
NODE=S013FSB **$\bar{f}_P$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$** 

VALUE	DOCUMENT ID	TECN
<b>-0.052±0.012 OUR AVERAGE</b>		
-0.051±0.011±0.005	BATLEY 04	NA48
-0.079±0.049±0.022	MAKOFF 93	E731

NODE=S013FPB  
NODE=S013FPB **$\lambda_g$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$** 

VALUE	DOCUMENT ID	TECN
<b>0.085±0.020 OUR AVERAGE</b>		
0.087±0.019±0.006	BATLEY 04	NA48
0.014±0.087±0.070	MAKOFF 93	E731

NODE=S013LMG  
NODE=S013LMG **$\bar{h}$  DECAY FORM FACTOR FOR  $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$** 

VALUE	DOCUMENT ID	TECN
<b>-0.30±0.13 OUR AVERAGE</b>		
-0.32±0.12±0.07	BATLEY 04	NA48
-0.07±0.31±0.31	MAKOFF 93	E731

NODE=S013HB  
NODE=S013HB **$L_3$  CHIRAL PERT. THEO. PARAM. FOR  $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$** 

VALUE (units $10^{-3}$ )	DOCUMENT ID	TECN
<b>-3.96±0.28 OUR AVERAGE</b>		Error includes scale factor of 1.6.
-4.1 ± 0.2	BATLEY 04	NA48
-3.4 ± 0.4	1 MAKOFF 93	E731

NODE=S013L3  
NODE=S013L3

<sup>1</sup> MAKOFF 93 sign has been changed to negative to agree with the sign convention used in BATLEY 04.

NODE=S013L3;LINKAGE=MA

 **$a_V$ , VECTOR MESON EXCHANGE CONTRIBUTION**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.43±0.06 OUR AVERAGE</b>				Error includes scale factor of 1.5.
-0.31±0.05±0.07	1.4k	1 ABOUZAID 08	KTEV	
-0.46±0.03±0.04		LAI 02B	NA48	$K_L^0 \rightarrow \pi^0 2\gamma$
-0.67±0.21±0.12		ALAVI-HARATI01E	KTEV	$K_L^0 \rightarrow \pi^0 e^+ e^- \gamma$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.72±0.05±0.06		2 ALAVI-HARATI99B	KTEV	$K_L^0 \rightarrow \pi^0 2\gamma$

NODE=S013AV  
NODE=S013AV

<sup>1</sup> Using KTeV dataset collected in 1996, 1997, and 1999.

<sup>2</sup> Superseded by ABOUZAID 08.

NODE=S013AV;LINKAGE=AB  
NODE=S013AV;LINKAGE=AL**See the related review(s):**

[CP Violation in  \$K\_L^0\$  Decays](#)

**CP-VIOLATION PARAMETERS IN  $K_L^0$  DECAYS****— CHARGE ASYMMETRY IN  $K_{l3}^0$  DECAYS —**

Such asymmetry violates CP. It is related to  $\text{Re}(\epsilon)$ .

 **$A_L$  = weighted average of  $A_L(\mu)$  and  $A_L(e)$** 

In previous editions and in the literature the symbol used for this asymmetry was  $\delta_L$  or  $\delta$ . We use  $A_L$  for consistency with  $B^0$  asymmetry notation and with recent  $K_S^0$  notation.

VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.332±0.006 OUR AVERAGE</b>				Includes data from the 2 datablocks that follow this one.

NODE=S013245

NODE=S013310

NODE=S013310

NODE=S013AL

NODE=S013AL

NODE=S013AL

**$A_L(\mu) = [\Gamma(\pi^- \mu^+ \nu_\mu) - \Gamma(\pi^+ \mu^- \bar{\nu}_\mu)]/\text{SUM}$** 

Only the combined value below is put into the Meson Summary Table.

VALUE (%)	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

NODE=S013A1

NODE=S013A1

NODE=S013A1

**0.304±0.025 OUR AVERAGE**

0.313±0.029	15M	GEWENIGER	74	ASPK
0.278±0.051	7.7M	PICCIONI	72	ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.60 ±0.14	4.1M	MCCARTHY	73	CNTR
0.57 ±0.17	1M	<sup>1</sup> PACIOTTI	69	OSPK
0.403±0.134	1M	<sup>1</sup> DORFAN	67	OSPK

<sup>1</sup>PACIOTTI 69 is a reanalysis of DORFAN 67 and is corrected for  $\mu^+ \mu^-$  range difference in MCCARTHY 72.

NODE=S013A1;LINKAGE=D

 **$A_L(e) = [\Gamma(\pi^- e^+ \nu_e) - \Gamma(\pi^+ e^- \bar{\nu}_e)]/\text{SUM}$** 

Only the combined value below is put into the Meson Summary Table.

VALUE (%)	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

NODE=S013A2

NODE=S013A2

NODE=S013A2

**0.334 ±0.007 OUR AVERAGE**

0.3322±0.0058±0.0047	298M	ALAVI-HARATI02		
0.341 ±0.018	34M	GEWENIGER	74	ASPK
0.318 ±0.038	40M	FITCH	73	ASPK
0.346 ±0.033	10M	MARX	70	CNTR

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.36 ±0.18	600k	ASHFORD	72	ASPK
0.246 ±0.059	10M	<sup>1</sup> SAAL	69	CNTR
0.224 ±0.036	10M	<sup>1</sup> BENNETT	67	CNTR

<sup>1</sup>SAAL 69 is a reanalysis of BENNETT 67.

NODE=S013A2;LINKAGE=B

**PARAMETERS FOR  $K_L^0 \rightarrow 2\pi$  DECAY**

$$\eta_{+-} = A(K_L^0 \rightarrow \pi^+ \pi^-) / A(K_S^0 \rightarrow \pi^+ \pi^-)$$

$$\eta_{00} = A(K_L^0 \rightarrow \pi^0 \pi^0) / A(K_S^0 \rightarrow \pi^0 \pi^0)$$

NODE=S013315

NODE=S013315

The fitted values of  $|\eta_{+-}|$  and  $|\eta_{00}|$  given below are the results of a fit to  $|\eta_{+-}|$ ,  $|\eta_{00}|$ ,  $|\eta_{00}/\eta_{+-}|$ , and  $\text{Re}(\epsilon'/\epsilon)$ . Independent information on  $|\eta_{+-}|$  and  $|\eta_{00}|$  can be obtained from the fitted values of the  $K_L^0 \rightarrow \pi\pi$  and  $K_S^0 \rightarrow \pi\pi$  branching ratios and the  $K_L^0$  and  $K_S^0$  lifetimes. This information is included as data in the  $|\eta_{+-}|$  and  $|\eta_{00}|$  sections with a Document ID "BRFIT." See the note "CP violation in  $K_L$  decays" above for details.

 **$|\eta_{00}| = |A(K_L^0 \rightarrow 2\pi^0) / A(K_S^0 \rightarrow 2\pi^0)|$** 

VALUE (units $10^{-3}$ )	DOCUMENT ID	TECN	COMMENT
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**2.222±0.012 OUR FIT** Error includes scale factor of 1.7.  $[(2.220 \pm 0.011) \times 10^{-3}$  OUR 2025 FIT Scale factor = 1.8]

NODE=S013E00

NODE=S013E00

NEW

**2.243±0.014**

BRFIT 16

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.47 ±0.31 ±0.24		ANGELOPO...	98	CPLR
2.49 ±0.40	1	ADLER	96B	CPLR Sup. by ANGELOPOULOS 98
2.33 ±0.18		CHRISTENS...	79	ASPK
2.71 ±0.37	2	WOLFF	71	OSPK Cu reg., 4 $\gamma$ 's
2.95 ±0.63	2	CHOLLET	70	OSPK Cu reg., 4 $\gamma$ 's

<sup>1</sup>Error is statistical only.

NODE=S013E00;LINKAGE=X

<sup>2</sup>CHOLLET 70 gives  $|\eta_{00}| = (1.23 \pm 0.24) \times (\text{regeneration amplitude}, 2 \text{ GeV}/c \text{ Cu})/10000\text{mb}$ . WOLFF 71 gives  $|\eta_{00}| = (1.13 \pm 0.12) \times (\text{regeneration amplitude}, 2 \text{ GeV}/c \text{ Cu})/10000\text{mb}$ . We compute both  $|\eta_{00}|$  values for (regeneration amplitude, 2 GeV/c Cu) = 24 ± 2mb. This regeneration amplitude results from averaging over FAISSNER 69, extrapolated using optical-model calculations of Bohm et al., Physics Letters **27B** 594 (1968) and the data of BALATS 71. (From H. Faissner, private communication).

NODE=S013E00;LINKAGE=C

$$|\eta_{+-}| = |\mathbf{A}(K_L^0 \rightarrow \pi^+ \pi^-) / \mathbf{A}(K_S^0 \rightarrow \pi^+ \pi^-)|$$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>2.233 ± 0.012 OUR FIT</b>	Error includes scale factor of 1.7. [( $2.232 \pm 0.011$ ) $\times 10^{-3}$ OUR 2025 FIT Scale factor = 1.8]			
<b>2.226 ± 0.008 OUR AVERAGE</b>	$[(2.226 \pm 0.007) \times 10^{-3}$ OUR 2025 AVERAGE]			
<b>2.226 ± 0.008</b>	BRFIT	16		
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.223 ± 0.012		<sup>1</sup> LAI 07 NA48		
2.219 ± 0.013		<sup>2</sup> AMBROSINO 06F KLOE		
2.228 ± 0.010		<sup>3</sup> ALEXOPOU... 04 KTeV		
2.286 ± 0.023 ± 0.026	70M	<sup>4</sup> APOSTOLA... 99C CPLR $K^0 - \bar{K}^0$ asymmetry		
2.310 ± 0.043 ± 0.031		<sup>5</sup> ADLER 95B CPLR $K^0 - \bar{K}^0$ asymmetry		
2.32 ± 0.14 ± 0.03	$10^5$	ADLER 92B CPLR $K^0 - \bar{K}^0$ asymmetry		
2.30 ± 0.035		GEWENIGER 74B ASPK		

<sup>1</sup> Value obtained from the NA48 measurements of  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma(K_L^0 \rightarrow \pi e \nu_e)$  and  $\tau_{K_S^0}$  and KLOE measurements of  $B(K_S^0 \rightarrow \pi^+ \pi^-)$  and  $\tau_{K_L^0}$ .  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)$

is defined to include the inner bremsstrahlung component  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^- \gamma)$  (IB)) but exclude the direct emission component  $B(K_S^0 \rightarrow \pi^+ \pi^-)$  (DE)). Their  $|\eta_{+-}|$  value is not directly used in our fit, but enters the fit via their branching ratio and lifetime measurements.

<sup>2</sup> AMBROSINO 06F uses KLOE branching ratios and  $\tau_L$  together with  $\tau_S$  from PDG 04. Their  $|\eta_{+-}|$  value is not directly used in our fit, but enters the fit via their branching ratio and lifetime measurements.

<sup>3</sup> ALEXOPOULOS 04  $|\eta_{+-}|$  uses their  $K_L^0 \rightarrow \pi\pi$  branching fractions,  $\tau_S = (0.8963 \pm 0.0005) \times 10^{-10}$  s from the average of KTeV and NA48  $\tau_S$  measurements, and assumes that  $\Gamma(K_S^0 \rightarrow \pi\ell\nu_\ell) = \Gamma(K_L^0 \rightarrow \pi\ell\nu_\ell)$  giving  $B(K_S^0 \rightarrow \pi\ell\nu_\ell) = 0.118\%$ . Their  $|\eta_{+-}|$  is not directly used in our fit, but enters our fit via their branching ratio measurements.

<sup>4</sup> APOSTOLAKIS 99C report ( $2.264 \pm 0.023 \pm 0.026 + 9.1[\tau_s - 0.8934]$ )  $\times 10^{-3}$ . We evaluate for our 2006 best value  $\tau_s = (0.8958 \pm 0.0005) \times 10^{-10}$  s.

<sup>5</sup> ADLER 95B report ( $2.312 \pm 0.043 \pm 0.030 - 1[\Delta m - 0.5274] + 9.1[\tau_s - 0.8926]$ )  $\times 10^{-3}$ . We evaluate for our 1996 best values  $\Delta m = (0.5304 \pm 0.0014) \times 10^{-10} \text{ fs}^{-1}$  and  $\tau_s = (0.8927 \pm 0.0009) \times 10^{-10}$  s. Superseded by APOSTOLAKIS 99C.

$$|\epsilon| = (2|\eta_{+-}| + |\eta_{00}|)/3$$

This expression is a very good approximation, good to about one part in  $10^{-4}$  because of the small measured value of  $\phi_{00} - \phi_{+-}$  and small theoretical ambiguities.

VALUE (units $10^{-3}$ )	DOCUMENT ID
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<b>2.229 ± 0.012 OUR FIT</b>	Error includes scale factor of 1.7. [ $(2.228 \pm 0.011) \times 10^{-3}$ OUR 2025 FIT Scale factor = 1.8]
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$$|\eta_{00}/\eta_{+-}|$$

VALUE	EVTS	DOCUMENT ID	TECN
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<b>0.9950 ± 0.0007 OUR FIT</b>	Error includes scale factor of 1.6.
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<b>0.9930 ± 0.0020 OUR AVERAGE</b>
------------------------------------

0.9931 ± 0.0020		<sup>1,2</sup> BARR 93D NA31
0.9904 ± 0.0084 ± 0.0036		<sup>3</sup> WOODS 88 E731
• • • We do not use the following data for averages, fits, limits, etc. • • •		
0.9939 ± 0.0013 ± 0.0015	1M	<sup>1</sup> BARR 93D NA31
0.9899 ± 0.0020 ± 0.0025		<sup>1</sup> BURKHARDT 88 NA31

<sup>1</sup> This is the square root of the ratio  $R$  given by BURKHARDT 88 and BARR 93D.

<sup>2</sup> This is the combined results from BARR 93D and BURKHARDT 88, taking into account a common systematic uncertainty of 0.0014.

<sup>3</sup> We calculate  $|\eta_{00}/\eta_{+-}| = 1 - 3(\epsilon'/\epsilon)$  from WOODS 88 ( $\epsilon'/\epsilon$ ) value.

$$\text{Re}(\epsilon'/\epsilon) = (1 - |\eta_{00}/\eta_{+-}|)/3$$

We have neglected terms of order  $\omega \cdot \text{Re}(\epsilon'/\epsilon)$ , where  $\omega = \text{Re}(A_2)/\text{Re}(A_0) \simeq 1/22$ . If included, this correction would lower  $\text{Re}(\epsilon'/\epsilon)$  by about  $0.04 \times 10^{-3}$ . See SOZZI 04.

VALUE (units $10^{-3}$ )	DOCUMENT ID	TECN	COMMENT
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<b>1.67 ± 0.23 OUR FIT</b>	Error includes scale factor of 1.6. [( $1.66 \pm 0.23$ ) $\times 10^{-3}$ OUR 2025 FIT Scale factor = 1.6]
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<b>1.68 ± 0.20 OUR AVERAGE</b>	Error includes scale factor of 1.4. See the ideogram below.
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<sup>1</sup> ABOUZAID 11 KTeV Assuming CPT

<sup>2</sup> BATLEY 02 NA48

<sup>3</sup> GIBBONS 93B E731

• • • We use the following data for averages but not for fits. • • •

<sup>2,3</sup> BARR 93D NA31

NODE=S013E+-

NODE=S013E+-

NEW

NEW

NODE=S013E+-;LINKAGE=LA

NODE=S013E+-;LINKAGE=AM

NODE=S013E+-;LINKAGE=AL

NODE=S013E+-;LINKAGE=VA

NODE=S013E+-;LINKAGE=D

NODE=S013EP

NODE=S013EP

NODE=S013EP

NEW

NODE=S013ER

NODE=S013ER

OCCUR=2

NODE=S013ER;LINKAGE=A

NODE=S013ER;LINKAGE=E

NODE=S013ER;LINKAGE=B

NODE=S013EPS

NODE=S013EPS

NODE=S013EPS

NEW

OCCUR=2

OCCUR=2;NOTFITTED

• • • We do not use the following data for averages, fits, limits, etc. • • •

$2.110 \pm 0.343$	<sup>1,4</sup> ABOUZAID	11	KTEV	Not assuming <i>CPT</i>
$2.07 \pm 0.28$	ALAVI-HARATI03	KTEV	In ABOUZAID 11	
$1.53 \pm 0.26$	LAI	01C	NA48	Incl. in BATLEY 02
$2.80 \pm 0.30 \pm 0.28$	ALAVI-HARATI99D	KTEV	In ALAVI-HARATI 03	
$1.85 \pm 0.45 \pm 0.58$	FANTI	99C	NA48	In LAI 01C
$2.0 \pm 0.7$	<sup>5</sup> BARR	93D	NA31	
$-0.4 \pm 1.4 \pm 0.6$	PATTERSON	90	E731	in GIBBONS 93B
$3.3 \pm 1.1$	<sup>5</sup> BURKHARDT	88	NA31	
$3.2 \pm 2.8 \pm 1.2$	<sup>2</sup> WOODS	88	E731	

1 The two ABOUZAID 11 values use the same data. The fits are performed with and without *CPT* invariance requirement.

2 These values are derived from  $|\eta_{00}/\eta_{+-}|$  measurements. They enter the average in this section but enter the fit via the  $|\eta_{00}/\eta_{+-}|$  only.

3 This is the combined results from BARR 93D and BURKHARDT 88, taking into account their common systematic uncertainty.

4 We use ABOUZAID 11  $\text{Re}(\epsilon'/\epsilon)$  value with *CPT* assumption in our fits for  $|\eta_{+-}|$ ,  $|\eta_{00}|$ , and  $\text{Re}(\epsilon'/\epsilon)$ .

5 These values are derived from  $|\eta_{00}/\eta_{+-}|$  measurements.

TYPE=noCPT

OCCUR=2

NOTFITTED

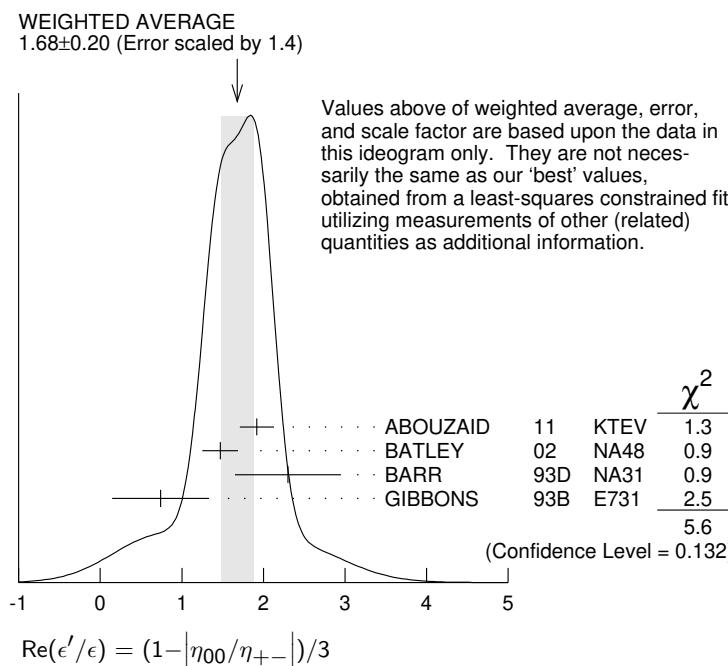
NODE=S013EPS;LINKAGE=AB

NODE=S013EPS;LINKAGE=A

NODE=S013EPS;LINKAGE=E

NODE=S013EPS;LINKAGE=AU

NODE=S013EPS;LINKAGE=AO



### $\phi_{+-}$ , PHASE of $\eta_{+-}$

The dependence of the phase on  $\Delta m$  and  $\tau_S$  is given for each experiment in the comments below, where  $\Delta m$  is the  $K_L^0 - K_S^0$  mass difference in units  $10^{10} \text{ s}^{-1}$  and  $\tau_S$  is the  $K_S$  mean life in units  $10^{-10} \text{ s}$ . We also give the regeneration phase  $\phi_f$  in the comments below.

OUR FIT is described in the note on "CP violation in  $K_L$  decays" in the  $K_L^0$  Particle Listings. Most experiments in this section are included in both the "Not Assuming *CPT*" and "Assuming *CPT*" fits. In the latter fit, they have little direct influence on  $\phi_{+-}$  because their errors are large compared to that assuming *CPT*, but they influence  $\Delta m$  and  $\tau_S$  through their dependencies on these parameters, which are given in the footnotes.

VALUE (°)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>43.51 ± 0.05 OUR FIT</b>				Error includes scale factor of 1.2. Assuming <i>CPT</i>
<b>43.4 ± 0.5 OUR FIT</b>				Error includes scale factor of 1.2. Not assuming <i>CPT</i>
$42.9 \pm 0.6 \pm 0.3$	70M	<sup>1</sup> APOSTOLA...	99C	CPLR $K^0 - \bar{K}^0$ asymmetry
$42.9 \pm 0.8 \pm 0.2$		<sup>2,3</sup> SCHWINGEN...	95	E773 CH <sub>1.1</sub> regenerator
$41.4 \pm 0.9 \pm 0.2$		<sup>3,4</sup> GIBBONS	93	E731 B <sub>4</sub> C regenerator
$44.5 \pm 1.6 \pm 0.5$		<sup>5</sup> CAROSI	90	NA31 Vacuum regen.
$43.3 \pm 1.0 \pm 0.5$		<sup>6</sup> GEWENIGER	74B	ASPK Vacuum regen.

NODE=S013F+-

NODE=S013F+-

NODE=S013F+-

• • • We do not use the following data for averages, fits, limits, etc. • • •

43.76 $\pm$ 0.64	7	ABOUZAID	11	KTEV	Not assuming CPT
44.12 $\pm$ 0.72 $\pm$ 1.20	8	ALAVI-HARATI03	11	KTEV	Not assuming CPT
42.5 $\pm$ 0.4 $\pm$ 0.3	9,10	ADLER	96C	RVUE	
43.4 $\pm$ 1.1 $\pm$ 0.3	11	ADLER	95B	CPLR	$K^0 - \bar{K}^0$ asymmetry
42.3 $\pm$ 4.4 $\pm$ 1.4	100k	12	ADLER	92B	CPLR $K^0 - \bar{K}^0$ asymmetry
47.7 $\pm$ 2.0 $\pm$ 0.9	3,13	KARLSSON	90	E731	
44.3 $\pm$ 2.8 $\pm$ 0.2	14	CARITHERS	75	SPEC	C regenerator

<sup>1</sup> APOSTOLAKIS 99C measures  $\phi_{+-} = (43.19 \pm 0.53 \pm 0.28) + 300 [\Delta m - 0.5301] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>2</sup> SCHWINGENHEUER 95 measures  $\phi_{+-} = (43.53 \pm 0.76) + 173 [\Delta m - 0.5282] - 275 [\tau_s - 0.8926] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>3</sup> These experiments measure  $\phi_{+-} - \phi_f$  and calculate the regeneration phase from the power law momentum dependence of the regeneration amplitude using analyticity and dispersion relations. SCHWINGENHEUER 95 [GIBBONS 93] includes a systematic error of  $0.35^\circ$  [ $0.5^\circ$ ] for uncertainties in their modeling of the regeneration amplitude.

<sup>4</sup> GIBBONS 93 measures  $\phi_{+-} = (42.21 \pm 0.9) + 189 [\Delta m - 0.5257] - 460 [\tau_s - 0.8922] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values. This is actually reported in SCHWINGENHEUER 95, footnote 8. GIBBONS 93 reports  $\phi_{+-} (42.2 \pm 1.4)^\circ$ . They measure  $\phi_{+-} - \phi_f$  and calculate the regeneration phase  $\phi_f$  from the power law momentum dependence of the regeneration amplitude using analyticity. An error of  $0.6^\circ$  is included for possible uncertainties in the regeneration phase.

<sup>5</sup> CAROSI 90 measures  $\phi_{+-} = (46.9 \pm 1.4 \pm 0.7) + 579 [\Delta m - 0.5351] + 303 [\tau_s - 0.8922] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>6</sup> GEWENIGER 74B measures  $\phi_{+-} = (49.4 \pm 1.0) + 565 [\Delta m - 0.540] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>7</sup> Not independent of other phase parameters reported in ABOUZAID 11.

<sup>8</sup> ALAVI-HARATI 03  $\phi_{+-}$  is correlated with their  $\Delta m = m_{K_L^0} - m_{K_S^0}$  and  $\tau_{K_S}$  measurements in the  $K_L^0$  and  $K_S^0$  sections respectively. The correlation coefficients are  $\rho(\phi_{+-}, \Delta m) = +0.955$ ,  $\rho(\phi_{+-}, \tau_S) = -0.871$ , and  $\rho(\tau_S, \Delta m) = -0.840$ . CPT is not assumed. Uses scintillator Pb regenerator. Superseded by ABOUZAID 11.

<sup>9</sup> ADLER 96C measures  $\phi_{+-} = (43.82 \pm 0.41) + 339 [\Delta m - 0.5307] - 252 [\tau_s - 0.8922] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>10</sup> ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value in the 1996 edition of this Review (Physical Review **D54** 1 (1996)).

<sup>11</sup> ADLER 95B measures  $\phi_{+-} = (42.7 \pm 0.9 \pm 0.6) + 316 [\Delta m - 0.5274] + 30 [\tau_s - 0.8926] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>12</sup> ADLER 92B quote separately two systematic errors:  $\pm 0.4$  from their experiment and  $\pm 1.0$  degrees due to the uncertainty in the value of  $\Delta m$ .

<sup>13</sup> KARLSSON 90 systematic error does not include regeneration phase uncertainty.

<sup>14</sup> CARITHERS 75 measures  $\phi_{+-} = (45.5 \pm 2.8) + 224 [\Delta m - 0.5348] (\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ } \hbar \text{ s}^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.  $\phi_f = -40.9 \pm 2.6^\circ$ .

TYPE=noCPT

TYPE=noCPT

NODE=S013F+-;LINKAGE=FG

NODE=S013F+-;LINKAGE=S1

NODE=S013F+-;LINKAGE=S2

NODE=S013F+-;LINKAGE=GF

NODE=S013F+-;LINKAGE=I

NODE=S013F+-;LINKAGE=G

NODE=S013F+-;LINKAGE=AB

NODE=S013F+-;LINKAGE=KF

NODE=S013F+-;LINKAGE=R

NODE=S013F+-;LINKAGE=Y1

NODE=S013F+-;LINKAGE=DD

NODE=S013F+-;LINKAGE=M

NODE=S013F+-;LINKAGE=Q

NODE=S013F+-;LINKAGE=H

## $\phi_{00}$ , PHASE OF $\eta_{00}$

See comment in  $\phi_{+-}$  header above for treatment of  $\Delta m$  and  $\tau_s$  dependence, as well as for the inclusion of data in both the "Assuming CPT" and "Not Assuming CPT" fits.

OUR FIT is described in the note on "CP violation in  $K_L$  decays" in the  $K_L^0$  Particle Listings.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
<b>43.52 ± 0.05 OUR FIT</b>			Error includes scale factor of 1.2. Assuming CPT
<b>43.7 ± 0.6 OUR FIT</b>			Error includes scale factor of 1.2. Not assuming CPT
44.5 ± 2.3 ± 0.5	<sup>1</sup> CAROSI	90	NA31
• • • We do not use the following data for averages, fits, limits, etc. • • •			
44.06 ± 0.68	<sup>2</sup> ABOUZAID	11	KTEV Not assuming CPT
41.7 ± 5.9 ± 0.2	<sup>3</sup> ANGELOPO...	98	CPLR
50.8 ± 7.1 ± 1.7	<sup>4</sup> ADLER	96B	CPLR Sup. by ANGELOPOULOS 98
47.4 ± 1.4 ± 0.9	<sup>5</sup> KARLSSON	90	E731

<sup>1</sup> CAROSI 90 measures  $\phi_{00} = (47.1 \pm 2.1 \pm 1.0) + 579 [\Delta m - 0.5351] + 252 [\tau_s - 0.8922]$  (°). We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ h s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>2</sup> Not independent of other phase parameters reported in ABOUZAID 11.

<sup>3</sup> ANGELOPOULOS 98 measures  $\phi_{00} = (42.0 \pm 5.6 \pm 1.9) + 240 [\Delta m - 0.5307]$  (°). We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ h s}^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values. The  $\tau_s$  dependence is negligible.

<sup>4</sup> ADLER 96B identified initial neutral kaon individually as being a  $K^0$  or a  $\bar{K}^0$ . The systematic uncertainty is  $\pm 1.5^\circ$  combined in quadrature with  $\pm 0.8^\circ$  due to  $\Delta m$ .

<sup>5</sup> KARLSSON 90 systematic error does not include regeneration phase uncertainty.

## $\phi_\epsilon = (2\phi_{+-} + \phi_{00})/3$

This expression is a very good approximation, good to about  $10^{-3}$  degrees because of the small measured values of  $\phi_{00} - \phi_{+-}$  and  $\text{Re } \epsilon'/\epsilon$ , and small theoretical ambiguities.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
<b>43.52 ± 0.04 OUR FIT</b>			Error includes scale factor of 1.2. Assuming CPT
<b>43.5 ± 0.5 OUR FIT</b>			Error includes scale factor of 1.3. Not assuming CPT
43.5164 ± 0.0002 ± 0.0509	<sup>1</sup> SUPERWEAK	16	Assuming CPT
43.86 ± 0.63	<sup>2</sup> ABOUZAID	11	KTEV Not assuming CPT

<sup>1</sup> SUPERWEAK 16 is a fake measurement used to impose the CPT or Superweak constraint  $\phi_{+-} = \phi_{SW} = \tan^{-1}[2 \frac{\Delta m}{\hbar} (\frac{\tau_S \tau_L}{\tau_L - \tau_S})]$ . This "measurement" is linearized using values near the PDG 04 edition values of  $\Delta m$ ,  $\tau_S$  and  $\tau_L$ , and then adjusted to our current values as described in the following "measurement". SUPERWEAK 16 measures  $\phi_\epsilon = (43.50258 \pm 0.00021) + 54.1 [\Delta m - 0.5289] + 32.0 [\tau_s - 0.89564]$  (°). We have adjusted the measurement to use our best values of ( $\Delta m = 0.5293 \pm 0.0009$ ) ( $10^{10} \text{ h s}^{-1}$ ), ( $\tau_s = 0.8954 \pm 0.0004$ ) ( $10^{-10} \text{ s}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>2</sup> ABOUZAID 11 uses the full KTeV dataset collected in 1996, 1997, and 1999. See  $\text{Im}(\epsilon'/\epsilon)$  section for correlation information.

## $\text{Im}(\epsilon'/\epsilon) = -(\phi_{00} - \phi_{+-})/3$

For small  $|\epsilon'/\epsilon|$ ,  $\text{Im}(\epsilon'/\epsilon)$  is related to the phases of  $\eta_{00}$  and  $\eta_{+-}$  by the above expression.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
<b>-0.002 ± 0.005 OUR FIT</b>			Error includes scale factor of 1.7. Assuming CPT
<b>-0.11 ± 0.11 OUR FIT</b>			Not assuming CPT
<b>-0.0985 ± 0.1157</b>	<sup>1</sup> ABOUZAID	11	KTEV Not assuming CPT

<sup>1</sup> ABOUZAID 11 uses the full KTeV dataset collected in 1996, 1997, and 1999. The fit has  $\Delta m$ ,  $\tau_s$ ,  $\phi_\epsilon$ ,  $\text{Re}(\epsilon'/\epsilon)$ , and  $\text{Im}(\epsilon'/\epsilon)$  as free parameters. The reported value of  $\text{Im}(\epsilon'/\epsilon) = (-17.20 \pm 20.20) \times 10^{-4}$  rad. The correlation coefficients are  $\rho(\phi_\epsilon, \Delta m) = 0.828$ ,  $\rho(\phi_\epsilon, \tau_s) = -0.765$ ,  $\rho(\Delta m, \tau_s) = -0.858$ ,  $\rho(\text{Im}(\epsilon'/\epsilon), \phi_\epsilon) = -0.041$ ,  $\rho(\text{Im}(\epsilon'/\epsilon), \Delta m) = 0.026$ ,  $\rho(\text{Im}(\epsilon'/\epsilon), \tau_s) = -0.010$ .

NODE=S013FOO

NODE=S013FOO

NODE=S013FOO

TYPE=noCPT

NODE=S013FOO;LINKAGE=I

NODE=S013FOO;LINKAGE=AB

NODE=S013FOO;LINKAGE=K1

NODE=S013FOO;LINKAGE=A

NODE=S013FOO;LINKAGE=Q

NODE=S013EPH

NODE=S013EPH

NODE=S013EPH

TYPE=CPT

TYPE=noCPT

NODE=S013EPH;LINKAGE=SW

NODE=S013EPH;LINKAGE=AB

NODE=S013EPI

NODE=S013EPI

NODE=S013EPI

TYPE=noCPT

NODE=S013EPI;LINKAGE=AB

**DECAY-PLANE ASYMMETRY IN  $\pi^+\pi^-e^+e^-$  DECAYS**

This is the  $CP$ -violating asymmetry

$$A = \frac{N_{\sin\phi\cos\phi>0.0} - N_{\sin\phi\cos\phi<0.0}}{N_{\sin\phi\cos\phi>0.0} + N_{\sin\phi\cos\phi<0.0}}$$

where  $\phi$  is the angle between the  $e^+e^-$  and  $\pi^+\pi^-$  planes in the  $K_L^0$  rest frame.

 **$CP$  ASYMMETRY  $A$  in  $K_L^0 \rightarrow \pi^+\pi^-e^+e^-$** 

VALUE (%)	DOCUMENT ID	TECN
<b>13.7±1.5 OUR AVERAGE</b>		
13.6±1.4±1.5	ABOUZAID 06	KTEV
14.2±3.0±1.9	LAI 03C	NA48
13.6±2.5±1.2	ALAVI-HARATI00B	KTEV

NODE=S013303

NODE=S013303

**PARAMETERS FOR  $e^+e^-e^+e^-$  DECAYS**

These are the  $CP$ -violating parameters in the  $\phi$  distribution, where  $\phi$  is the angle between the planes of the two  $e^+e^-$  pairs in the kaon rest frame:

$$d\Gamma/d\phi \propto 1 + \beta_{CP} \cos(2\phi) + \gamma_{CP} \sin(2\phi)$$

where  $\beta_{CP} = -0.20$  and  $\gamma_{CP} = 0$  values correspond to no  $CP$  violation.

 **$\beta_{CP}$  from  $K_L^0 \rightarrow e^+e^-e^+e^-$** 

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.19±0.07 OUR AVERAGE</b>				
-0.13±0.10±0.03	200	<sup>1</sup> LAI 05B	NA48	
-0.23±0.09±0.02	441	ALAVI-HARATI01D	KTEV	$M_{ee} > 8 \text{ MeV}/c^2$

NODE=S013BCP

NODE=S013BCP

<sup>1</sup> LAI 05B obtains  $\beta_{CP} = -0.13 \pm 0.10$  (stat) if  $\gamma_{CP} = 0$  is assumed.

 **$\gamma_{CP}$  from  $K_L^0 \rightarrow e^+e^-e^+e^-$** 

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.01±0.11 OUR AVERAGE</b>				
-0.13±0.10±0.03	200	LAI 05B	NA48	Error includes scale factor of 1.6.
-0.09±0.09±0.02	441	ALAVI-HARATI01D	KTEV	$M_{ee} > 8 \text{ MeV}/c^2$

NODE=S013BCP;LINKAGE=LA

NODE=S013GCP

NODE=S013GCP

**CHARGE ASYMMETRY IN  $\pi^+\pi^-\pi^0$  DECAYS**

These are  $CP$ -violating charge-asymmetry parameters, defined at beginning of section "LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+\pi^-\pi^0$  above.

See also note on Dalitz plot parameters in  $K^\pm$  section and note on " $CP$  violation in  $K_L$  decays" above.

**LINEAR COEFFICIENT  $j$  FOR  $K_L^0 \rightarrow \pi^+\pi^-\pi^0$** 

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.0012±0.0008 OUR AVERAGE</b>			
0.0010±0.0024±0.0030	500k	ANGELOPO... 98C	CPLR
-0.001 ± 0.011	6499	CHO 77	
0.001 ± 0.003	4709	PEACH 77	
0.0013±0.0009	3M	SCRIBANO 70	
0.0 ± 0.017	4400	SMITH 70	OSPK
0.001 ± 0.004	238k	BLANPIED 68	

NODE=S013JT0

NODE=S013JT0

**QUADRATIC COEFFICIENT  $f$  FOR  $K_L^0 \rightarrow \pi^+\pi^-\pi^0$** 

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.0045±0.0024±0.0059</b>	500k	ANGELOPO... 98C	CPLR

NODE=S013FT0

NODE=S013FT0

**PARAMETERS for  $K_L^0 \rightarrow \pi^+\pi^-\gamma$  DECAY**

$$|\eta_{+-\gamma}| = |A(K_L^0 \rightarrow \pi^+\pi^-\gamma, CP \text{ violating})/A(K_S^0 \rightarrow \pi^+\pi^-\gamma)|$$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN
<b>2.35 ± 0.07 OUR AVERAGE</b>			
2.359±0.062±0.040	9045	MATTHEWS 95	E773
2.15 ± 0.26 ± 0.20	3671	RAMBERG 93B	E731

NODE=S013307

NODE=S013E+G

NODE=S013E+G

**$\phi_{+-\gamma}$  = phase of  $\eta_{+-\gamma}$** 

VALUE (°)	EVTS	DOCUMENT ID	TECN
<b>44 ± 4 OUR AVERAGE</b>			
43.8 ± 3.5 ± 1.9	9045	MATTHEWS 95	E773
72 ± 23 ± 17	3671	RAMBERG 93B	E731

NODE=S013P+G  
NODE=S013P+G **$|\epsilon'_{+-\gamma}|/\epsilon$  for  $K_L^0 \rightarrow \pi^+\pi^-\gamma$** 

VALUE	CL%	EVTS	DOCUMENT ID	TECN
<0.3	90	3671	1 RAMBERG 93B	E731

<sup>1</sup> RAMBERG 93B limit on  $|\epsilon'_{+-\gamma}|/\epsilon$  assumes than any difference between  $\eta_{+-}$  and  $\eta_{+-\gamma}$  is due to direct  $CP$  violation.

NODE=S013EPG  
NODE=S013EPG **$|g_{E1}|$  for  $K_L^0 \rightarrow \pi^+\pi^-\gamma$** 

This parameter is the amplitude of the direct emission of a  $CP$  violating E1 electric dipole photon.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<0.21	90	111k	ABOUZAID 06A	KTEV	$E_\gamma^*$ > 20 MeV

NODE=S013GE1  
NODE=S013GE1

NODE=S013GE1

**T VIOLATION TESTS IN  $K_L^0$  DECAYS** **$\text{Im}(\xi)$  in  $K_{\mu 3}^0$  DECAY (from transverse  $\mu$  pol.)**

Test of T reversal invariance.	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.007±0.026 OUR AVERAGE</b>				

0.009±0.030	12M	MORSE	80	CNTR	Polarization
0.35 ± 0.30	207k	1 CLARK	77	SPEC	POL, $t=0$
-0.085±0.064	2.2M	2 SANDWEISS	73	CNTR	POL, $t=0$
-0.02 ± 0.08		LONGO	69	CNTR	POL, $t=3.3$
-0.2 ± 0.6		ABRAMS	68B	OSPK	Polarization

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.012±0.026 SCHMIDT 79 CNTR Repl. by MORSE 80

1 CLARK 77 value has additional  $\xi(0)$  dependence +0.21Re[ $\xi(0)$ ].

2 SANDWEISS 73 value corrected from value quoted in their paper due to new value of  $\text{Re}(\xi)$ . See footnote 4 of SCHMIDT 79.

NODE=S013280

NODE=S013IXI  
NODE=S013IXI  
NODE=S013IXI

OCCUR=2

NODE=S013IXI;LINKAGE=C  
NODE=S013IXI;LINKAGE=S**CPT-INVARIANCE TESTS IN  $K_L^0$  DECAYS****PHASE DIFFERENCE  $\phi_{00} - \phi_{+-}$** 

Test of CPT.

OUR FIT is described in the note on "CP violation in  $K_L$  decays" in the  $K_L^0$  Particle Listings.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
<b>0.006±0.014 OUR FIT</b>	Error includes scale factor of 1.7. Assuming CPT		
<b>0.34 ± 0.32 OUR FIT</b>	Not assuming CPT		
<b>• • • We do not use the following data for averages, fits, limits, etc. • • •</b>			
0.006±0.008	1 SUPERWEAK 16		Assuming CPT
-0.30 ± 0.88	2 SCHWINGEN...95		Combined E731, E773
0.30 ± 0.35	3 ABOUZAID 11	KTEV	Not assuming CPT
0.39 ± 0.22 ± 0.45	4 ALAVI-HARATI03	KTEV	
0.62 ± 0.71 ± 0.75	SCHWINGEN...95	E773	
-1.6 ± 1.2	5 GIBBONS 93	E731	
0.2 ± 2.6 ± 1.2	6 CAROSI 90	NA31	
-0.3 ± 2.4 ± 1.2	KARLSSON 90	E731	

NODE=S013246

NODE=S013DF  
NODE=S013DF

NODE=S013DF

TYPE=CPT  
OCCUR=2

TYPE=noCPT

NOTFITTED

NODE=S013DF;LINKAGE=SW

NODE=S013DF;LINKAGE=A

NODE=S013DF;LINKAGE=AB

NODE=S013DF;LINKAGE=AP

NODE=S013DF;LINKAGE=GB

NODE=S013DF;LINKAGE=CC

<sup>1</sup> SUPERWEAK 16 is a fake experiment to constrain  $\phi_{00} - \phi_{+-}$  to a small value as described in the note "CP violation in  $K_L$  decays."

<sup>2</sup> This SCHWINGENHEUER 95 values is the combined result of SCHWINGENHEUER 95 and GIBBONS 93, accounting for correlated systematic errors.

<sup>3</sup> Not independent of other phase parameters reported in ABOUZAID 11.

<sup>4</sup> ALAVI-HARATI 03 fit  $\text{Re}(\epsilon'/\epsilon)$ ,  $\text{Im}(\epsilon'/\epsilon)$ ,  $\Delta m$ ,  $\tau_S$ , and  $\phi_{+-}$  simultaneously, not assuming CPT. Phase difference is obtained from  $\phi_{00} - \phi_{+-} \approx -3\text{Im}(\epsilon'/\epsilon)$  for small  $|\epsilon'/\epsilon|$ . Superseded by ABOUZAID 11.

<sup>5</sup> GIBBONS 93 give detailed dependence of systematic error on lifetime (see the section on the  $K_S^0$  mean life) and mass difference (see the section on  $m_{K_L^0} - m_{K_S^0}$ ).

<sup>6</sup> CAROSI 90 is excluded from the fit because it is not independent of  $\phi_{+-}$  and  $\phi_{00}$  values.

## PHASE DIFFERENCE $\phi_{+-} = \phi_{SW}$

Test of *CPT*. The Superweak phase  $\phi_{SW} \equiv \tan^{-1}(2\Delta m/\Delta\Gamma)$  where  $\Delta m = m_{K_L^0} - m_{K_S^0}$  and  $\Delta\Gamma = \hbar(\tau_L - \tau_S)/(\tau_L \tau_S)$ .

VALUE (°)	DOCUMENT ID	TECN
<b>0.61±0.62±1.01</b>	<sup>1</sup> ALAVI-HARATI03	KTEV

<sup>1</sup> ALAVI-HARATI 03 fit is the same as their  $\phi_{+-}$ ,  $\tau_{K_S}$ ,  $\Delta m$  fit, except that the parameter  $\phi_{+-} - \phi_{SW}$  is used in place of  $\phi$ .

$$\text{Re}\left(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}\right) - \frac{A_L}{2}$$

Test of *CPT*

VALUE (units $10^{-6}$ )	DOCUMENT ID	TECN	COMMENT
<b>-3±35</b>	<sup>1</sup> ALAVI-HARATI02	E799	Uses $A_L$ from $K_{e3}$ decays

<sup>1</sup> ALAVI-HARATI 02 uses PDG 00 values of  $\eta_{+-}$  and  $\eta_{00}$ .

## $\Delta S = \Delta Q$ IN $K^0$ DECAYS

The relative amount of  $\Delta S \neq \Delta Q$  component present is measured by the parameter  $x$ , defined as

$$x = A(\bar{K}^0 \rightarrow \pi^- \ell^+ \nu) / A(K^0 \rightarrow \pi^- \ell^+ \nu).$$

We list  $\text{Re}\{x\}$  and  $\text{Im}\{x\}$  for  $K_{e3}$  and  $K_{\mu 3}$  combined.

$$x = A(\bar{K}^0 \rightarrow \pi^- \ell^+ \nu) / A(K^0 \rightarrow \pi^- \ell^+ \nu) = A(\Delta S = -\Delta Q) / A(\Delta S = \Delta Q)$$

### REAL PART OF $x$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.0018±0.0041±0.0045</b>		ANGELOPO...	98D CPLR	$K_{e3}$ from $K^0$
• • • We do not use the following data for averages, fits, limits, etc.				• • •
0.10 $\pm 0.18$	79	SMITH	75B WIRE	$\pi^- p \rightarrow K^0 \Lambda$
0.04 $\pm 0.03$	4724	NIEBERGALL	74 ASPK	$K^+ p \rightarrow K^0 p \pi^+$
-0.008 $\pm 0.044$	1757	FACKLER	73 OSPK	$K_{e3}$ from $K^0$
-0.03 $\pm 0.07$	1367	HART	73 OSPK	$K_{e3}$ from $K^0 \Lambda$
-0.070 $\pm 0.036$	1079	MALLARY	73 OSPK	$K_{e3}$ from $K^0 \Lambda X$
0.03 $\pm 0.06$	410	<sup>1</sup> BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.04 $\pm 0.10$	100	<sup>2</sup> GRAHAM	72 OSPK	$K_{\mu 3}$ from $K^0 \Lambda$
-0.05 $\pm 0.09$	442	<sup>2</sup> GRAHAM	72 OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.26 $\pm 0.14$	126	MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.13 $\pm 0.11$	342	<sup>2</sup> MANTSCH	72 OSPK	$K_{e3}$ from $K^0 \Lambda$
0.04 $\pm 0.07$	222	<sup>1</sup> BURGUN	71 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.25 $\pm 0.07$	252	WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
0.12 $\pm 0.09$	215	<sup>3</sup> CHO	70 DBC	$K^+ d \rightarrow K^0 pp$
-0.020 $\pm 0.025$		<sup>4</sup> BENNETT	69 CNTR	Charge asym+ Cu regen.
0.09 $\pm 0.14$	686	LITTENBERG	69 OSPK	$K^+ n \rightarrow K^0 p$
0.03 $\pm 0.03$		<sup>4</sup> BENNETT	68 CNTR	
0.09 $\pm 0.07$	121	JAMES	68 HBC	$\bar{p}p$
0.17 $\pm 0.16$	116	FELDMAN	67B OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.17 $\pm 0.10$	335	<sup>3</sup> HILL	67 DBC	$K^+ d \rightarrow K^0 pp$
0.035 $\pm 0.11$	196	AUBERT	65 HLBC	$K^+$ charge exch.
0.06 $\pm 0.18$	152	<sup>5</sup> BALDO...	65 HLBC	$K^+$ charge exch.
-0.08 $\pm 0.28$	109	<sup>6</sup> FRANZINI	65 HBC	$\bar{p}p$

<sup>1</sup> BURGUN 72 is a final result which includes BURGUN 71.

<sup>2</sup> First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.

<sup>3</sup> CHO 70 is analysis of unambiguous events in new data and HILL 67.

<sup>4</sup> BENNETT 69 is a reanalysis of BENNETT 68.

<sup>5</sup> BALDO-CEOLIN 65 gives  $x$  and  $\theta$  converted by us to  $\text{Re}(x)$  and  $\text{Im}(x)$ .

<sup>6</sup> FRANZINI 65 gives  $x$  and  $\theta$  for  $\text{Re}(x)$  and  $\text{Im}(x)$ . See SCHMIDT 67.

NODE=S013DFS

NODE=S013DFS

NODE=S013DFS

NODE=S013DFS;LINKAGE=A

NODE=S013CPT

NODE=S013CPT

NODE=S013CPT

NODE=S013CPT;LINKAGE=A

NODE=S013249

NODE=S013250

NODE=S013REX

NODE=S013REX

OCCUR=2

NODE=S013REX;LINKAGE=U

NODE=S013REX;LINKAGE=G

NODE=S013REX;LINKAGE=N

NODE=S013REX;LINKAGE=B

NODE=S013REX;LINKAGE=C

NODE=S013REX;LINKAGE=F

**IMAGINARY PART OF  $x$** Assumes  $m_{K_L^0} - m_{K_S^0}$  positive. See Listings above.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.0012±0.0019±0.0009</b>	640k	ANGELOPO...	01B	CPLR $K_{e3}$ from $K^0$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.0012±0.0019	640k	1 ANGELOPO...	98E	CPLR $K_{e3}$ from $K^0$
-0.10 +0.16 -0.19	79	SMITH	75B	WIRE $\pi^- p \rightarrow K^0 \Lambda$
-0.06 ±0.05	4724	NIEBERGALL	74	ASPK $K^+ p \rightarrow K^0 p \pi^+$
-0.017 ±0.060	1757	FACKLER	73	OSPK $K_{e3}$ from $K^0$
0.09 ±0.07	1367	HART	73	OSPK $K_{e3}$ from $K^0 \Lambda$
0.107 +0.092 -0.074	1079	MALLARY	73	OSPK $K_{e3}$ from $K^0 \Lambda X$
0.07 +0.06 -0.07	410	2 BURGUN	72	HBC $K^+ p \rightarrow K^0 p \pi^+$
0.12 +0.17 -0.16	100	3 GRAHAM	72	OSPK $K_{\mu 3}$ from $K^0 \Lambda$
0.05 ±0.13	442	3 GRAHAM	72	OSPK $\pi^- p \rightarrow K^0 \Lambda$
0.21 +0.15 -0.12	126	MANN	72	HBC $K^- p \rightarrow n \bar{K}^0$
-0.04 ±0.16	342	3 MANTSCH	72	OSPK $K_{e3}$ from $K^0 \Lambda$
0.12 +0.08 -0.09	222	2 BURGUN	71	HBC $K^+ p \rightarrow K^0 p \pi^+$
0.0 ±0.08	252	WEBBER	71	HBC $K^- p \rightarrow n \bar{K}^0$
-0.08 ±0.07	215	4 CHO	70	DBC $K^+ d \rightarrow K^0 pp$
-0.11 +0.10 -0.11	686	LITTENBERG	69	OSPK $K^+ n \rightarrow K^0 p$
+0.22 +0.37 -0.29	121	JAMES	68	HBC $\bar{p} p$
0.0 ±0.25	116	FELDMAN	67B	OSPK $\pi^- p \rightarrow K^0 \Lambda$
-0.20 ±0.10	335	4 HILL	67	DBC $K^+ d \rightarrow K^0 pp$
-0.21 +0.11 -0.15	196	AUBERT	65	HLBC $K^+$ charge exch.
-0.44 +0.32 -0.19	152	5 BALDO-...	65	HLBC $K^+$ charge exch.
+0.24 +0.40 -0.30	109	6 FRANZINI	65	HBC $\bar{p} p$

1 Superseded by ANGELOPOULOS 01B.

2 BURGUN 72 is a final result which includes BURGUN 71.

3 First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.

4 Footnote 10 of HILL 67 should read +0.58, not -0.58 (private communication) CHO 70 is analysis of unambiguous events in new data and HILL 67.

5 BALDO-CEOLIN 65 gives  $x$  and  $\theta$  converted by us to Re( $x$ ) and Im( $x$ ).6 FRANZINI 65 gives  $x$  and  $\theta$  for Re( $x$ ) and Im( $x$ ). See SCHMIDT 67.

NODE=S013IMX

NODE=S013IMX

NODE=S013IMX

OCCUR=2

NODE=S013IMX;LINKAGE=A

NODE=S013IMX;LINKAGE=U

NODE=S013IMX;LINKAGE=G

NODE=S013IMX;LINKAGE=N

NODE=S013IMX;LINKAGE=C

NODE=S013IMX;LINKAGE=F

 **$K_L^0$  REFERENCES**

AAIJ	23AE	PR D108 L031102	R. Aaij <i>et al.</i>	(LHCb Collab.)
AHN	21	PRL 126 121801	J.K. Ahn <i>et al.</i>	(KOTO Collab.)
SHIMIZU	20	PR D102 051103	N. Shimizu <i>et al.</i>	(KOTO Collab.)
AHN	19	PRL 122 021802	J.K. Ahn <i>et al.</i>	(KOTO Collab.)
AHN	17	PTEP 2017 021C01	J.K. Ahn <i>et al.</i>	(KOTO Collab.)
BRIT	16	RPP 2016 edition	C.-J. Lin	(PDG Collab.)
ETAFIT	16	RPP 2016 edition	C.-J. Lin	(PDG Collab.)
SUPERWEAK	16	RPP 2016 edition	C.-J. Lin	(PDG Collab.)
ABOUZAID	11	PR D83 092001	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	11A	PRL 107 201803	E. Abouzaid <i>et al.</i>	(KTeV Collab.)
OGATA	11	PR D84 052009	R. Ogata <i>et al.</i>	(KEK E391a Collab.)
TUNG	11	PR D83 031101	Y.C. Tung <i>et al.</i>	(KEK E391a Collab.)
ABOUZAID	10	PR D81 052001	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
AHN	10	PR D81 072004	J.K. Ahn <i>et al.</i>	(KEK E391a Collab.)
ABOUZAID	08	PR D77 112004	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	08A	PR D78 032009	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	08B	PR D78 032014	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	08C	PR L100 131803	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
AHN	08	PR L100 201802	J.K. Ahn <i>et al.</i>	(KEK E391a Collab.)
AMBROSINO	08F	EPJ C55 539	F. Ambrosino <i>et al.</i>	(KLOE Collab.)
ABOUZAID	07B	PRL 99 051804	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	07C	PRL 99 081803	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
ABOUZAID	07D	PR D76 052001	E. Abouzaid <i>et al.</i>	(FNAL KTeV Collab.)
AMBROSINO	07C	JHEP 0712 105	F. Ambrosino <i>et al.</i>	(KLOE Collab.)
ANDRE	07	ANP 322 2518	T. Andre	(E615 Collab.)
LAI	07	PL B645 26	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
LAI	07A	PL B647 341	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
NIX	07	PR D76 011101	J. Nix <i>et al.</i>	(KEK E391a Collab.)
ABOUZAID	06	PRL 96 101801	E. Abouzaid <i>et al.</i>	(KTeV Collab.)
ABOUZAID	06A	PR D74 032004	E. Abouzaid <i>et al.</i>	(KTeV Collab.)
Also		PR D74 039905 (errat.)	E. Abouzaid <i>et al.</i>	(KTeV Collab.)
ABOUZAID	06C	PR D74 097101	E. Abouzaid <i>et al.</i>	(KTeV Collab.)
AHN	06	PR D74 051105	J.K. Ahn <i>et al.</i>	(KEK E391a Collab.)
Also		PR D74 079901 (errat.)	J.K. Ahn <i>et al.</i>	(KEK E391a Collab.)

NODE=S013

REFID=62337

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REFID=51505

REFID=51339

REFID=51466

AMBROSINO	06	PL B632 43	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=51011
AMBROSINO	06D	PL B636 166	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=51072
AMBROSINO	06F	PL B638 140	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=51074
BATLEY	06B	PL B633 173	J.R. Batley <i>et al.</i>	(CERN NA48/2 Collab.)	REFID=51071
HILL	06	PR D74 096006	R.J. Hill	(FNAL)	REFID=51545
PDG	06	JP G33 1	W.-M. Yao <i>et al.</i>	(PDG Collab.)	REFID=51004
ALEXOPOU...	05	PR D71 012001	T. Alexopoulos <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50390
AMBROSINO	05C	PL B626 15	F. Ambrosino <i>et al.</i>	(KLOE Collab.)	REFID=50881
CABIBBO	05	JHEP 0503 021	N. Cabibbo, G. Isidori	(CERN, ROMAI, FRAS)	REFID=51070
LAI	05	PL B605 247	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=50384
LAI	05B	PL B615 31	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=50603
PARK	05	PRL 94 021801	H.K. Park <i>et al.</i>	(FNAL HyperCP Collab.)	REFID=50480
ALAVI-HARATI	04A	PRL 93 021805	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV/E799 Collab.)	REFID=50060
ALEXOPOU...	04	PR D70 092006	T. Alexopoulos <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50242
ALEXOPOU...	04A	PR D70 092007	T. Alexopoulos <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50243
BATLEY	04	PL B595 75	J.R. Batley <i>et al.</i>	(CERN NA48 Collab.)	REFID=49979
CIRIGLIANO	04	EPJ C35 53	V. Cirigliano, H. Neufeld, H. Pichl	(CIT, VALE+)	REFID=49972
LAI	04B	PL B602 41	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=50285
LAI	04C	PL B604 1	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=50289
PDG	04	PL B592 1	S. Eidelman <i>et al.</i>	(PDG Collab.)	REFID=49653
SOZZI	04	EPJ C36 37	M. Sozzi	(PISA)	REFID=51122
ADINOLFI	03	PL B566 61	M. Adinolfi <i>et al.</i>	(KLOE Collab.)	REFID=49491
ALAVI-HARATI	03	PR D67 012005	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=49244
Also		PR D70 079904 (errat.)	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=50236
ALAVI-HARATI	03B	PRL 90 141801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=49355
LAI	03	PL B551 7	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49148
LAI	03C	EPJ C30 33	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=49502
ALAVI-HARATI	02	PRL 88 181601	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48706
ALAVI-HARATI	02C	PRL 89 211801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48996
BATLEY	02	PL B544 97	J.R. Batley <i>et al.</i>	(CERN NA48 Collab.)	REFID=48919
CIRIGLIANO	02	EPJ C23 121	V. Cirigliano <i>et al.</i>	(VIEN, VALE, MARS)	REFID=50523
LAI	02B	PL B536 229	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=48763
ALAVI-HARATI	01	PRL 86 397	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48025
ALAVI-HARATI	01B	PRL 86 761	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48034
ALAVI-HARATI	01D	PRL 86 5425	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48148
ALAVI-HARATI	01E	PRL 87 021801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48176
ALAVI-HARATI	01F	PR D64 012003	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48178
ALAVI-HARATI	01G	PRL 87 071801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48209
ALAVI-HARATI	01H	PRL 87 111802	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48250
ALAVI-HARATI	01J	PR D64 112004	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=48424
ANGELOPO...	01	PL B503 49	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=48097
ANGELOPO...	01B	EPJ C22 55	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=48507
LAI	01B	PL B515 261	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=48280
LAI	01C	EPJ C22 231	A. Lai <i>et al.</i>	(CERN NA48 Collab.)	REFID=48510
ALAVI-HARATI	00	PR D61 072006	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47541
ALAVI-HARATI	00B	PRL 84 408	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47543
ALAVI-HARATI	00D	PRL 84 5279	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47632
ALAVI-HARATI	00E	PR D62 112001	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47821
AMBROSE	00	PRL 84 1389	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)	REFID=47540
APOSTOLA...	00	PL B473 186	A. Apostolakis <i>et al.</i>	(CPLEAR Collab.)	REFID=47542
PDG	00	EPJ C15 1	D.E. Groom <i>et al.</i>	(PDG Collab.)	REFID=47469
ALAVI-HARATI	99B	PRL 83 917	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47074
ALAVI-HARATI	99D	PRL 83 22	A. Apostolakis <i>et al.</i>	(FNAL KTeV Collab.)	REFID=47095
APOSTOLA...	99C	PL B458 545	A. Apostolakis <i>et al.</i>	(CPLEAR Collab.)	REFID=47042
Also		EPJ C18 41	A. Apostolakis <i>et al.</i>	(CPLEAR Collab.)	REFID=48038
FANTI	99B	PL B458 553	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)	REFID=47043
FANTI	99C	PL B465 335	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)	REFID=47251
MURAKAMI	99	PL B463 333	K. Murakami <i>et al.</i>	(KEK E162 Collab.)	REFID=47228
ADAMS	98	PRL 80 4123	J. Adams <i>et al.</i>	(FNAL KTeV Collab.)	REFID=46014
AMBROSE	98	PRL 81 4309	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)	REFID=46494
AMBROSE	98B	PRL 81 5734	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)	REFID=46696
ANGELOPO...	98B	PL B420 191	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46030
ANGELOPO...	98C	EPJ C5 389	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46264
ANGELOPO...	98D	PL B444 38	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46539
Also		EPJ C22 55	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=48507
ANGELOPO...	98E	PL B444 43	A. Angelopoulos <i>et al.</i>	(CPLEAR Collab.)	REFID=46540
ARISAKA	98	PL B432 230	K. Arisaka <i>et al.</i>	(FNAL E799 Collab.)	REFID=46071
BENDER	98	PL B418 411	M. Bender <i>et al.</i>	(CERN NA48 Collab.)	REFID=46025
DAMBROSIO	98	PL B423 385	G. D'Ambrusio, G. Isidori, J. Portoles		REFID=52185
SETZU	98	PL B420 205	M.G. Setzu <i>et al.</i>		REFID=46031
TAKEUCHI	98	PL B443 409	Y. Takeuchi <i>et al.</i>	(KYOT, KEK, HIRO)	REFID=46537
FANTI	97	ZPHY C76 653	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)	REFID=45792
NOMURA	97	PL B408 445	T. Nomura <i>et al.</i>	(KYOT, KEK, HIRO)	REFID=45660
ADLER	96B	ZPHY C70 211	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44818
ADLER	96C	PL B369 367	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44836
GU	96	PRL 76 4312	P. Gu <i>et al.</i>	(RUTG, UCLA, EFI, COLO+)	REFID=44805
LEBER	96	PL B369 69	F. Leber <i>et al.</i>	(MAINZ, CERN, EDIN, ORSAY+)	REFID=44829
PDG	96	PR D54 1	R. M. Barnett <i>et al.</i>	(PDG Collab.)	REFID=44495
ADLER	95	PL B363 237	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44561
ADLER	95B	PL B363 243	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=44562
AKAGI	95	PR D51 2061	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)	REFID=44147
BARR	95	ZPHY C65 361	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=44179
BARR	95C	PL B358 399	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=44473
HEINSON	95	PR D51 985	A.P. Heinson <i>et al.</i>	(BNL E791 Collab.)	REFID=44138
KREUTZ	95	ZPHY C65 67	A. Kreutz <i>et al.</i>	(SIEG, EDIN, MAINZ, ORSAY+)	REFID=44159
MATTHEWS	95	PRL 75 2803	J.N. Matthews <i>et al.</i>	(RUTG, EFI, ELMT+)	REFID=44487
SCHWINGEN...	95	PRL 74 4376	B. Schwingenheuer <i>et al.</i>	(EFI, CHIC+)	REFID=44259
SPENCER	95	PRL 74 3323	M.B. Spencer <i>et al.</i>	(UCLA, EFI, COLO+)	REFID=44198
BARR	94	PL B328 528	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=43828
GU	94	PRL 72 3000	P. Gu <i>et al.</i>	(RUTG, UCLA, EFI, COLO+)	REFID=43825
NAKAYA	94	PRL 73 2169	T. Nakaya <i>et al.</i>	(OSAK, UCLA, EFI, COLO+)	REFID=43993
ROBERTS	94	PR D50 1874	D. Roberts <i>et al.</i>	(UCLA, EFI, COLO+)	REFID=43867
AKAGI	93	PR D47 2644	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)	REFID=43283
ARISAKA	93	PRL 70 1049	K. Arisaka <i>et al.</i>	(BNL E791 Collab.)	REFID=43206
ARISAKA	93B	PRL 71 3910	K. Arisaka <i>et al.</i>	(BNL E791 Collab.)	REFID=43637
BARR	93D	PL B317 233	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LALO+)	REFID=43581
GIBBONS	93	PRL 70 1199	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=43209
Also		PRL D55 6625	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=45465
GIBBONS	93B	PRL 70 1203	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=43210

GIBBONS	93C	Thesis RX-1487	L.K. Gibbons	(CHIC)	REFID=43829	
Also		PR D55 625	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=45465	
HARRIS	93	PRL 71 3914	D.A. Harris <i>et al.</i>	(EFI, UCLA, COLO+)	REFID=43638	
HARRIS	93B	PRL 71 3918	D.A. Harris <i>et al.</i>	(EFI, UCLA, COLO+)	REFID=43639	
MAKOFF	93	PRL 70 1591	G. Makoff <i>et al.</i>	(FNAL E731 Collab.)	REFID=43270	
Also		PR 75 2069 (errat.)	G. Makoff <i>et al.</i>		REFID=44426	
RAMBERG	93	PRL 70 2525	E. Ramberg <i>et al.</i>	(FNAL E731 Collab.)	REFID=43263	
RAMBERG	93B	PRL 70 2529	E.J. Ramberg <i>et al.</i>	(FNAL E731 Collab.)	REFID=43264	
VAGINS	93	PRL 71 35	M.R. Vagins <i>et al.</i>	(BNL E845 Collab.)	REFID=43364	
ADLER	92B	PL B286 180	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=42122	
Also		SJNP 55 840	R. Adler <i>et al.</i>	(CPLEAR Collab.)	REFID=42110	
BARR	92	PL B284 440	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=42092	
MORSE	92	PR D45 36	W.M. Morse <i>et al.</i>	(BNL, YALE, VASS)	REFID=41922	
PDG	92	PR D45 S1	K. Hikasa <i>et al.</i>	(KEK, LBL, BOST+)	REFID=41900	
SOMALWAR	92	PRL 68 2580	S.V. Somalwar <i>et al.</i>	(FNAL E731 Collab.)	REFID=41971	
AKAGI	91B	PRL 67 2618	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)	REFID=41756	
BARR	91	PL B259 389	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=41489	
HEINSON	91	PR D44 1	A.P. Heinson <i>et al.</i>	(UCI, UCLA, LANL+)	REFID=41517	
PAPADIMITR...	91	PR D44 573	V. Papadimitriou <i>et al.</i>	(FNAL E731 Collab.)	REFID=41556	
BARKER	90	PR D41 3546	A.R. Barker <i>et al.</i>	(FNAL E731 Collab.)	REFID=41257	
Also		PR 61 2661	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)	REFID=40624	
BARR	90B	PL B240 283	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=41212	
BARR	90C	PL B242 523	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=41316	
CAROSI	90	PL B237 303	R. Carosi <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=41118	
KARLSSON	90	PR 64 2976	M. Karlsson <i>et al.</i>	(FNAL E731 Collab.)	REFID=41186	
OHL	90	PRL 64 2755	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)	REFID=41180	
OHL	90B	PRL 65 1407	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)	REFID=41303	
PATTERSON	90	PRL 64 1491	J.R. Patterson <i>et al.</i>	(FNAL E731 Collab.)	REFID=41129	
INAGAKI	89	PR D40 1712	T. Inagaki <i>et al.</i>	(KEK, TOKY, KYOT)	REFID=40851	
MATHIAZHA...	89	PRL 63 2181	C. Mathiazagan <i>et al.</i>	(UCI, UCLA, LANL+)	REFID=40975	
MATHIAZHA...	89B	PRL 63 2185	C. Mathiazagan <i>et al.</i>	(UCI, UCLA, LANL+)	REFID=40976	
WAHL	89	CERN-EP/89-86	H. Wahl	(CERN)	REFID=41130	
BARR	88	PL B214 303	G.D. Barr <i>et al.</i>	(CERN, EDIN, MAINZ, LAZO+)	REFID=40658	
BURKHARDT	88	PL B206 169	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MAINZ+)	REFID=40545	
JASTRZEM...	88	PRL 61 2300	E. Jastrzembski <i>et al.</i>	(BNL, YALE)	REFID=40622	
WOODS	88	PRD 60 1695	M. Woods <i>et al.</i>	(FNAL E731 Collab.)	REFID=40546	
BURKHARDT	87	PL B199 139	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MAINZ+)	REFID=40237	
ARONSON	86	PR D33 3180	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)	REFID=11410	
Also		PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)	REFID=11411	
PDG	86C	PL 170B 132	M. Aguilar-Benitez <i>et al.</i>	(CERN, CIT+)	REFID=41169	
COUPAL	85	PR 55 566	D.P. Coupal <i>et al.</i>	(CHIC, SACL)	REFID=11409	
BALATS	83	SJNP 38 556	M.Y. Balats <i>et al.</i>	(ITEP)	REFID=11405	
Translated from YAF 38 927.						
BERGSTROM	83	PL 131B 229	L. Bergstrom, E. Masso, P. Singer	(CERN)	REFID=41926	
ARONSON	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)	REFID=11411	
ARONSON	82B	PRL 48 1306	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11401	
Also		PL 116B 73	E. Fischbach <i>et al.</i>	(PURD, BNL, CHIC)	REFID=11402	
Also		PR D28 476	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11403	
Also		PR D28 495	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)	REFID=11404	
PDG	82B	PL 111B 70	M. Roos <i>et al.</i>	(HELS, CIT, CERN)	REFID=41156	
BIRULEV	81	NP B182 1	V.K. Birulev <i>et al.</i>	(JINR)	REFID=11399	
Also		SJNP 31 622	V.K. Birulev <i>et al.</i>	(JINR)	REFID=11400	
Translated from YAF 31 1204.						
CARROLL	80B	PRL 44 529	A.S. Carroll <i>et al.</i>	(BNL, ROCH)	REFID=11395	
CARROLL	80C	PL 96B 407	A.S. Carroll <i>et al.</i>	(BNL, ROCH)	REFID=11396	
CHO	80	PR D22 2688	Y. Cho <i>et al.</i>	(ANL, CMU)	REFID=11397	
MORSE	80	PR D21 1750	W.M. Morse <i>et al.</i>	(BNL, YALE)	REFID=11398	
CHRISTENS...	79	PRL 43 1209	J.H. Christenson <i>et al.</i>	(NYU)	REFID=11388	
SCHMIDT	79	PRL 43 556	M.P. Schmidt <i>et al.</i>	(YALE, BNL)	REFID=11391	
HILL	78	PL 73B 483	D.G. Hill <i>et al.</i>	(BNL, SLAC, SBER)	REFID=11386	
CHO	77	PR D15 587	Y. Cho <i>et al.</i>	(ANL, CMU)	REFID=11379	
CLARK	77	PR D15 553	A.R. Clark <i>et al.</i>	(LBL)	REFID=11380	
Also		Thesis LBL-4275	G. Shen	(LBL)	REFID=11381	
DEVOE	77	PR D16 565	R. Devoe <i>et al.</i>	(EFI, ANL)	REFID=11382	
PEACH	77	NP B127 399	K.J. Peach <i>et al.</i>	(BGNA, EDIN, GLAS+)	REFID=11384	
BIRULEV	76	SJNP 24 178	V.K. Birulev <i>et al.</i>	(JINR)	REFID=11371	
Translated from YAF 24 340.						
COOMBES	76	PRL 37 249	R.W. Coombes <i>et al.</i>	(STAN, NYU)	REFID=11372	
GJESDAL	76	NP B109 118	G. Gjesdal <i>et al.</i>	(CERN, HEIDH)	REFID=11376	
BALDO...	75	NC 25A 688	M. Baldo-Ceolin <i>et al.</i>	(PADO, WISC)	REFID=11108	
BLUMENTHAL	75	PRL 34 164	R.B. Blumenthal <i>et al.</i>	(PENN, CHIC, TEMP)	REFID=11367	
BUCHANAN	75	PR D11 457	C.D. Buchanan <i>et al.</i>	(UCLA, SLAC, JHU)	REFID=11368	
CARTHERS	75	PRL 34 1244	W.C.J. Carithers <i>et al.</i>	(COLU, NYU)	REFID=11109	
SMITH	75B	Thesis UCSD unpub.		J.G. Smith	(UCSD)	REFID=11370
BISI	74	PL 50B 504	V. Bisi, M.I. Ferrero	(TORI)	REFID=11346	
DONALDSON	74	Thesis SLAC-0184		G. Donaldson	(SLAC)	REFID=11374
Also		PR D14 2839	G. Donaldson <i>et al.</i>	(SLAC)	REFID=11373	
DONALDSON	74B	PR D9 2960	G. Donaldson <i>et al.</i>	(SLAC, UCSC)	REFID=11351	
Also		PRL 31 337	G. Donaldson <i>et al.</i>	(SLAC, UCSC)	REFID=11352	
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Also		Thesis CERN Int. 74-4	V. Luth	(CERN, HEIDH)	REFID=11356	
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Also		PL 52B 119	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)	REFID=11358	
GEWENIGER	74C	PL 52B 108	C. Geweniger <i>et al.</i>	(CERN, HEIDH)	REFID=11359	
GJESDAL	74	PL 52B 113	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)	REFID=11360	
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Also		Thesis COO-3072-13	R.C. Webb	(PRIN)	REFID=11334	
HART	73	NP B66 317	J.C. Hart <i>et al.</i>	(CAVE, RHEL)	REFID=11335	
MALLARY	73	PR D7 1953	M.L. Mallary <i>et al.</i>	(CIT)	REFID=11103	
Also		PRL 25 1214	F.J. Sciulli <i>et al.</i>	(CIT)	REFID=11337	
MCCARTHY	73	PR D7 687	R.L. McCarthy <i>et al.</i>	(LBL)	REFID=11338	
Also		PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)	REFID=11339	
Also		Thesis LBL-550	R.L. McCarthy	(LBL)	REFID=11340	
MESSNER	73	PRL 30 876	R. Messner <i>et al.</i>	(COLO, SLAC, UCSC)	REFID=11341	
SANDWEISS	73	PRL 30 1002	J. Sandweiss <i>et al.</i>	(YALE, ANL)	REFID=11343	
WILLIAMS	73	PRL 31 1521	H.H. Williams <i>et al.</i>	(BNL, YALE)	REFID=11344	
ASHFORD	72	PL 38B 47	V.A. Ashford <i>et al.</i>	(UCSD)	REFID=11301	
BANNER	72B	PRL 29 237	M. Banner <i>et al.</i>	(PRIN)	REFID=11303	
BARMIN	72B	SJNP 15 638	V.V. Barmin <i>et al.</i>	(ITEP)	REFID=11305	
Translated from YAF 15 1152.						

BURGUN	72	NP B50 194	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)	REFID=11306
GRAHAM	72	NC 9A 166	M.F. Graham <i>et al.</i>	(ILL, NEAS)	REFID=11311
JAMES	72	NP B49 1	F. James <i>et al.</i>	(CERN, SACL, OSLO)	REFID=11090
KRENZ	72	LNC 4 213	W. Krenz <i>et al.</i>	(AACH, CERN, EDIN)	REFID=11314
MANN	72	PR D6 137	W.A. Mann <i>et al.</i>	(MASA, BNL, YALE)	REFID=11315
MANTSCH	72	NC 9A 160	P.M. Mantsch <i>et al.</i>	(ILL, NEAS)	REFID=11316
MCCARTHY	72	PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)	REFID=11339
PICCIONI	72	PRL 29 1412	R. Piccioni <i>et al.</i>	(SLAC)	REFID=11319
Also		PR D9 2939	R. Piccioni <i>et al.</i>	(RUTG, MASA)	REFID=11320
VOSBURGH	72	PR D6 1834	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)	REFID=11321
Also		PRL 26 866	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)	REFID=11322
BALATS	71	SJNP 13 53	M.Y. Balats <i>et al.</i>	(ITEP)	REFID=11276
		Translated from YAF 13 93.			
BARMIN	71	PL 35B 604	V.V. Barmin <i>et al.</i>	(ITEP)	REFID=11277
BURGUN	71	LNC 2 1169	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)	REFID=11279
CARNEGIE	71	PR D4 1	R.K. Carnegie <i>et al.</i>	(PRIN)	REFID=11280
CHAN	71	Thethesis LBL-350	J.H.S. Chan	(LBL)	REFID=11281
CHO	71	PR D3 1557	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)	REFID=11084
ENSTROM	71	PR D4 2629	J.E. Enstrom	(SLAC, STAN)	REFID=11289
Also		Thethesis SLAC-0125	J. Enstrom	(STAN)	REFID=11290
JAMES	71	PL 35B 265	F. James <i>et al.</i>	(CERN, SACL, OSLO)	REFID=11085
MEISNER	71	PR D3 59	G.W. Meisner <i>et al.</i>	(MASA, BNL, YALE)	REFID=11086
REPELLIN	71	PL 36B 603	J.P. Repellin <i>et al.</i>	(ORSAY, CERN)	REFID=11087
WEBBER	71	PR D3 64	B.R. Webber <i>et al.</i>	(LRL)	REFID=11296
Also		PRL 21 498	B.R. Webber <i>et al.</i>	(LRL)	REFID=11297
Also		Thesis UCRL 19226	B.R. Webber	(LRL)	REFID=11081
WOLFF	71	PL 36B 517	B. Wolff <i>et al.</i>	(ORSAY, CERN)	REFID=11299
ALBROW	70	PL 33B 516	M.G. Albrow <i>et al.</i>	(MCHS, DARE)	REFID=11252
ARONSON	70	PRL 25 1057	S.H. Aronson <i>et al.</i>	(EFI, ILLC, SLAC)	REFID=11253
BARMIN	70	PL 33B 377	V.V. Barmin <i>et al.</i>	(ITEP, JINR)	REFID=11254
BASILE	70	PR D2 78	P. Basile <i>et al.</i>	(SACL)	REFID=11255
BECHERRAWY	70	PR D1 1452	T. Becherrawy	(ROCH)	REFID=11033
BUCHANAN	70	PL 33B 623	C.D. Buchanan <i>et al.</i>	(SLAC, JHU, UCLA)	REFID=11256
Also		Private Comm.	A.J. Cox		REFID=11257
BUDAGOV	70	PR D2 815	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)	REFID=11258
Also		PL 28B 215	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)	REFID=11225
CHO	70	PR D1 3031	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)	REFID=11262
Also		PRL 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)	REFID=11263
CHOLLET	70	PL 31B 658	J.C. Chollet <i>et al.</i>	(CERN)	REFID=11264
CULLEN	70	PL 32B 523	M. Cullen <i>et al.</i>	(AACH, CERN, TORI)	REFID=11265
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Also		Thesis Nevis 179	J. Marx	(COLU)	REFID=11271
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Also		Thesis UCRL 19226	B.R. Webber	(LRL)	REFID=11081
BANNER	69	PR 188 2033	M. Banner <i>et al.</i>	(PRIN)	REFID=11071
Also		PRL 21 1103	M. Banner <i>et al.</i>	(PRIN)	REFID=11234
Also		PRL 21 1107	J.W. Cronin, J.K. Liu, J.E. Pilcher	(PRIN)	REFID=11235
BENNETT	69	PL 29B 317	S. Bennett <i>et al.</i>	(COLU, BNL)	REFID=11237
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PACIOTTI	69	Thesis UCRL 19446	M.A. Paciotti	(LRL)	REFID=11250
SAAL	69	Thesis	H.J. Saal	(COLU)	REFID=11251
ABRAMS	68B	PR 176 1603	R.J. Abrams <i>et al.</i>	(ILL)	REFID=11213
ARNOLD	68B	PL 28B 56	R.G. Arnold <i>et al.</i>	(CERN, ORSAY)	REFID=11214
BASILE	68B	PL 28B 58	P. Basile <i>et al.</i>	(SACL)	REFID=11220
BENNETT	68	PL 27B 244	S. Bennett <i>et al.</i>	(COLU, CERN)	REFID=11221
BLANPIED	68	PRL 21 1650	W.A. Blanpied <i>et al.</i>	(CASE, HARV, MCGI)	REFID=11223
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KULYUKINA	68	JETP 26 20	L.A. Kulyukina <i>et al.</i>	(JINR)	REFID=11229
		Translated from ZETF 53 29.			
KUNZ	68	Thesis PU-68-46	P.F. Kunz	(PRIN)	REFID=11230
BENNETT	67	PRL 19 993	S. Bennett <i>et al.</i>	(COLU)	REFID=11188
DEBOUARD	67	NC 52A 662	X. de Bouard <i>et al.</i>	(CERN)	REFID=11196
Also		PL 15 58	X. de Bouard <i>et al.</i>	(CERN, ORSAY, MPIM)	REFID=11197
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GINNSBERG	67	PR 162 1570	E.S. Ginsberg	(MASB)	REFID=11028
HILL	67	PR 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)	REFID=11263
HOPKINS	67	PRL 19 185	H.W.K. Hopkins, T.C. Bacon, F.R. Eisler	(BNL)	REFID=11206
NEFKENS	67	PR 157 1233	B.M.K. Nefkens <i>et al.</i>	(ILL)	REFID=11211
SCHMIDT	67	Thesis Nevis 160	P. Schmidt	(COLU)	REFID=11423
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Also		PR 156 1444	C.J.B. Hawkins	(YALE)	REFID=11181
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Also		PL 24B 75	J.P. Lowys <i>et al.</i>	(EPOL, ORSAY)	REFID=11152
BALDO...	65	NC 38 684	M. Baldo-Ceolin <i>et al.</i>	(PADO)	REFID=11153
FRANZINI	65	PR 140 B127	P. Franzini <i>et al.</i>	(COLU, RUTG)	REFID=11157
GUIDONI	65	Argonne Conf. 49	P. Guidoni <i>et al.</i>	(BNL, YALE)	REFID=11159
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		Translated from ZETF 46 1504.			
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		Translated from ZETF 46 59.			
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